

# Collisions of Nuclei: New Ideas for Hard Probes

**Rainer Fries**

Texas A&M University & RIKEN BNL



**RIKEN BNL**  
Research Center

Seminar, TIFR, Mumbai  
December 15, 2009

# Overview

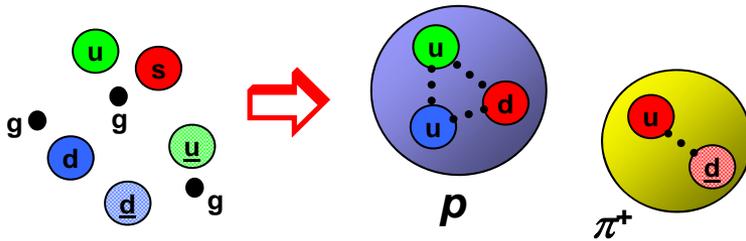
- Introduction: heavy ion collisions and hard probes
- Hadron chemistry and flavor conversions [With W. Liu,  
Phys.Rev.C77:054902,2008  
Phys.Rev.C78:037902,2008]
- Tomography + development of a new test environment [In progress, with R. Rodriguez ]
- Summary

# Introduction



# Matter in Extreme Conditions

- Evolution of the universe:
  - Microseconds after the Big Bang we start with a hot soup of matter
  - Quarks, gluons (and leptons)



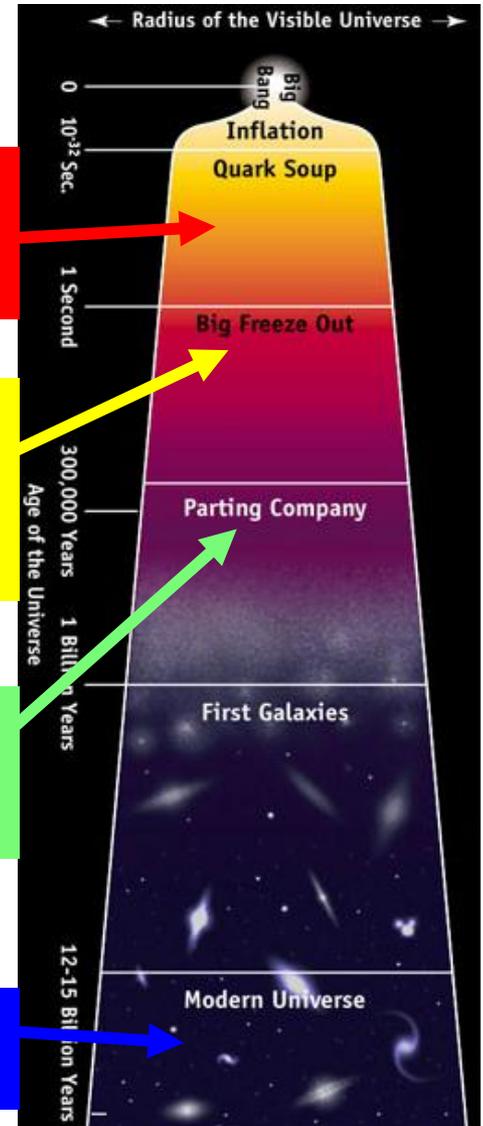
- Phase transition to hadrons (and leptons)
- Temperature  $T \sim 10^{12}$  K

Hadrons melt:  
quark gluon  
plasma (QGP)

Too hot for  
nucleons to be  
bound inside  
nuclei

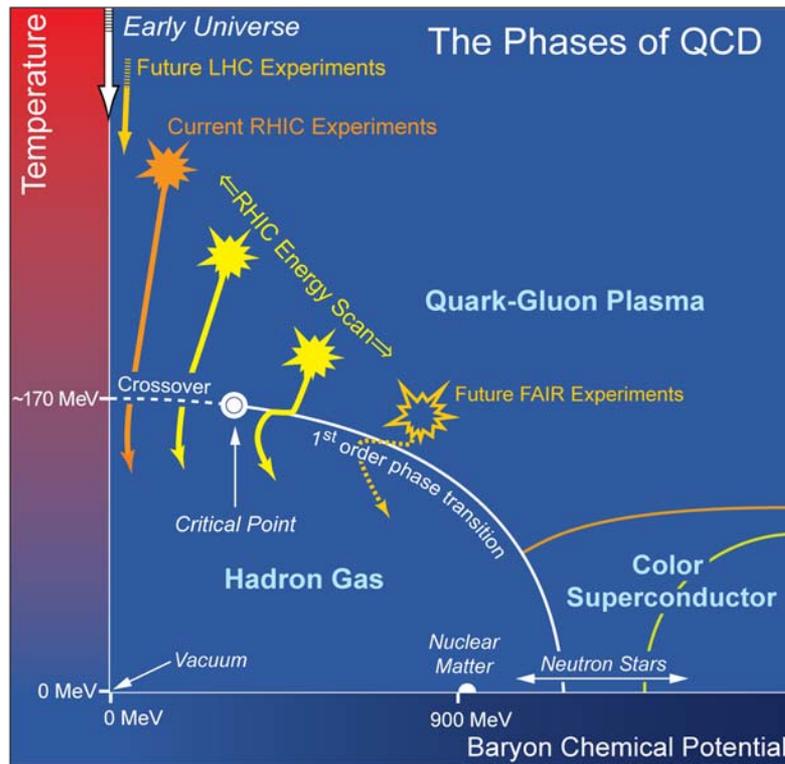
Molecules, atoms  
dissolve:  
EM plasma

Today's  
universe: 2.7 K



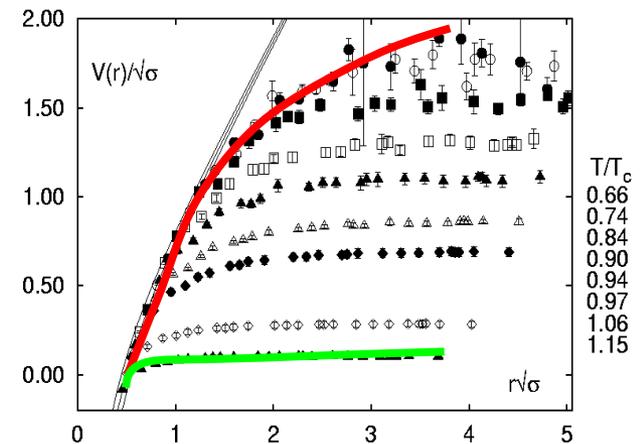
# Quark Gluon Plasma

- Asymptotic freedom & lattice QCD predict deconfinement of quarks and gluons above a critical temperature  $T_c$  + restoration of chiral symmetry.

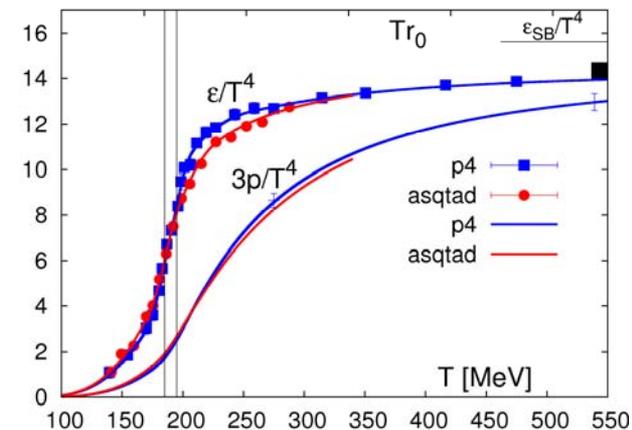


- Crossover at  $\mu = 0$ .

Static quark potential (Karsch et al.)



Energy density  $\varepsilon(T)$ , pressure  $p(T)$

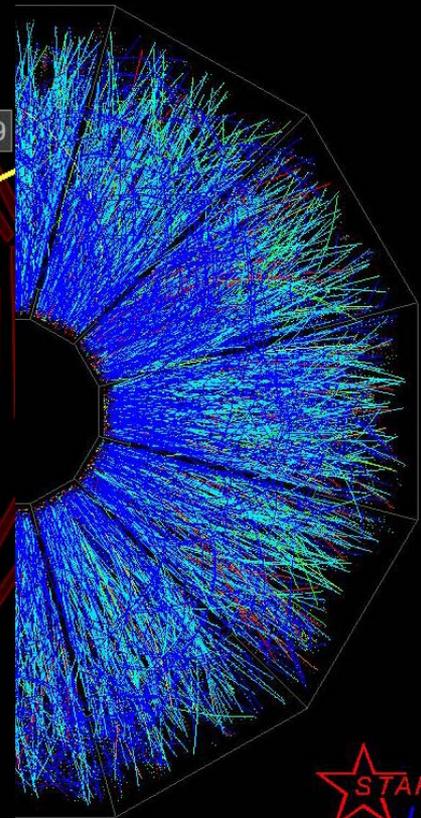
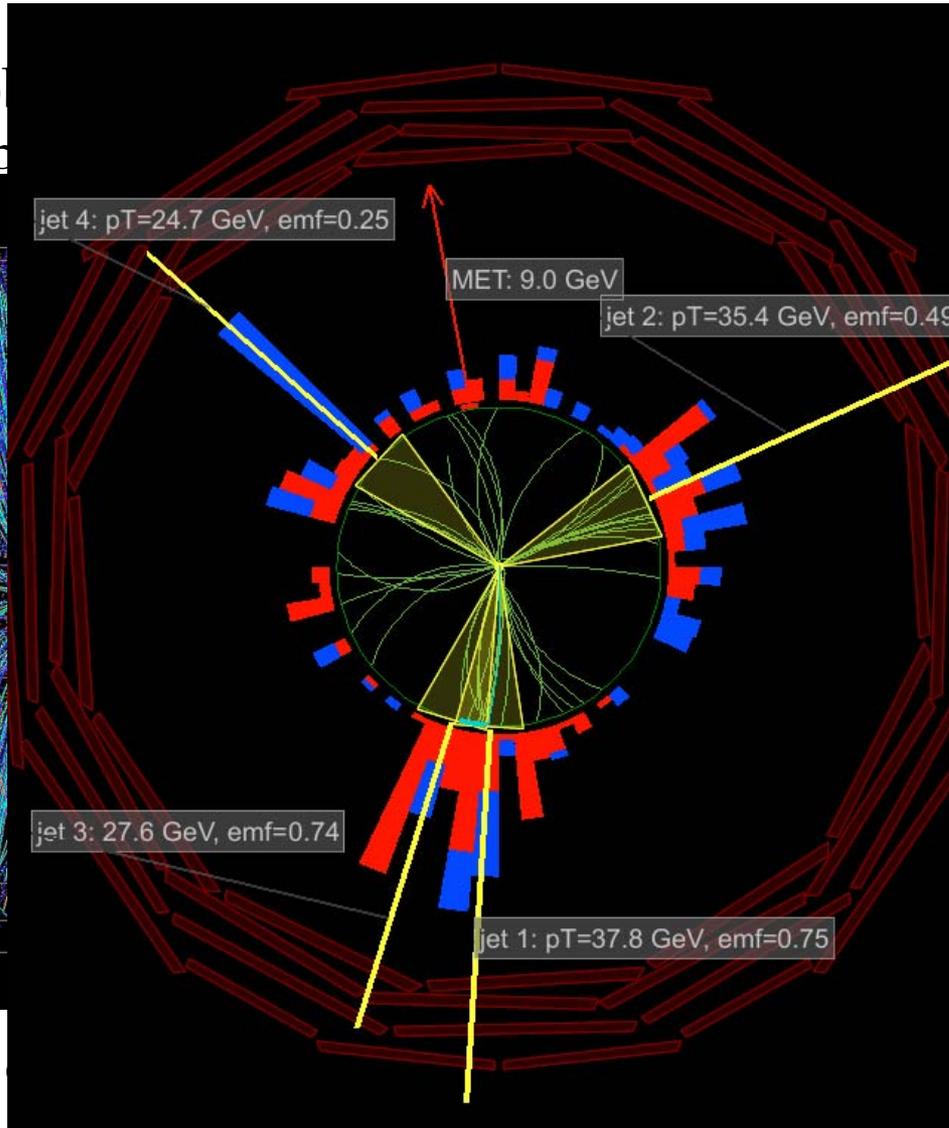
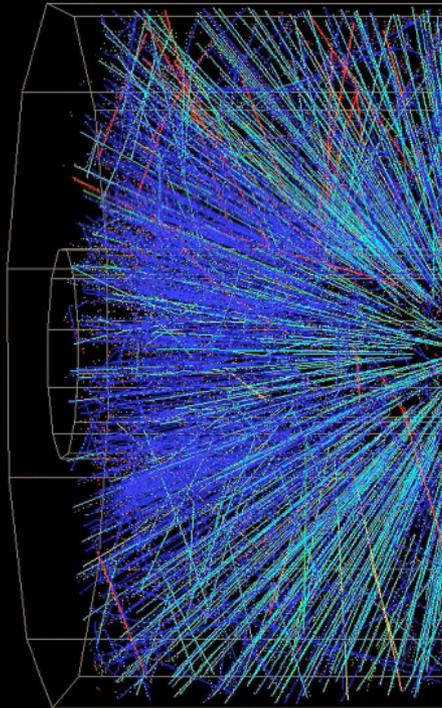


# How to Produce $10^{12}$ K Matter?

- In nature: not of extreme energy  
cosmic rays imp

extreme energy

(100 AGeV) Au →

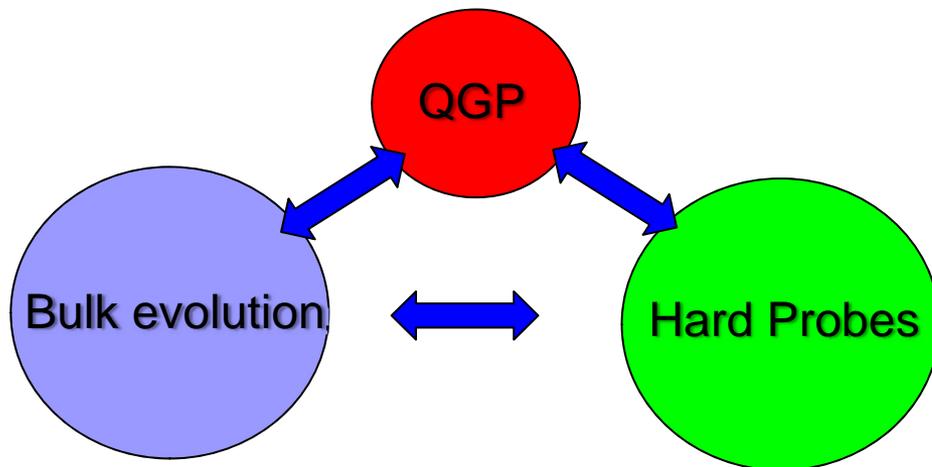
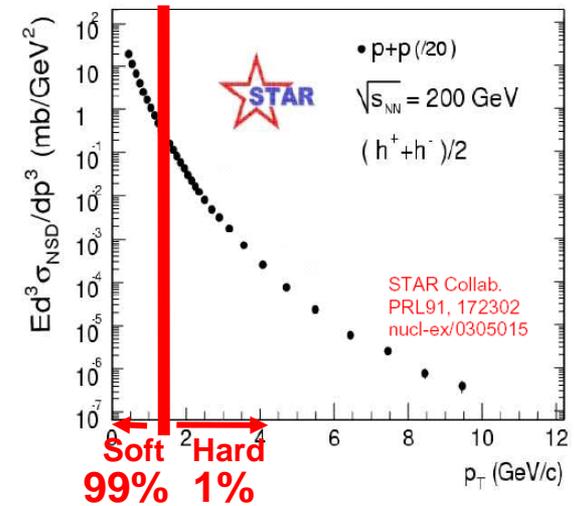


- In the lab: high

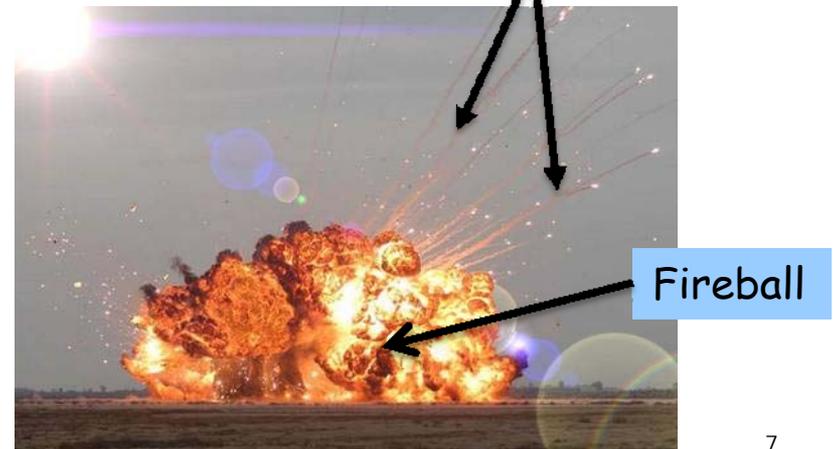


# Sketch of a HE Nuclear Collision

- Where is the QGP?
- Hierarchy in Momentum Space:
- Soft particles ( $P_T < 1-2$  GeV): Bulk fireball
  - Equilibration, thermalization  $\rightarrow$  Quark Gluon Plasma
  - Non-perturbative dynamics
- Hard particles ( $P_T > 1-2$  GeV): Rare probes
  - Hard probes of the bulk fireball (QGP)
  - Creation: perturbative, FSI: maybe perturbative.

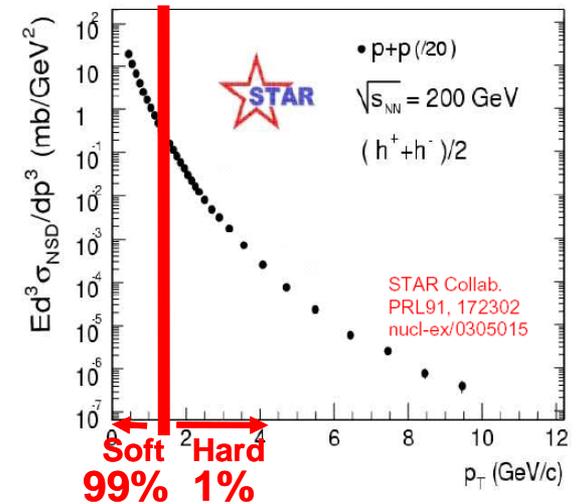


Some particles accelerated much more: fast probes.



# Sketch of a HE Nuclear Collision

- Where is the QGP?
- Hierarchy in Momentum Space:
- Soft particles ( $P_T < 1-2$  GeV): Bulk fireball
  - Equilibration, thermalization  $\rightarrow$  Quark Gluon Plasma
  - Non-perturbative dynamics
- Hard particles ( $P_T > 1-2$  GeV): Rare probes
  - Hard probes of the bulk fireball (QGP)
  - Creation: perturbative, FSI: maybe perturbative.



< 1fm/c

~ 10 fm/c

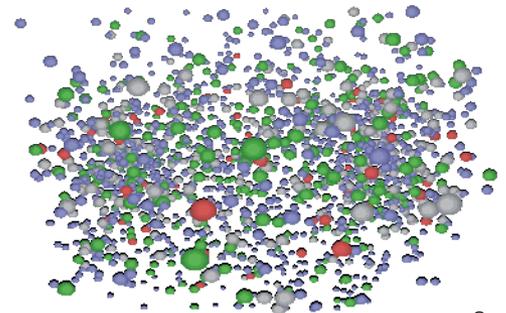
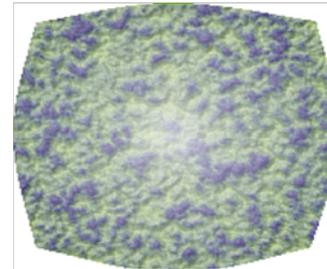
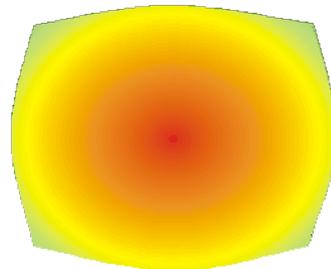
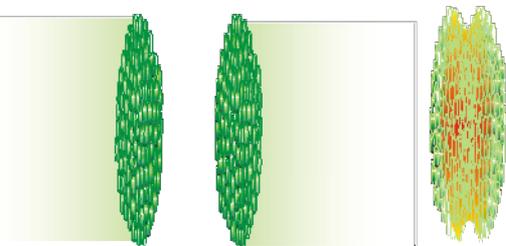
Time

Initial stage

Quark Gluon Plasma

Hadronization

Hadronic Phase

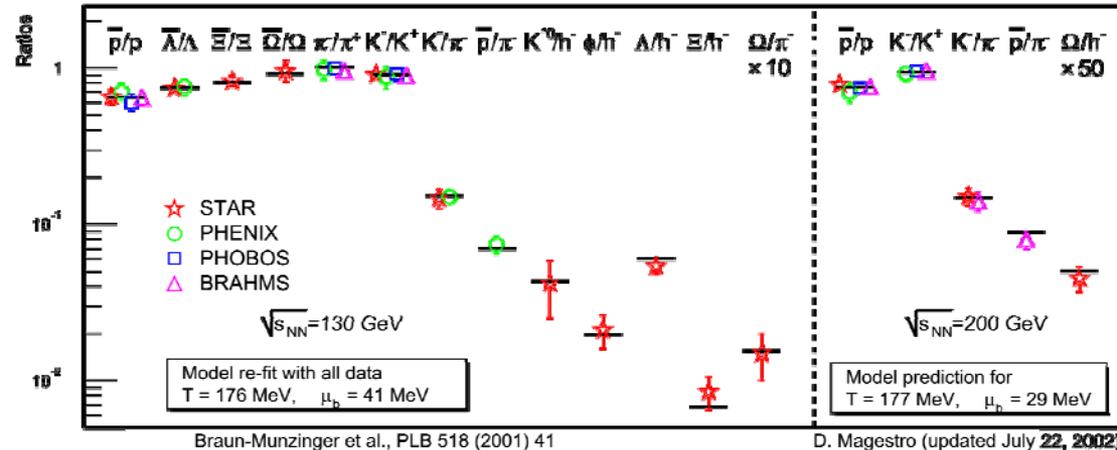


# Bulk Fireball: Temperature and Pressure

## ■ Hadron ratios: thermometer

- Chemical freeze-out around 175 MeV
- Low net baryon number

$$n_i(T, \mu) = \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{e^{(E_i - \mu_i B_i - \mu_s S_i)/T} \pm 1}$$

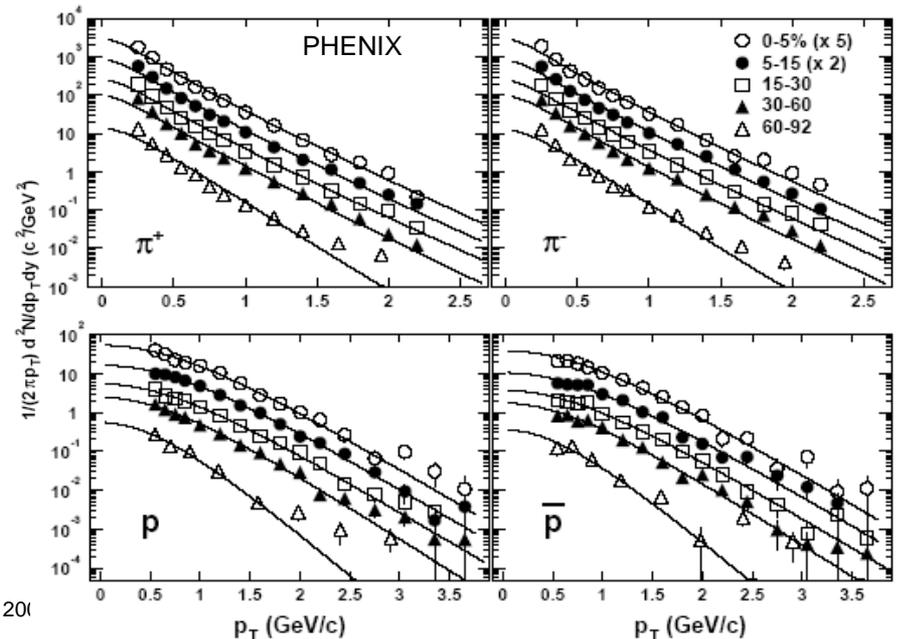


Braun-Munzinger et al., PLB 518 (2001) 41

D. Magestro (updated July 22, 2002)

## ■ Low- $P_T$ spectra: explosion-like blastwave

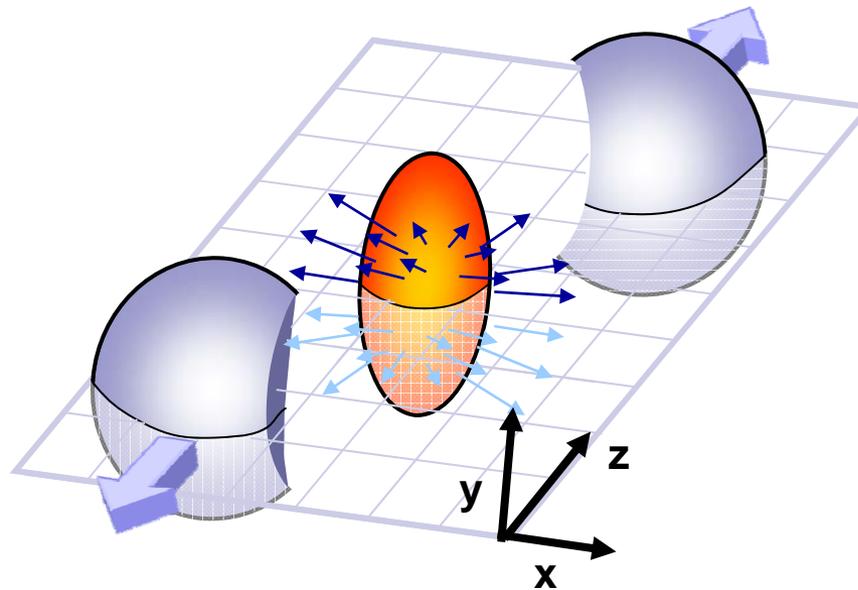
- Well described by hydrodynamic evolution.
- Expansion velocity  $\beta_L \sim 1, \beta_T \sim 0.5 - 0.7$



TIFR 201

# Bulk Fireball: $v_2$ Phenomenon

- Finite impact parameter  $b > 0$ :
  - Spatial anisotropy in the initial state
  - Momentum anisotropy in the final state



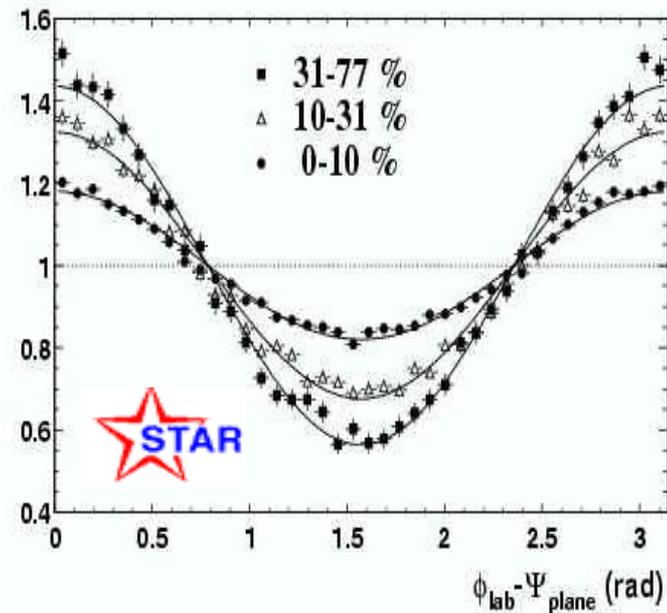
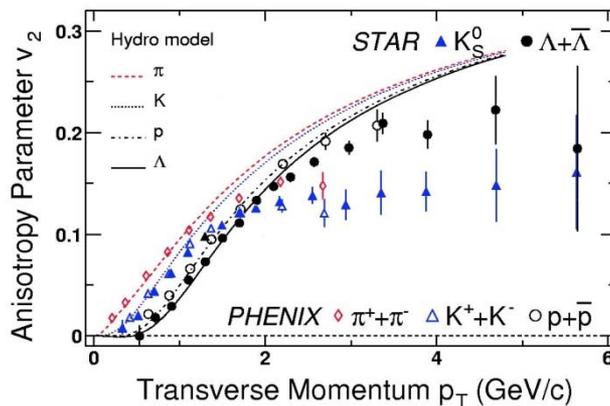
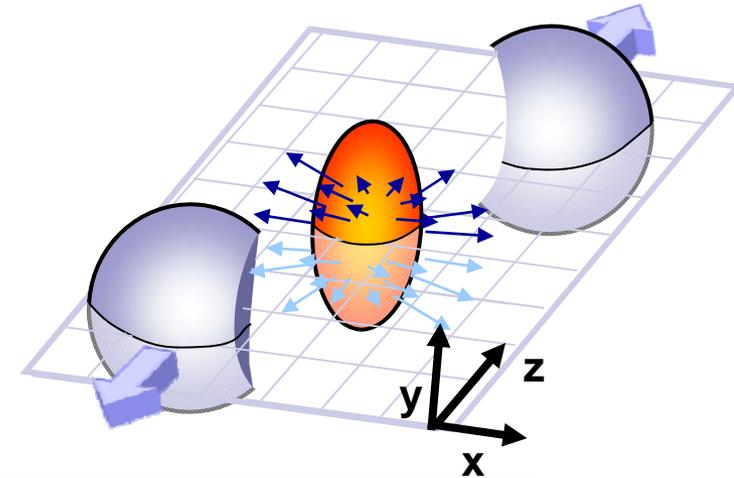
# Bulk Fireball: $v_2$ Phenomenon

- Finite impact parameter  $b > 0$ :
  - Spatial anisotropy in the initial state
  - Momentum anisotropy in the final state

- Fourier analysis

$$\frac{dN}{P_T dP_T d\varphi} = \frac{dN}{2\pi P_T dP_T} \left[ 1 + 2 \sum_n v_n(P_T) \cos(n\varphi) \right]$$

- $v_2$  = second harmonic (“elliptic flow”)
- Described very well by hydrodynamics



# Hard Probes: Jet Quenching

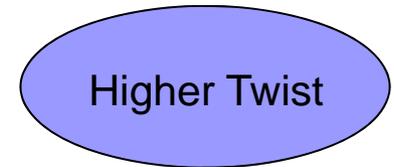
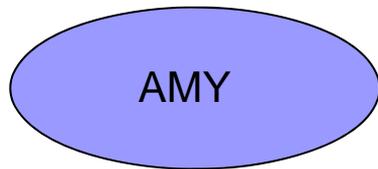
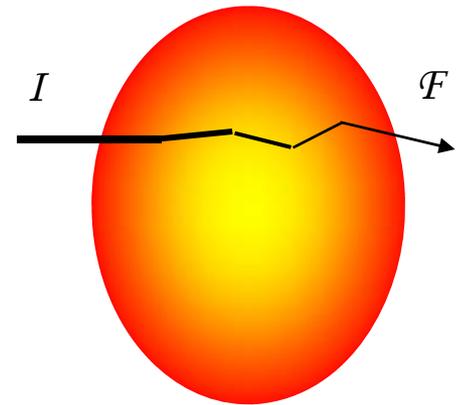
- Simplest possible probe: measure opacity of the medium
  - Drag force on QCD jets or hadrons = jet quenching
  - Most models: energy loss of the leading parton.
  - Related to broadening in transverse direction.

- Energy loss determined by the momentum transfer in collisions

- Sensitive to transport coefficient  $\hat{q} = \frac{\mu^2}{\lambda}$

= momentum transfer squared per mean free path/collision.

- Several calculations on the market using different sets of assumptions, e.g.



Perturbative plasma in the high temperature limit



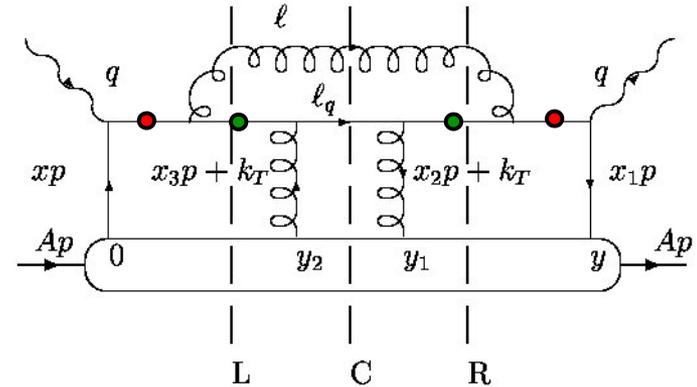
Extrapolated from DIS off large nuclei ( $e+A \rightarrow h+X$ )

# Energy Loss

- Example: higher twist
  - Compute modification to evolution equations of fragmentation functions in DIS on large nuclei.

$$\tilde{D}_{q/h}(z_h, \mu^2) = D_{q/h}(z_h, \mu^2) + \int_0^{\mu^2} \frac{dl_T^2}{l_T^2} \frac{\alpha_s}{2\pi} \int \frac{dz}{z} \times \left[ \Delta\gamma_{q \rightarrow qg}(z, x, l_T^2) D_{q/h}\left(\frac{z_h}{z}\right) + \Delta\gamma_{q \rightarrow gq}(z, x, l_T^2) D_{g/h}\left(\frac{z_h}{z}\right) \right]$$

$$\Delta\gamma_{q \rightarrow qg}(z, x, l_T^2) = \frac{2\pi\alpha_s C_A}{N_c l_T^2 f_{q/A}(x)} \left[ \frac{1+z^2}{(1-z)_+} T_{qg}(x, x_L) + \delta(1-z) \Delta T_{qg}(x, l_T^2) \right]$$



$$\frac{T_{qg}}{f_q} \sim \text{number of gluon scattering partners} \sim \hat{q}L$$

- Destructive interference between poles  $\rightarrow$  LPM effect

- Expected shift in energy  $\langle \Delta z \rangle = \int_0^{Q^2} \frac{dl_T^2}{l_T^2} \int_0^1 dz \frac{\alpha_s}{2\pi} z \Delta\gamma \sim \int \frac{dx_L}{x_L^2} R_A \sim \frac{R_A}{x_A} \sim A^{2/3}$

- Extrapolate to nuclear collisions.

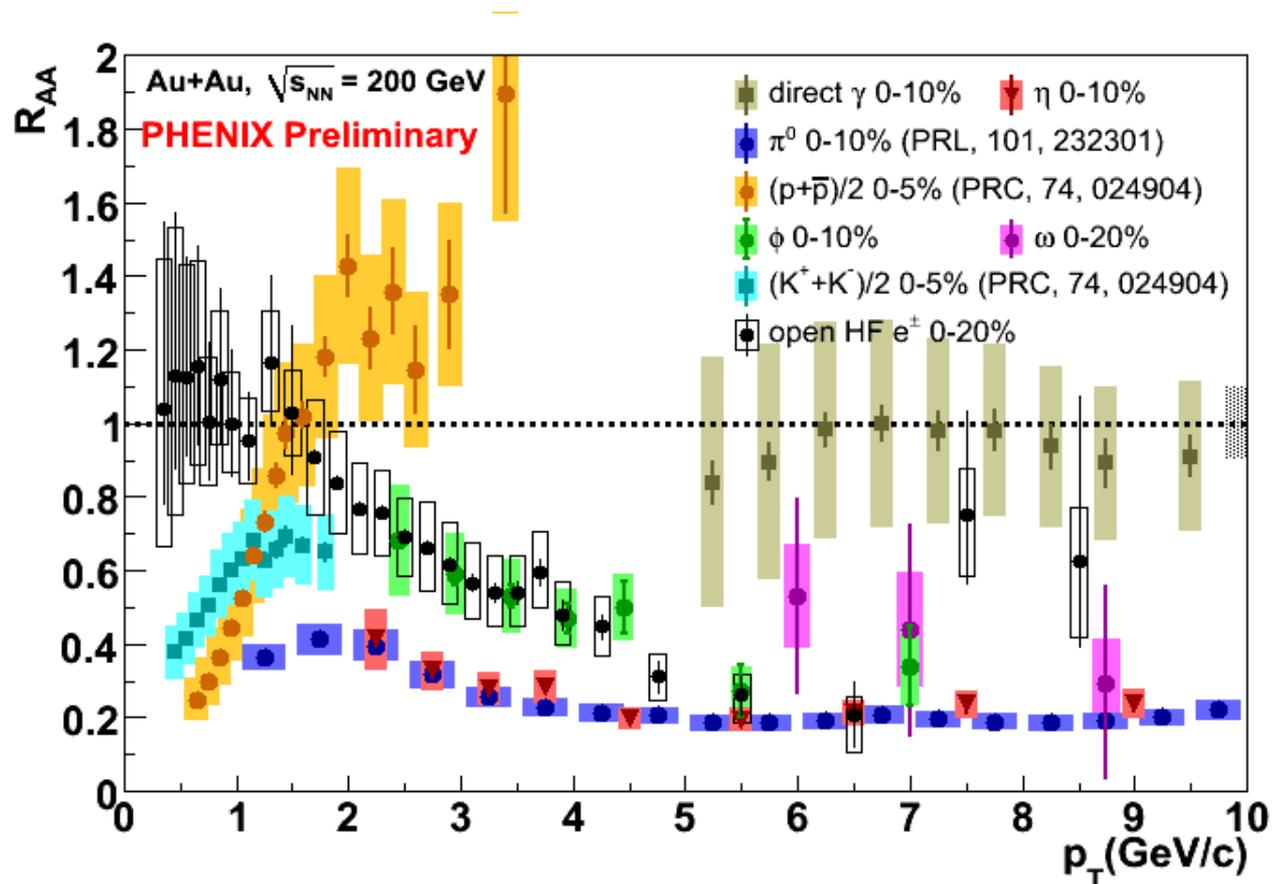
# Jet Quenching: Results

- RHIC: dramatic suppression effect for single hadrons

$$R_{AA} = \frac{dN_{AA} / dP_T}{N_{coll} dN_{NN} / dP_T}$$

Nuclear modification factor

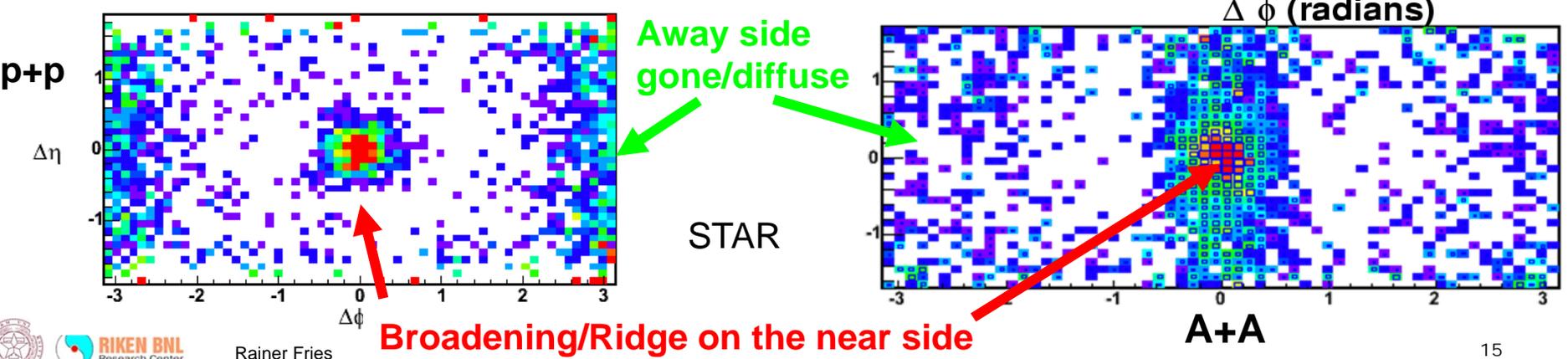
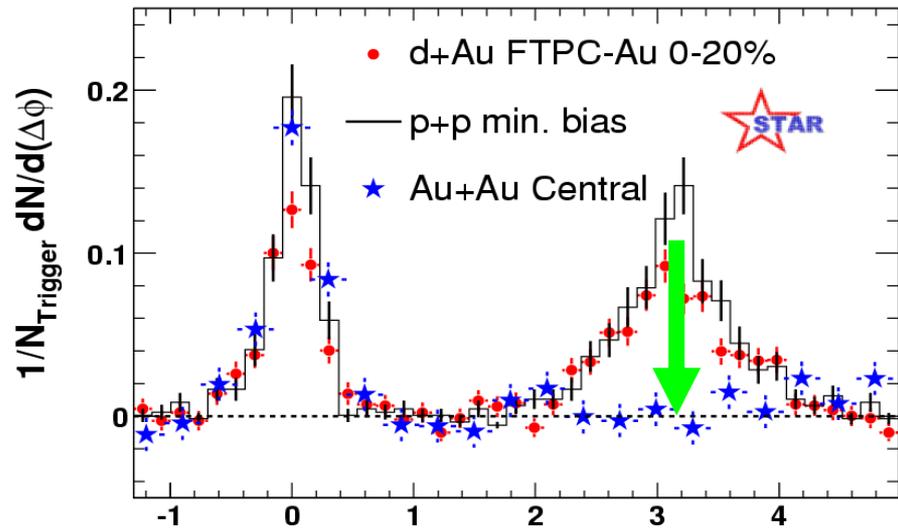
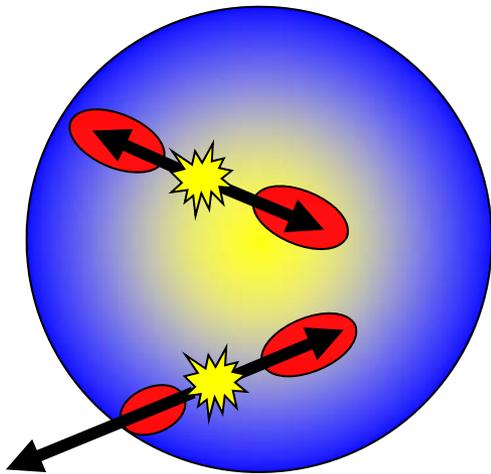
Factor 4 ...5  
suppression  
of the particle yield  
for  $P_T > 2$  GeV



# Jets: Correlations

- Away-side jets vanish

- Trigger on a high  $P_T$  hadron and look for associated hadron as a function of relative azimuthal angle and rapidity



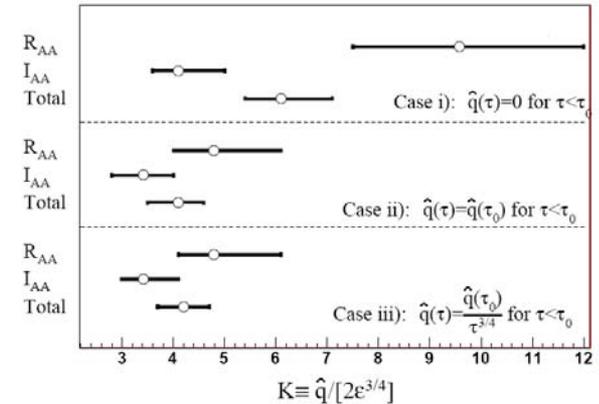
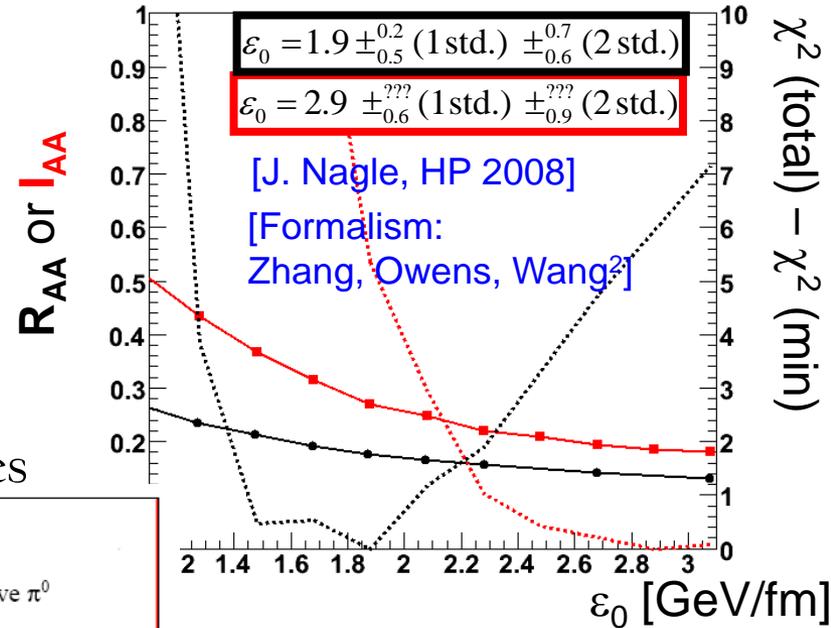
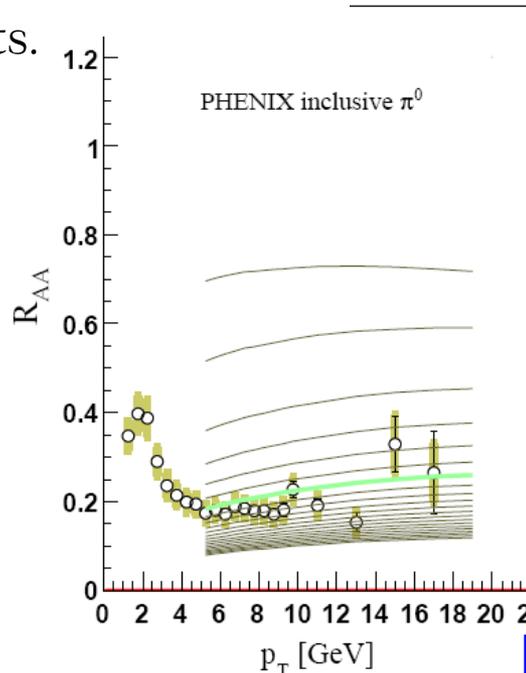
# Towards Precision Measurements (?)

- Fits of  $\hat{q}$  to data have begun.
- Different energy loss models give vastly different results. [S.A. Bass et al.]

$\hat{q}(\vec{r}, \tau)$	ASW	HT	AMY
scales as	$\hat{q}_0$	$\hat{q}_0$	$\hat{q}_0$
$T(\vec{r}, \tau)$	10 GeV <sup>2</sup> /fm	2.3 GeV <sup>2</sup> /fm	4.1 GeV <sup>2</sup> /fm

- Within a fixed model different observables give incompatible results.

- Lots of details matter!
  - Calibration (shadowing, Cronin effect)
  - Treatment of the initial fireball
  - ...

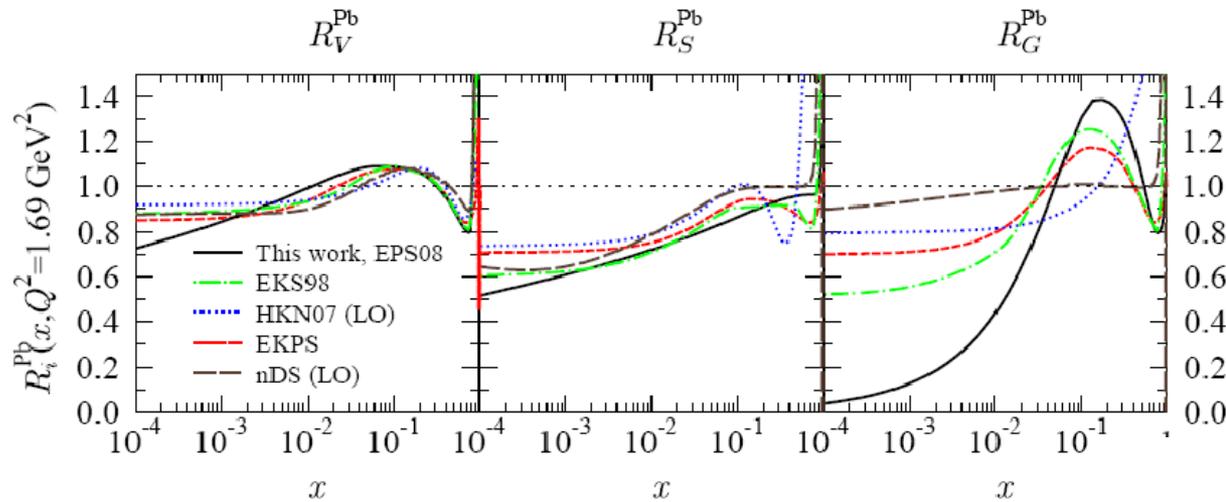


[Armesto et al., arxiv:0907.0667]

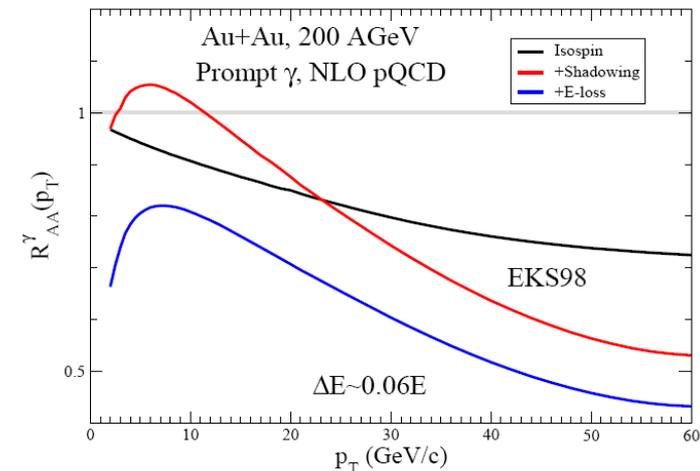
# Details: Initial State Effects

- First hurdle: initial state nuclear effects
- Shadowing, anti-shadowing, EMC effect on nuclear parton distributions
  - Large uncertainties, in particular for gluons and at small  $x$ .

[Eskola et al., (1998, 2008)]



- Cronin effect
- We can use photon/dileptons production in A+A to check our understanding.
- Electron-Ion Collider!

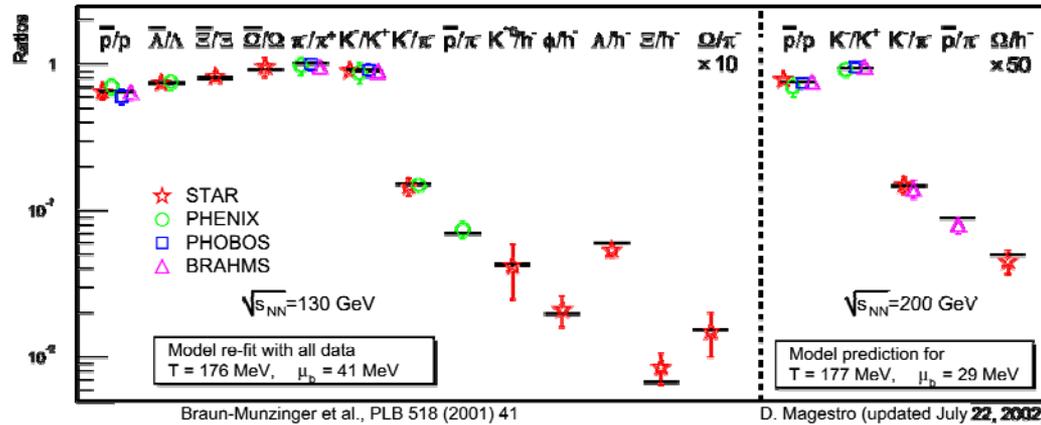


# Chemistry of Hadrons at High $P_T$

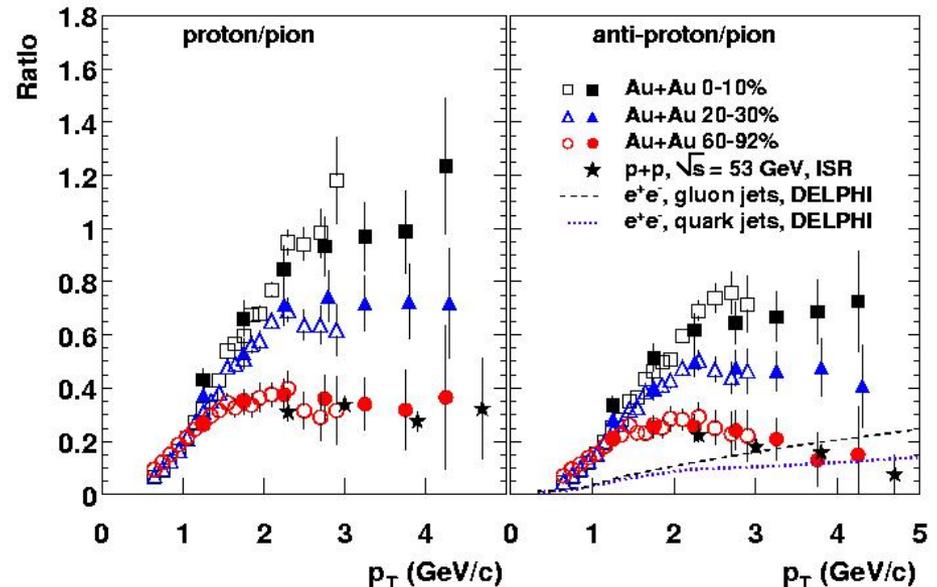


# Hadro-Chemistry at Low and Intermediate $P_T$

- Remember: hadron ratios given by statistical model.

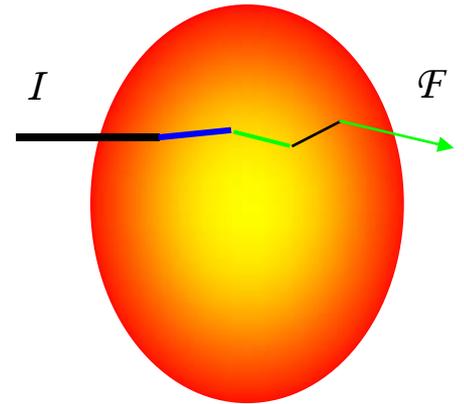


- Intermediate  $P_T$ : baryon/meson ratios and scaling laws led to quark recombination models.

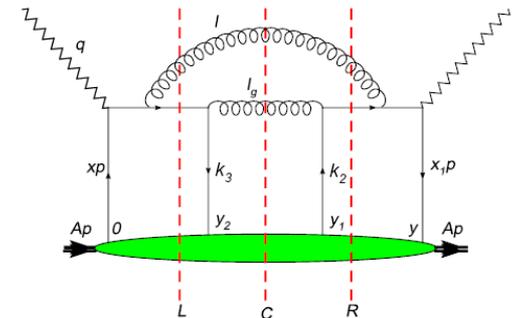
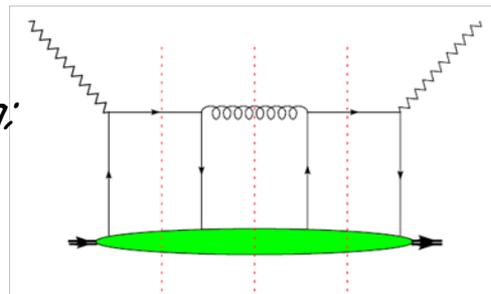


# Hard Probes Revisited

- How else can we use hard probes? Measure the “flavor”!
- Obviously: flavor of a parton can change when interacting with the medium.
- Here: very general definition of flavor:
  - Gluons  $g$
  - Light quarks  $q = u, d$
  - Strange quarks  $s$
  - Heavy quarks  $Q = c, b$
  - Real photons, virtual photons (dileptons)  $\gamma$
- Measure flavor conversions  $\rightarrow$  jet chemistry



*Example: Schäfer, Wang, Zhang;  
HT formalism*

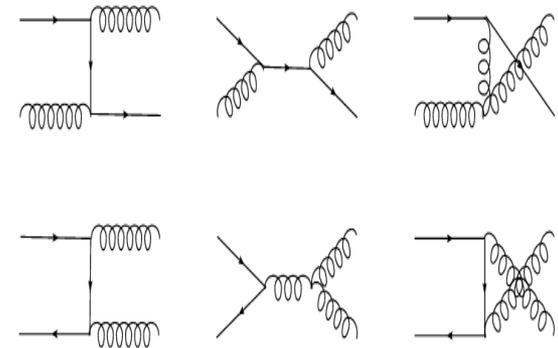


# Jet Chemistry

- Flavor of a jet here = identity of the leading parton.
  - Flavor of a jet is NOT a conserved quantity in a medium.
  - Only well-defined locally!

- The picture here:

- Parton propagation through the medium with elastic or inelastic collisions
- After any collision: final state parton with highest momentum is the new leading parton (“the jet”)



- Hadronization: parton chemistry → hadron chemistry

- Hadronization washes out signals; need robust flavor signals on the parton side.

- Other mechanisms might also change hadron chemistry in jets:

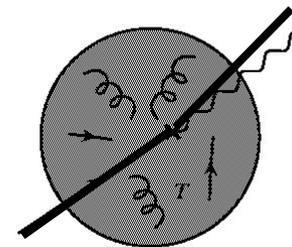
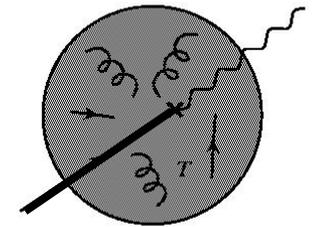
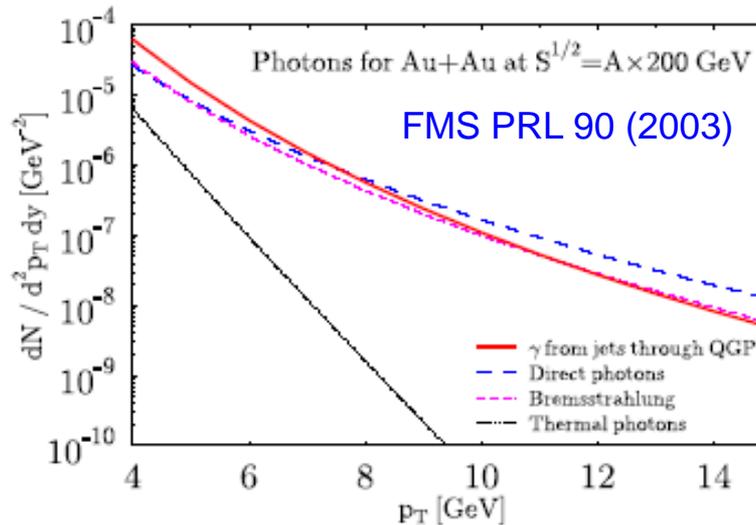
- E.g. changed multiplicities

[Sapeta, Wiedemann]

# Applications: Photons

- Photon and dilepton conversions:

[RJF, Müller, Srivastava]  
 [Srivastava, Gale, RJF]  
 [Zakharov], .....  
 [Zhang, Vitev]



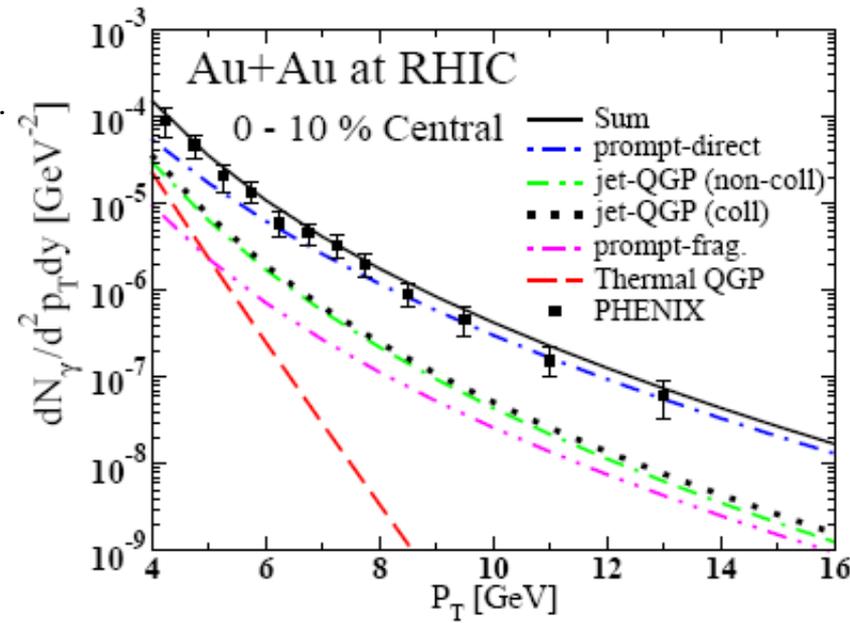
- First estimate:

- Competitive photon sources for  $P_T \sim 4-6$  GeV at RHIC energies, even more important at LHC.

- Experimental situation: not resolved

- From a recent calculation:

[Turbide, Gale, Frodermann, Heinz]

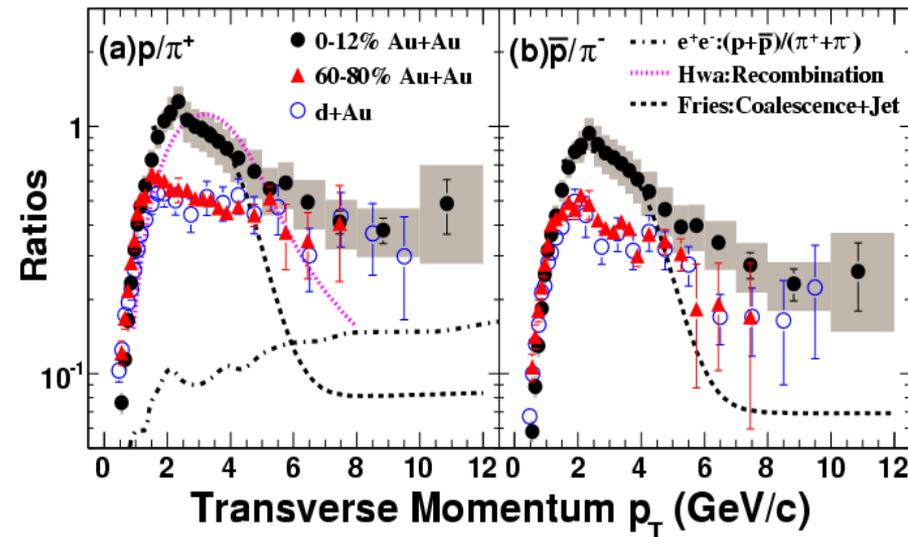
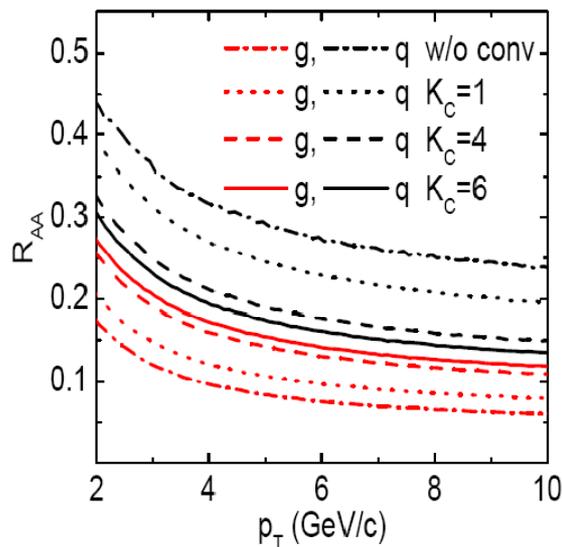


# Applications: Gluons and Protons

- Gluon  $\leftrightarrow$  (light) quark conversions [Ko, Liu, Zhang; Schäfer, Zhang, Wang; ...]
- Available in some jet quenching schemes (HT, AMY, ...)

- Relative quenching of gluons and factor 9/4

- Not explicitly observed in data
- Shouldn't be there in a system path!



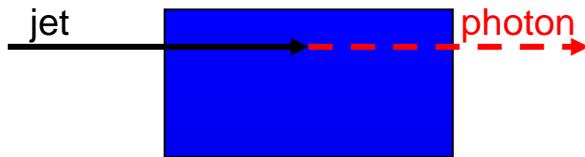
- Ko et al: elastic  $g \leftrightarrow q$  conversions
  - Lose 30% of quark jets at RHIC
  - enhance  $p/\pi$  ratio; need elastic cross sections  $\times 4$  to get p+p values
  - Dependence on fragmentation functions!

# Why Could It Be Exciting?

- For chemistry, momentum transfer is not important (unless there are threshold effects)
- Rather: flavor conversions are sensitive to the mean free paths  $\lambda$  of partons in the medium.
- Complementary information, could help settle interesting questions
  - Many interactions with small momentum transfer?
  - Few scatterings with large momentum transfer?
- But: measurements will be challenging
  - Need particle identification beyond 6-8 GeV/c at RHIC, outside of the recombination region.

# Two Examples for Rare Probes

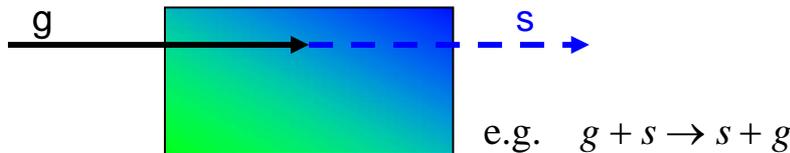
- Example 1: excess production of particles which are rare in the medium and rare in the probe sample



$$\frac{dN^{\text{rare}}}{dt} = \frac{1}{\lambda} N^{\text{jet}} \quad \Rightarrow \quad \frac{N^{\text{rare, excess}}}{N^{\text{jet}}} = \frac{L}{\lambda}$$

- Example: photons
- Need enough yield to outshine other sources of  $N^{\text{rare}}$ .

- Example 2: chemical equilibration of a rare probe particle



$$w_{jet} = \left( \frac{s}{u+d} \right)_{jet} \approx 5\% \quad @ 10 \text{ GeV for RHIC}$$

$$w_{ce} = \left( \frac{s}{u+d} \right)_{medium} \approx 50\%$$

- Example: strangeness at RHIC
- Coupling of jets (not equilibrated) to the equilibrated medium should drive jets towards chemical equilibrium.

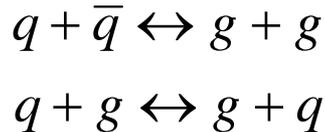
# Conversion Rates

- Coupled rate equations for numbers of jet particles (flavors a, b, c, ...) in a fireball simulation.

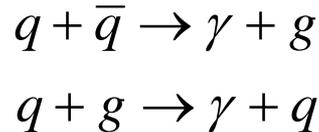
$$\frac{dN^a}{dt} = -\sum_b \Gamma^{a \rightarrow b}(p_T, T) N^a + \sum_c \Gamma^{c \rightarrow a}(p_T, T) N^c$$

$$\Gamma = \frac{1}{2E_1} \int \frac{g_2 d^3 p_2}{(2\pi)^3 2E_2} \frac{d^3 p_3}{(2\pi)^3 2E_3} \frac{d^3 p_4}{(2\pi)^3 2E_4} f(p_2) [1 \pm f(p_4)] \times |M_{12 \rightarrow 34}|^2 (2\pi)^4 \delta^{(4)}(p_1 + p_2 - p_3 - p_4) = \left\langle |M_{12 \rightarrow 34}|^2 \right\rangle$$

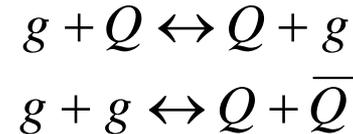
- Here: reaction rates from elastic  $2 \rightarrow 2$  collisions



Quark / gluon conversions



Photons and dileptons;  
inverse reaction negligible



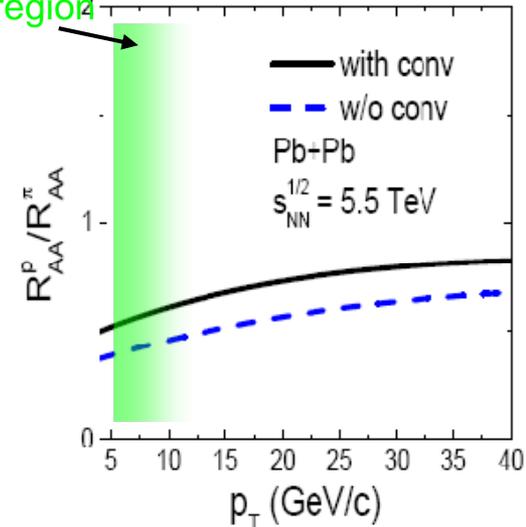
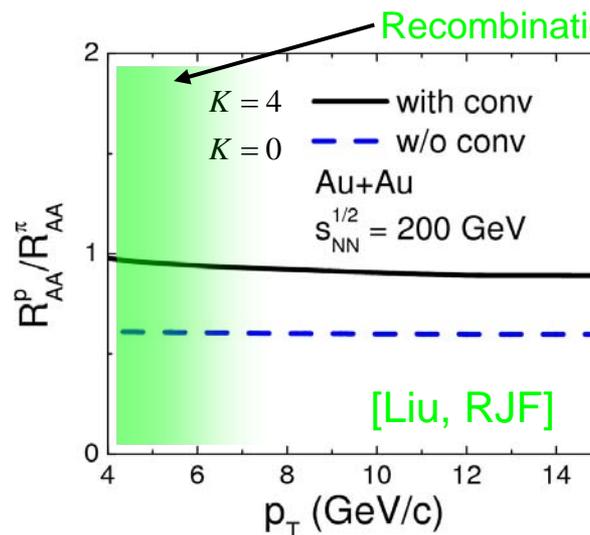
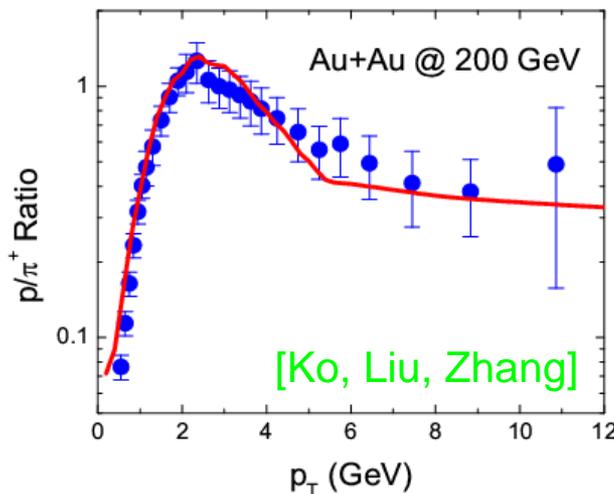
Heavy quarks production?

- Need to compare to  $2 \rightarrow 3$  processes.
- Non-perturbative mechanisms?

# Results: Protons

- Use the model by Ko, Liu and Zhang:
  - Rate equations plus energy loss.
  - Elastic channels; cross sections with  $K$ -factor
  - Longitudinally and transversely expanding fireball
    - RHIC:  $T_i = 350$  MeV @ 0.6 fm/c
    - LHC:  $T_i = 700$  MeV @ 0.2 fm/c
- Use double ratios to cut uncertainties from fragmentation functions.

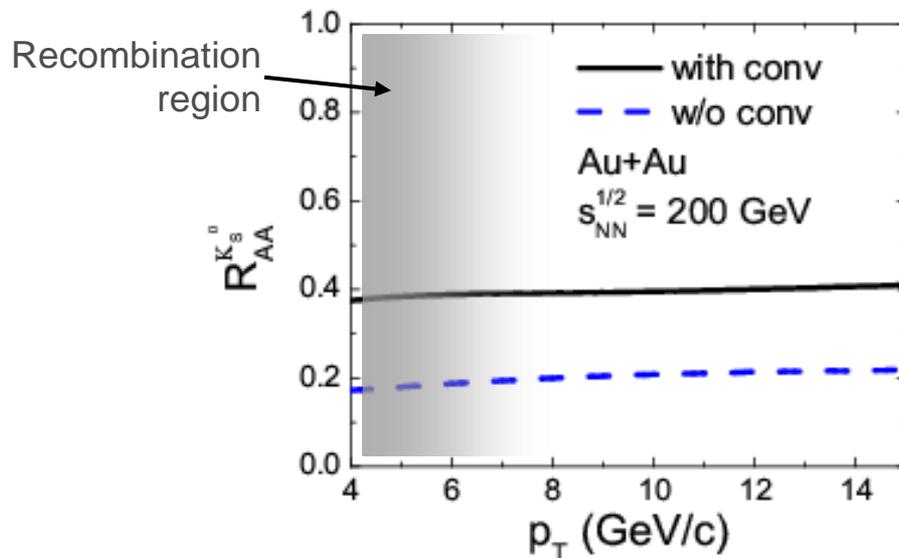
$$\gamma_{p/\pi^+} = \frac{(p/\pi^+)_{AA}}{(p/\pi^+)_{pp}} = \frac{R_{AA}^p}{R_{AA}^{\pi^+}}$$



# Results: Strangeness

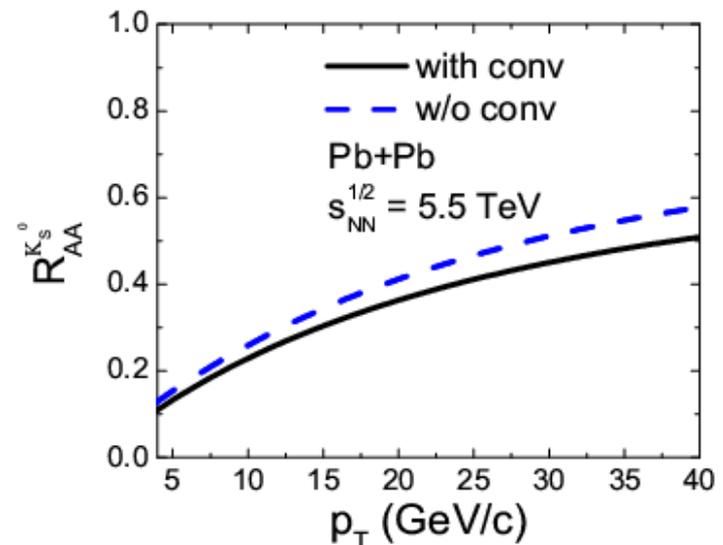
- Kaons: see expected enhancement at RHIC

- Measure above the recombination region!



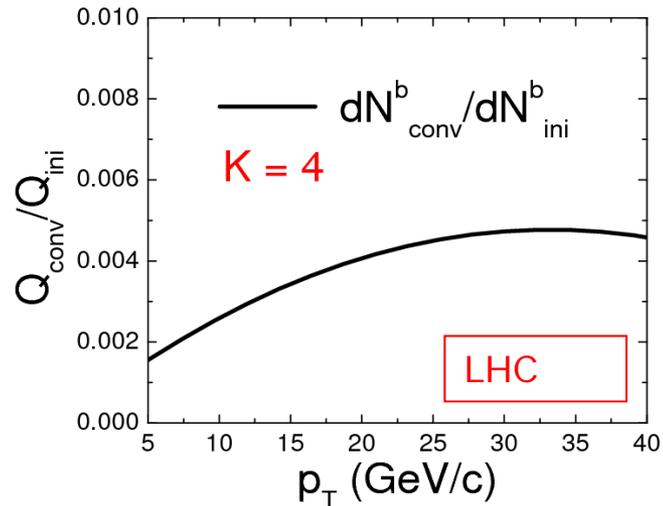
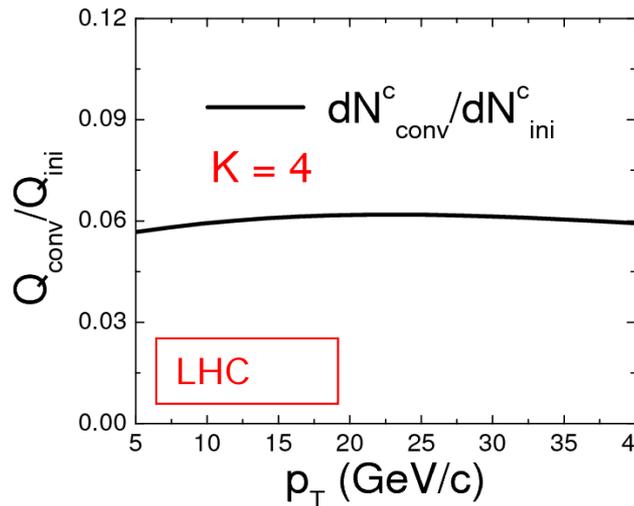
- No enhancement at LHC

- Too much initial strangeness!
- Maybe it works with charm at LHC?



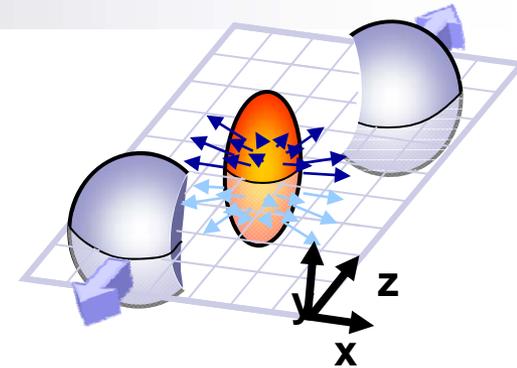
# Numerical Results: Heavy Quarks

- Have to take into account threshold effect
- At RHIC: additional heavy quark production marginal
- LHC: not at all like strangeness at RHIC; additional yield small
  - Reason: charm not chemically equilibrated at LHC
  - Results in small chemical gradient between jet and medium charm
  - Also: threshold effect

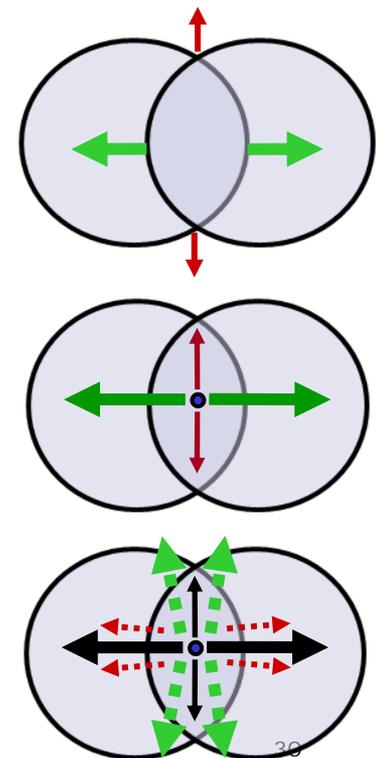


# Elliptic Flow $v_2$

- Azimuthal anisotropy for finite impact parameter.
- Three different mechanisms:



	Initial anisotropy	Final anisotropy	Elliptic flow $v_2$
Bulk	pressure gradient	collective flow	$v_2 > 0$
saturated hard probe	path length	quenching	$v_2 > 0$
rare hard $P_T$ probe	path length	additional production	$v_2 < 0$



[Turbide, Gale & RJF, PRL 96 (2006)]

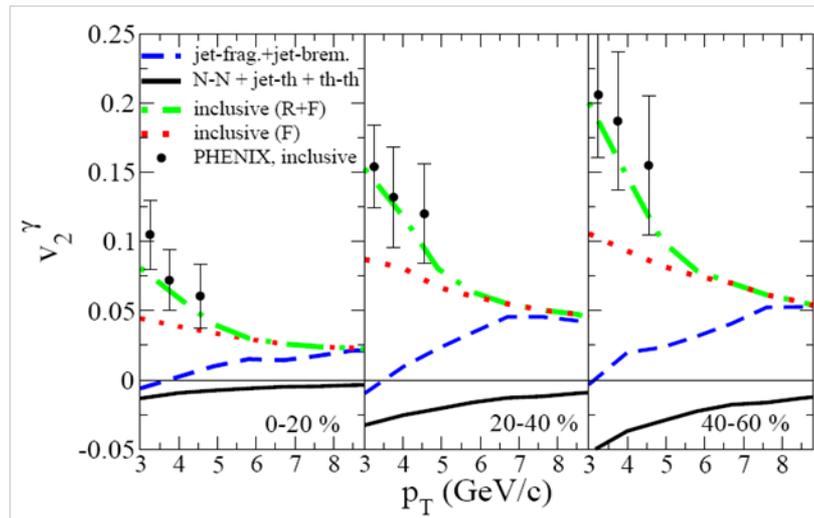
# Photon Elliptic Flow

- Have to add other photon sources with vanishing or positive  $v_2$ .

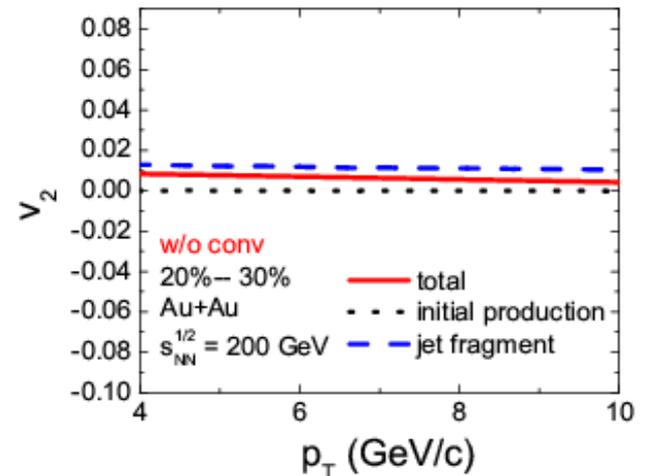
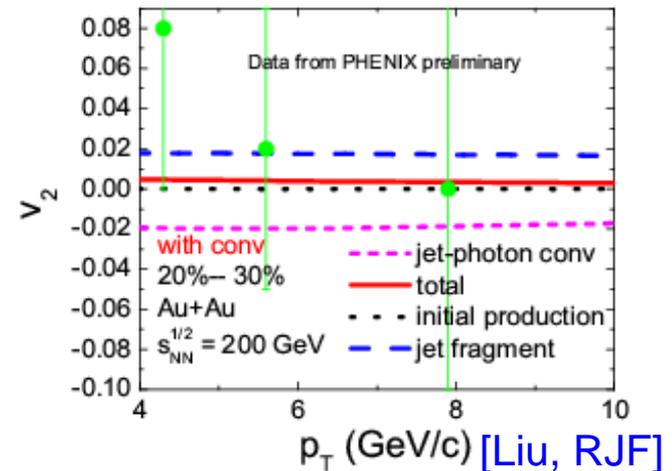
[Turbide, Gale, RJF;  
Chatterjee, Frodermann, Heinz, Srivastava; ...]

- Status:

- Large negative  $v_2$  excluded by experiment.
- Large uncertainties from fireball model?

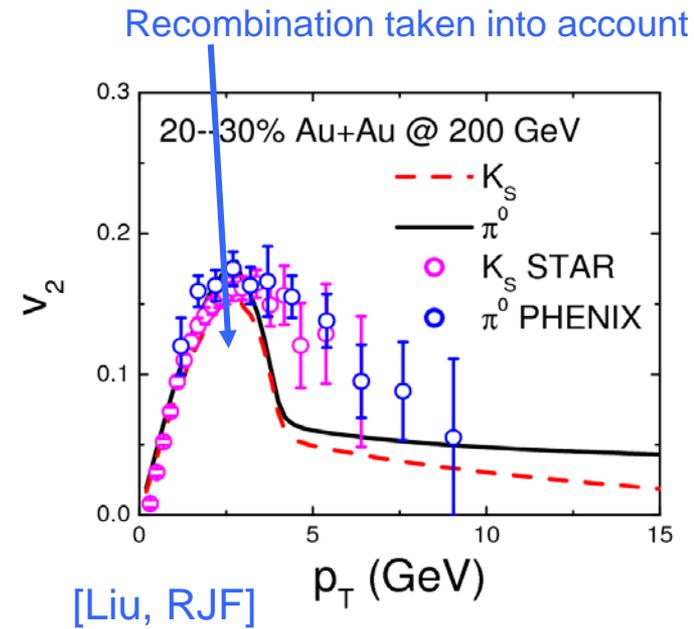
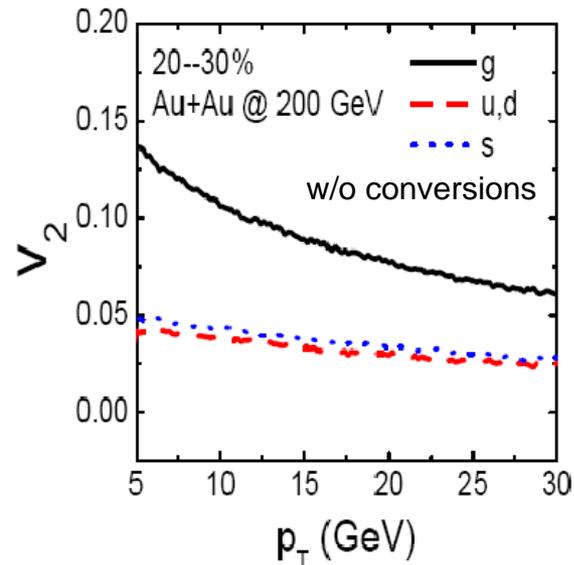
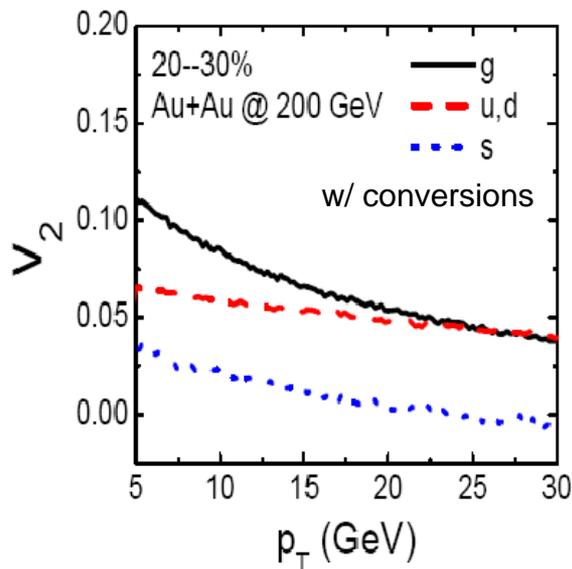


[Turbide, Gale, RJF]



# Strangeness Elliptic Flow

- Strangeness as non-equilibrated probe at RHIC: additional strange quarks have negative  $v_2$ .
- Expect suppression of kaon  $v_2$  outside of the recombination region.

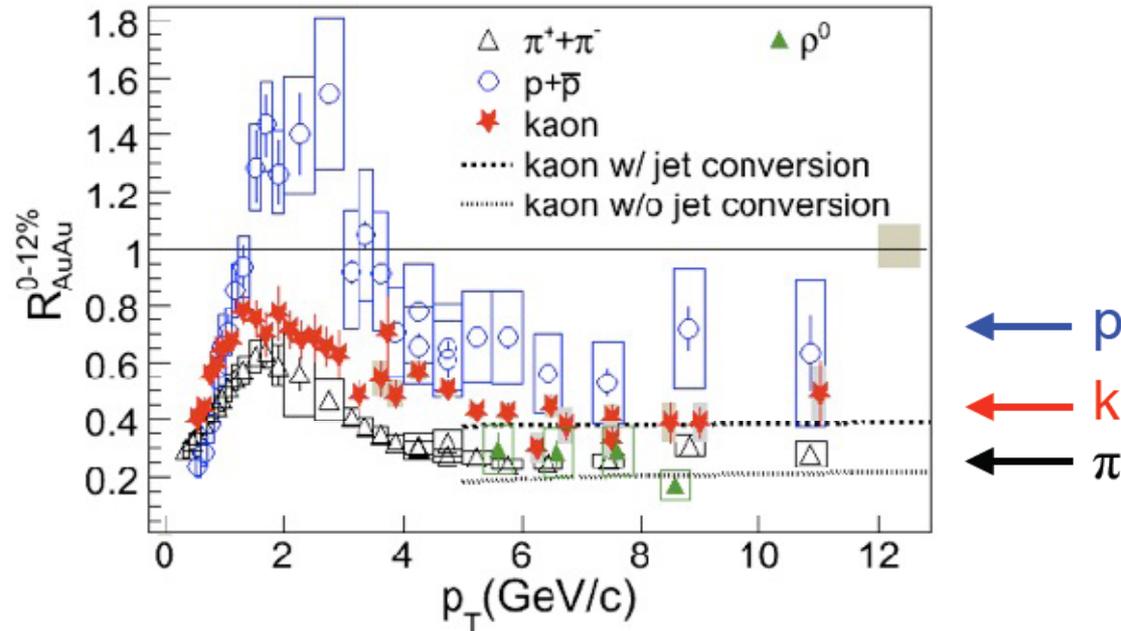


# New Results from STAR

[Liu, RJF, PRC (2008)]

## ■ STAR at QM 2009

- Kaon enhancement seen between 6 and 10 GeV/c.
- A first signal for conversions?
- Caution: p enhancement too big.



## ■ Blast from the past: remember strangeness enhancement from the 1980s?

# New Simulation of Hard Probes



# Plans for the Near Future

- We develop a standardized test bed to simulate  $N$  jets/hard particles in a fireball.
  - Part of a NSF project with R. Rodriguez, R.J. Fries, E. Ramirez
- Input:
  - initial phase space distributions
  - background (aka fireball)
  - specifics of dynamics (energy loss, fragmentation)
- What it should do:
  - Evolution of particle distributions;
  - (modified) fragmentation and hadronization
  - analysis of results in terms of experimentally relevant observables

# Propagating Particles in a Medium (PPM)

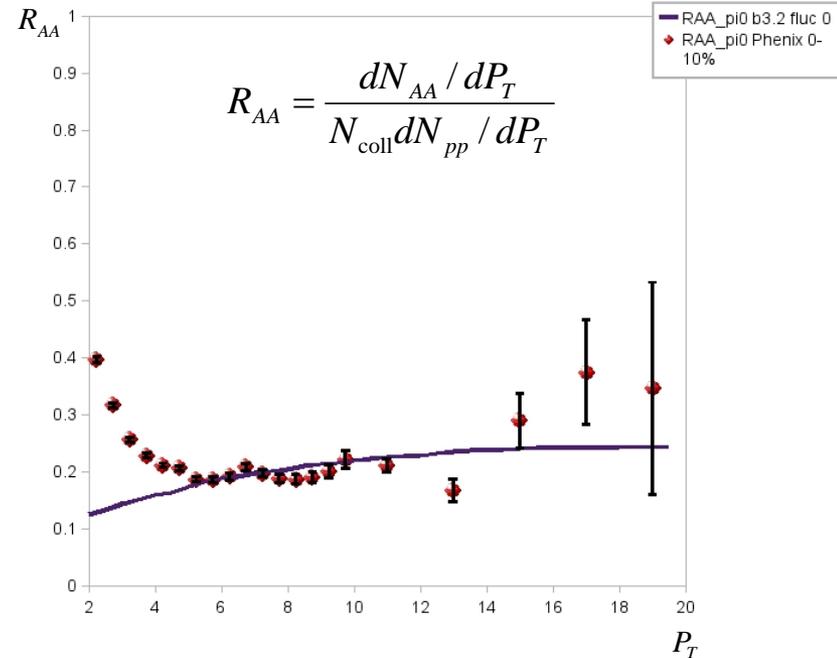
- Some results from the testing process

- Using vacuum fragmentation and GLV average energy loss

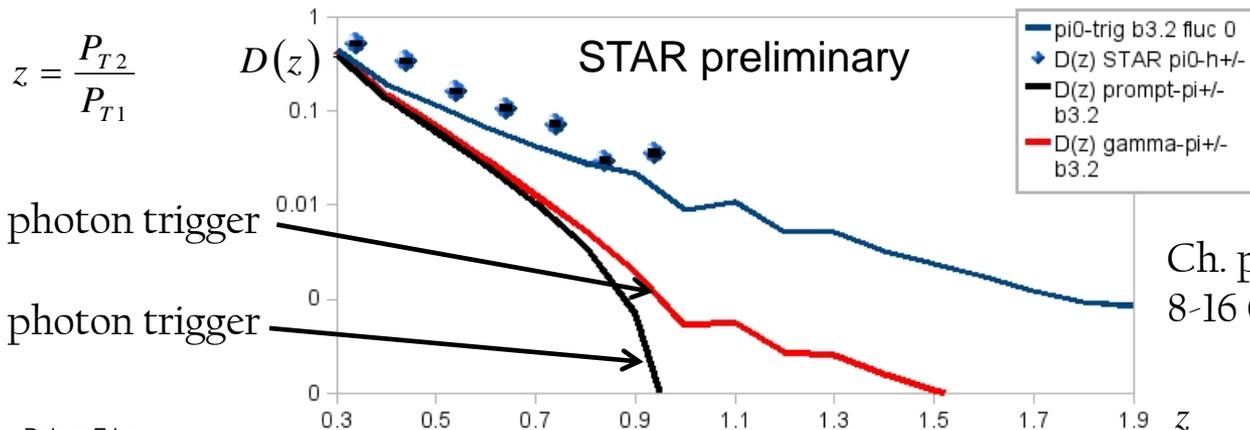
$$\Delta E = \frac{C_R \alpha_s}{4} \frac{\mu^2}{\lambda} L^2 \log E$$

- Neutral pion  $R_{AA}$  vs PHENIX data

- Estimate  $\hat{q} = \frac{\mu^2}{\lambda} \approx 2.5 \text{ GeV}^2/\text{fm}$



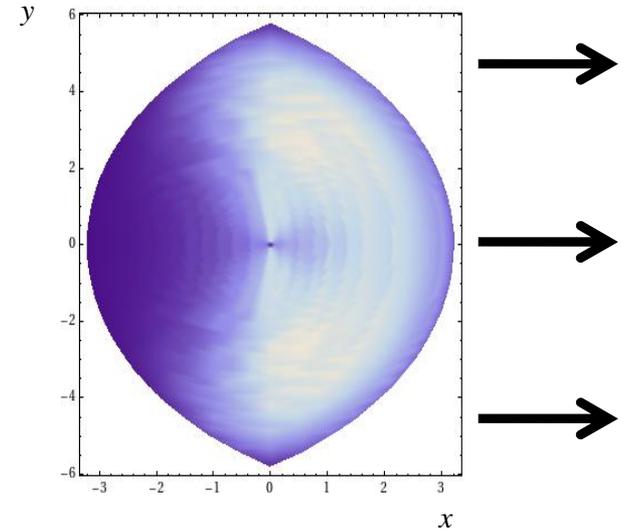
- Triggered away side fragmentation function for charged hadrons.



Ch. pion with  $\pi^0$  trigger  
8-16 GeV trigger  $P_T$

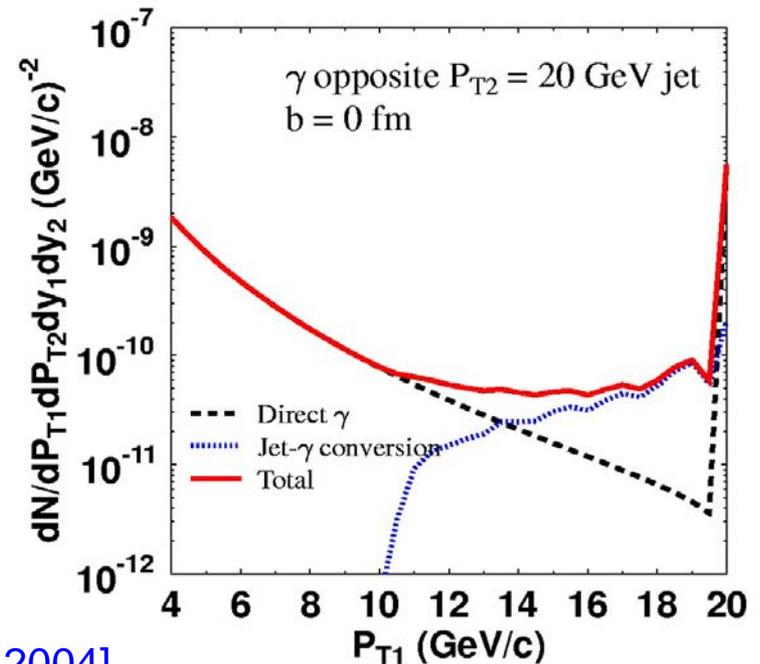
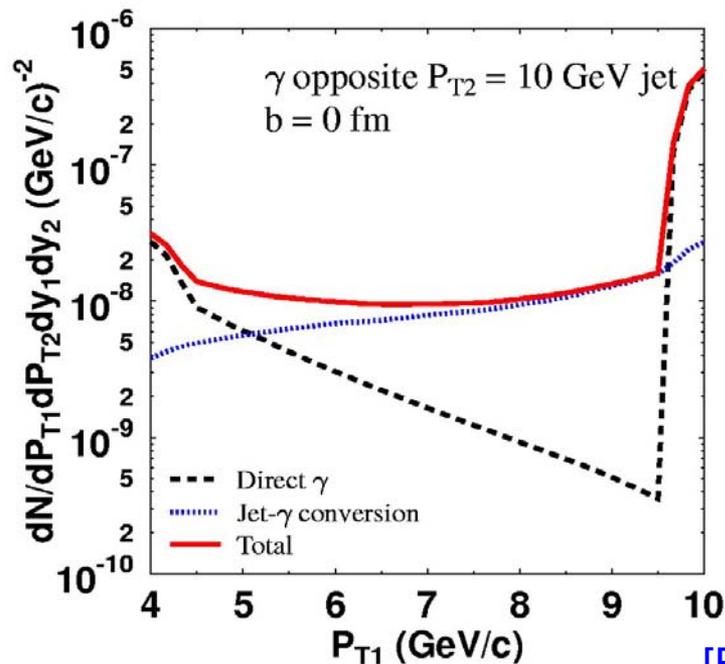
# Propagating Particles in a Medium (PPM)

- Map functions
  - Example: emissivity for 8-10 GeV up-quarks going to the right,  $b=7.4$  fm collision of Au ions.
- Goals:
  - Build a flexible test bed for hard and electromagnetic probes.
  - Comprehensive, quantitative studies of observables.
  - photon/Z – jet/hadron correlations at NLO accuracy.
- Understanding photon/Z – jet/hadron correlations  $\leftrightarrow$  understanding electromagnetic sources and conversion processes.
- Eventually code can be made public and/or be made part of a larger effort (Techqm, JET)



# Jet-Photon Correlations

- Additional photons are background for photon tagged jets.
- Turn this into an advantage: measure photon spectrum opposite to a jet of known energy to disentangle different sources.
- Photons opposite 10 and 20 GeV jets:



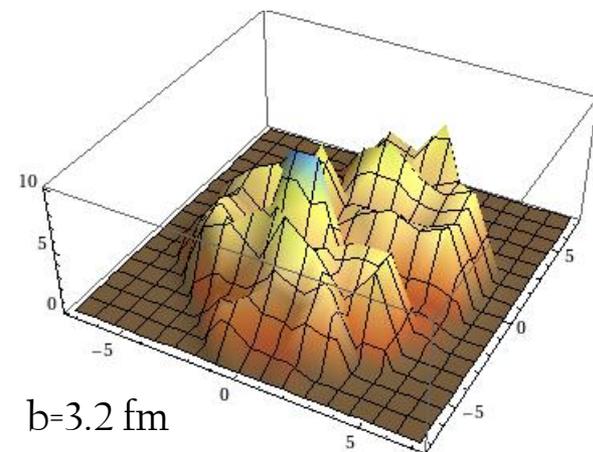
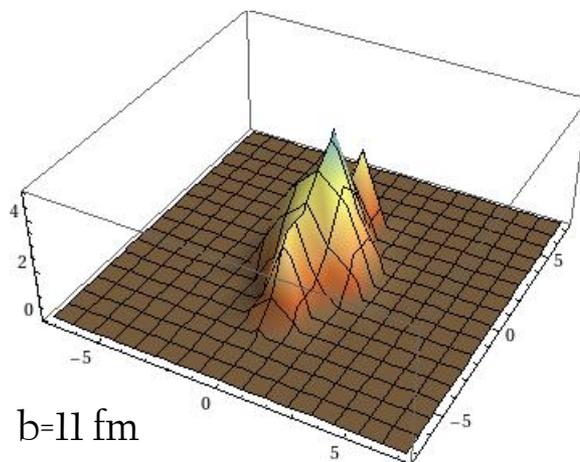
[RJF, DNP 2004]

# First Results: Resolving Spatial Structures



# Probing the Spatial Structure

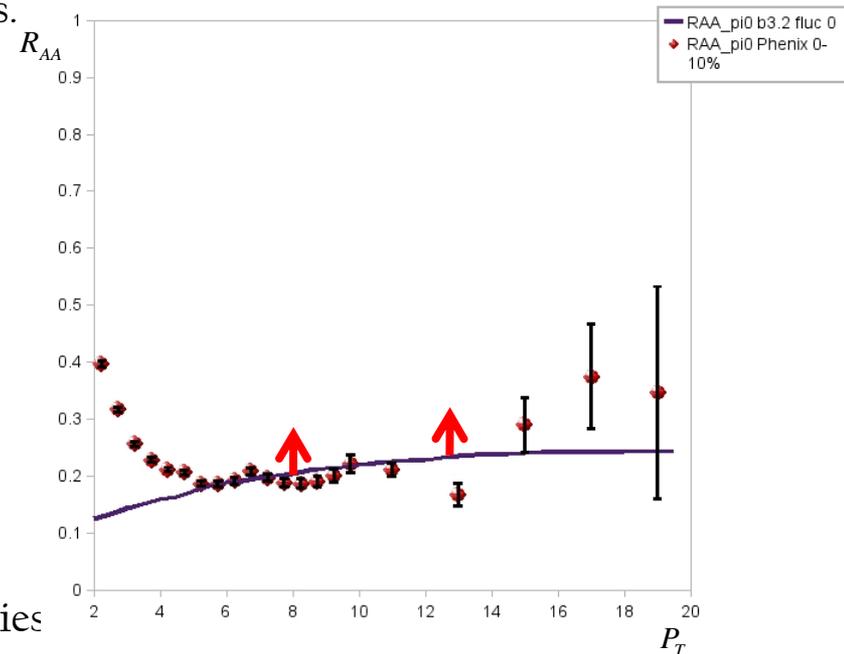
- What can hard probes tell us about the spatial structure of the fireball?
  - Or: can we do true tomography?
  - Seemingly hopeless: we sum over many events and only see an average fireball.
- What is the effect of an inhomogeneous fireball on hard probes?
  - Realistic initial conditions with fluctuations have been studied for hydrodynamics.
  - Applicability of hydro and elliptic flow seem to set some boundaries for times  $> 1$  fm/c.
  - Hard probes from the surface layer and in peripheral collisions might be affected by fluctuations in the background.



# Probing the Spatial Structure

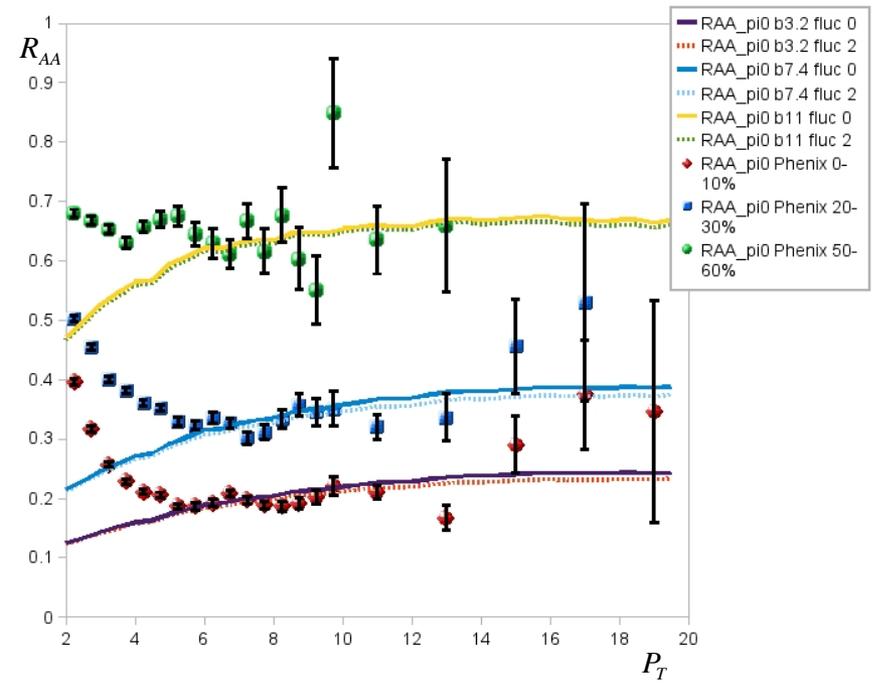
- Use events with fluctuating transverse profiles of the energy density.
  - Have tried simple transverse profiles with Gaussian fluctuations.
  - Here: initial state Glauber estimates of the number of participants (i.e. no energy flow build-up taken into account that would wash out inhomogeneities);
  - Assume  $\hat{q} \propto \varepsilon^{3/4} \propto n_{\text{part}}^{3/4}$ .
  - Will run some existing initial state simulations (e.g. GLISSANDO)
  - For every observable take average over events.

- Check single pion spectra:
  - As expected: fluctuations lead to slightly less suppression.
  - This can be absorbed in the definition of energy loss parameter,
  - Fit data well with  $\hat{q} = 3.1 \text{ GeV/fm}^2$
  - Nothing won, effect no longer observable.
  - But the extracted strength of energy loss changes by 25%. Add to the list of uncertainties



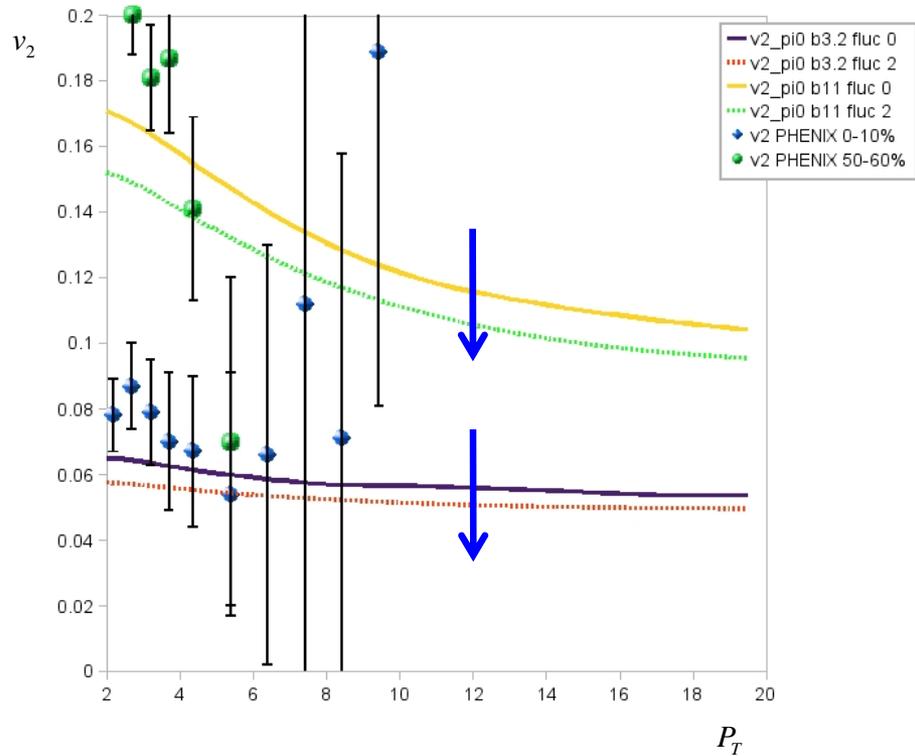
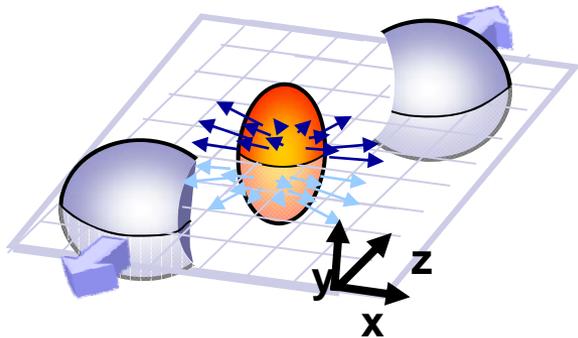
# Probing the Spatial Structure

- Centrality dependence and  $P_T$  dependence:
- With inhomogeneities dependence stays the same after rescaling of  $\hat{q}$ .
  - Results fit PHENIX pion data.
- No signature.



# Probing the Spatial Structure

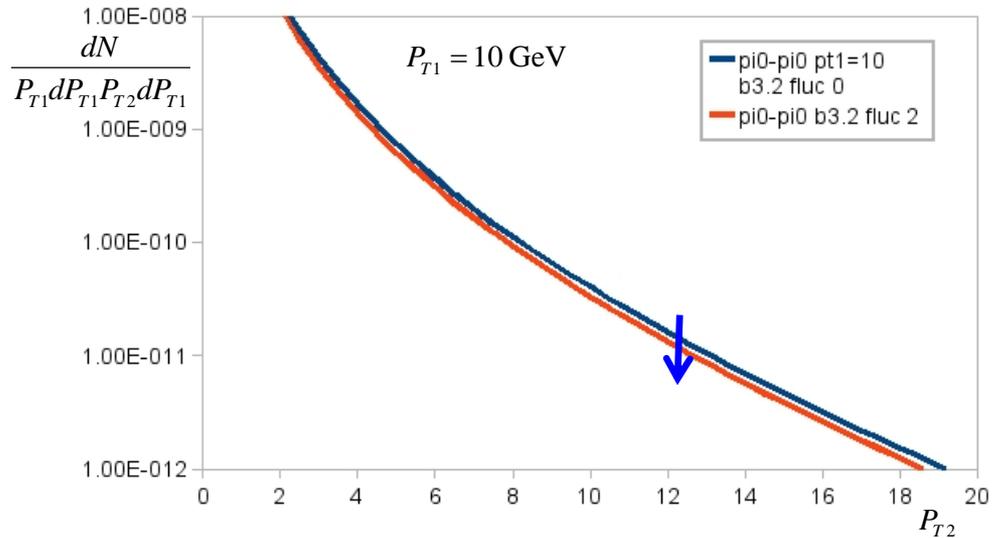
- Elliptic Flow  $v_2$ :



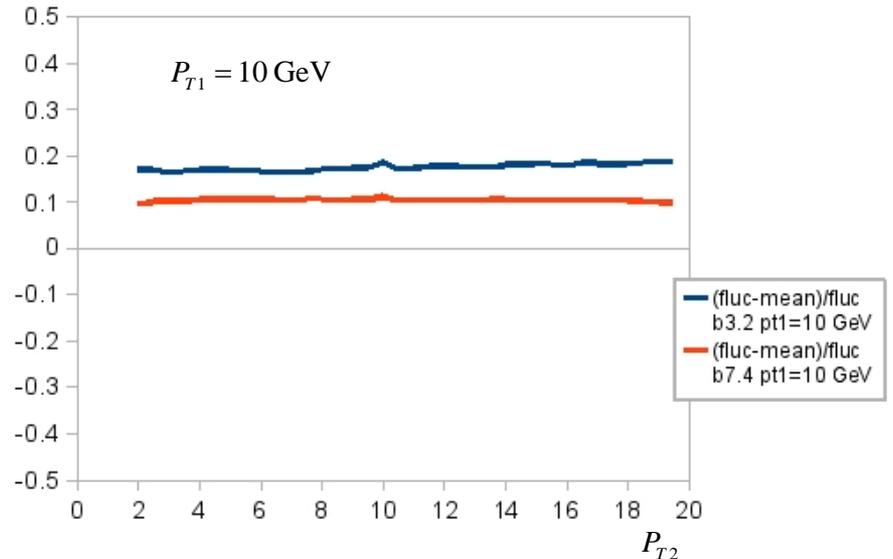
- 10-20% reduction in  $v_2$  even after redefinition of  $\hat{q}$ .

# Probing the Spatial Structure

- Dipion spectrum:
  - Visible deviation with inhomogeneities



- Relative deviation on linear scale:
- 10-20% reduction in correlation strength after redefinition of  $\hat{q}$ .



# Summary & Outlook

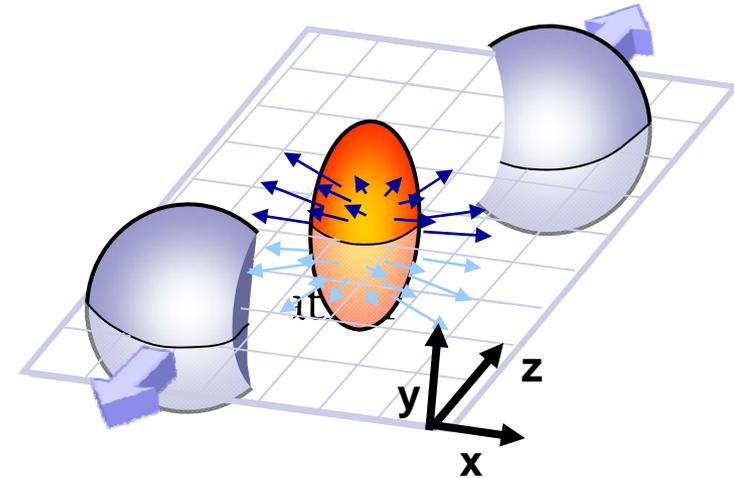
- Hadro-chemistry for hard probes
  - Flavor changing processes are present in jet-medium interactions.
  - Jet chemistry contains information complementary to jet quenching measurements.
  - Predict strangeness enhancement at high  $P_T$ .
- Work progressing on a new framework for studies of hard and electromagnetic probes.
- Study of partons in inhomogeneous backgrounds:
  - Found 25% change in the extracted quenching strength to explain the data.
  - Even after adjusting the quenching strength, up to 20% secondary effect visible in elliptic flow and di-hadron correlations.

# Backup

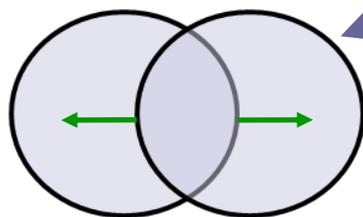


# Pressure

- Finite impact parameter  $b > 0$ :
  - Spatial anisotropy in the initial state
  - Momentum anisotropy in the final state
- Space  $\leftrightarrow$  momentum space



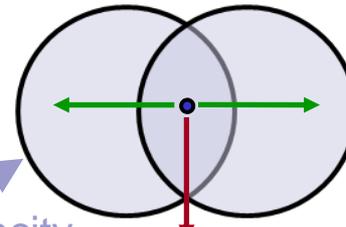
## Bulk/soft particles



$$Force = -\nabla P$$

Test EOS  
of the system

## Hard particles

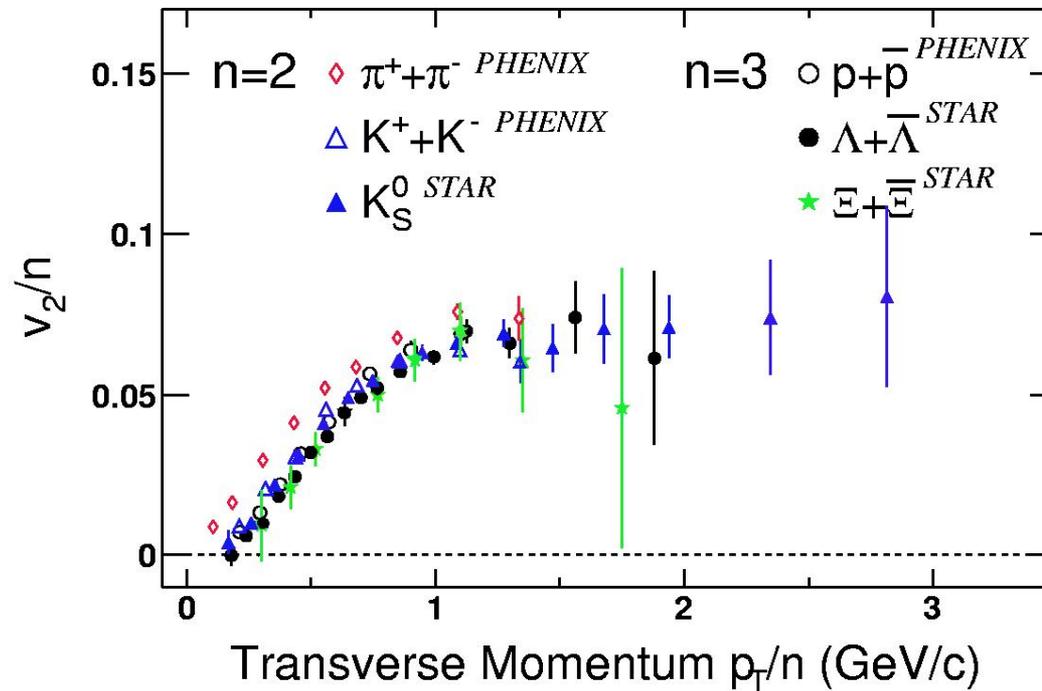


$$\Delta E \propto L$$

Test density/opacity  
of the medium

# Two Great Discoveries

- $v_2$  scaling for mesons and baryons



# Instantaneous Coalescence

- Simple realization of a recombination model

- Recombine valence quarks of hadrons

$$q\bar{q} \rightarrow M$$

$$qqq \rightarrow B$$

- Dressed quarks, no gluons

- Instantaneous projection of quark states on hadron states:

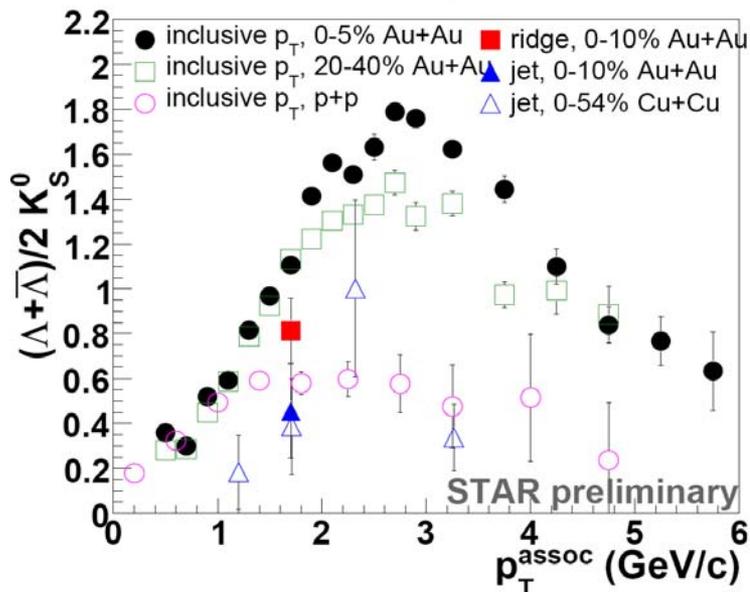
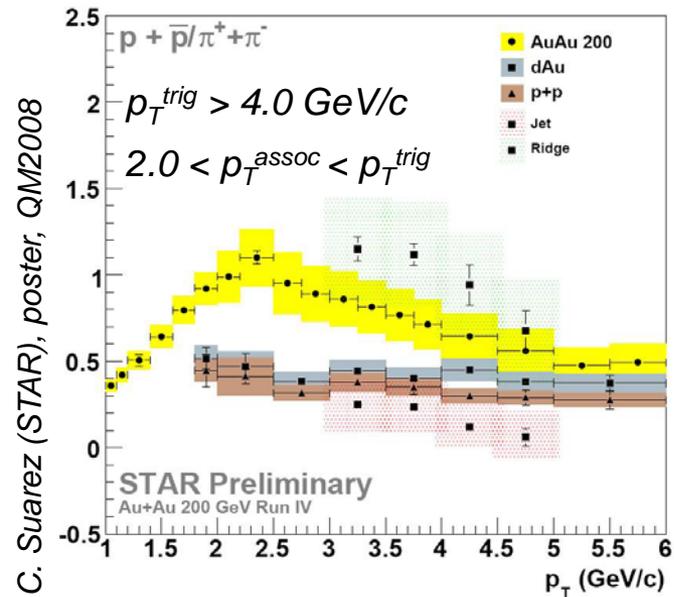
[Fries, Muller, Nonaka, Bass]  
 [Greco, Ko, Levai]  
 [Hwa, Yang]

$$\frac{d^3 N_M}{d^3 P} = C_M \int_{\Sigma} \overbrace{w_{\alpha} \otimes w_{\beta} \otimes \Phi_M}^{\text{Meson Wigner function}}$$

Production hypersurface
Product of quark distributions

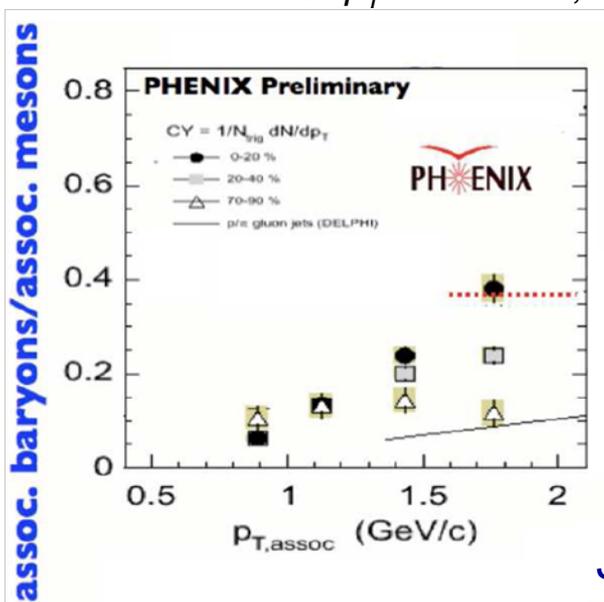
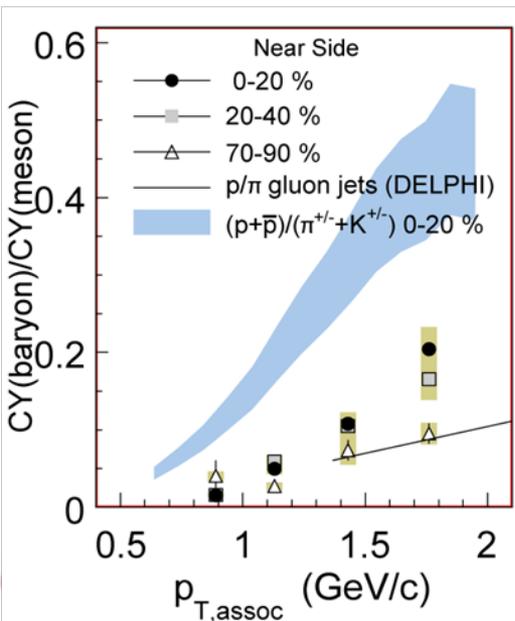
- Recombination itself does not make absolute predictions. If successful, it predicts the *difference* between hadron species → chemistry

# Particle composition in "jet" and ridge



Au+Au:  $2 < p_T^{trig} < 3 \text{ GeV}/c$ , Cu+Cu:  $3 < p_T^{trig} < 6 \text{ GeV}/c$

inclusive Au+Au: M. Lamont (STAR) SQM06  
 Cu+Cu: C. Nattrass (STAR), QM2008  
 Au+Au: J.B. (STAR), WWND07

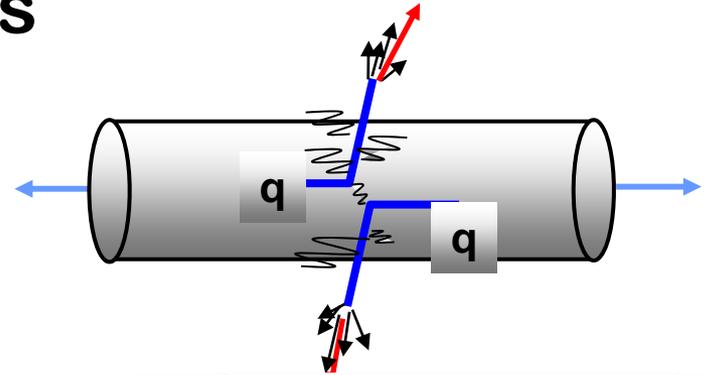


Baryon/meson ratios:

- "jet": smaller than inclusive and similar to p+p
- ridge: similar to inclusive

# Hard Probes

- Hard processes  $\Rightarrow$  QCD jets
- Our hope: this is a well-calibrated tool.
  - perturbative calculations available
  - p+p baseline experiment
- Description of initial hard process based on QCD factorization.



$$d\sigma^{A+B \rightarrow C+X} = \sum_{a,b,c} f_{a/A} \otimes d\sigma^{a+b \rightarrow c+X} \otimes f_{b/B} \otimes D_{C/c}$$

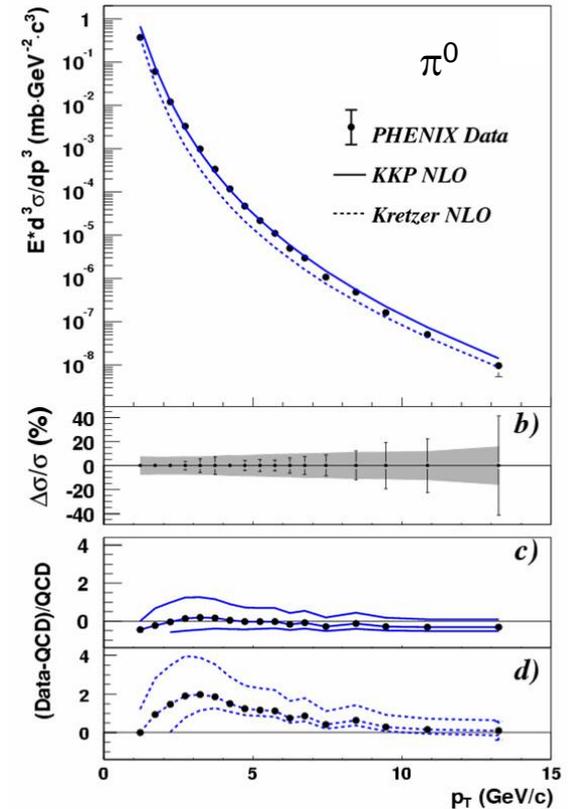
PDF

Parton  
cross  
section

PDF

FF

- p+p indeed well under control:



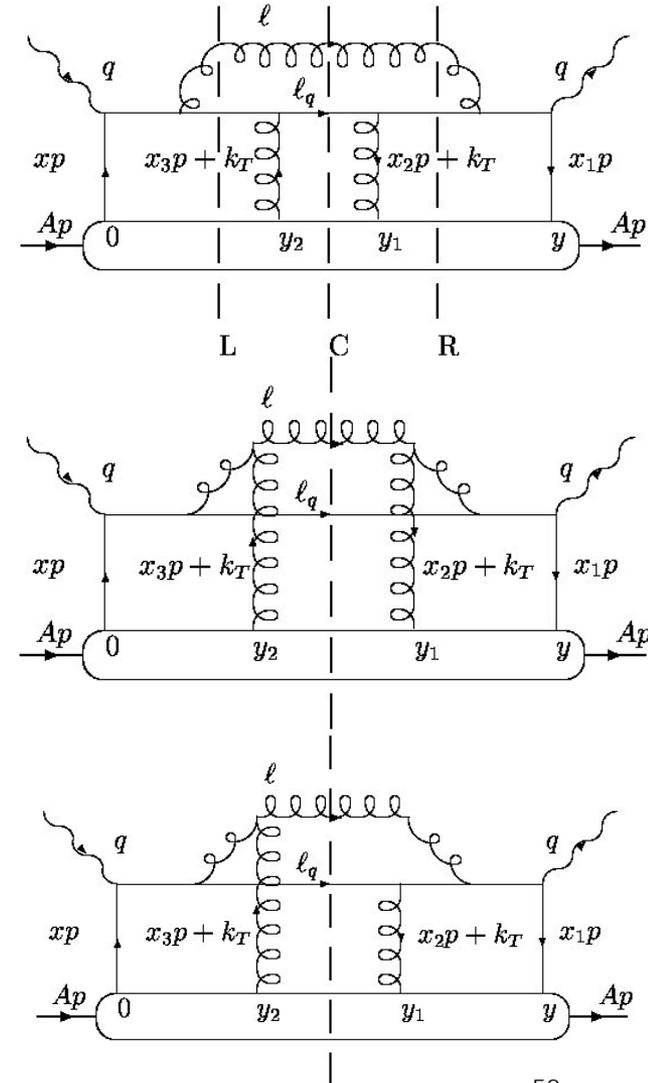
# Higher Twist Fragmentation Functions

- Rescattering of the final state partons off the nucleus.
- Twist-4 = double scattering or interference between single and triple scattering
- Hadronic tensor  $W$  in lowest order in  $\alpha_s$

$$\frac{dW^{\mu\nu}}{dz_h} = \sum_q \int dx f_{q/A}(x, \mu^2) H^{\mu\nu}(x, p, q) \tilde{D}_{q/h}(z_h, \mu^2)$$

- Modified fragmentation function

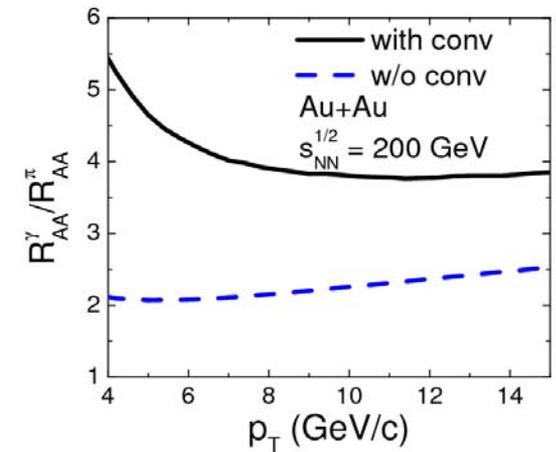
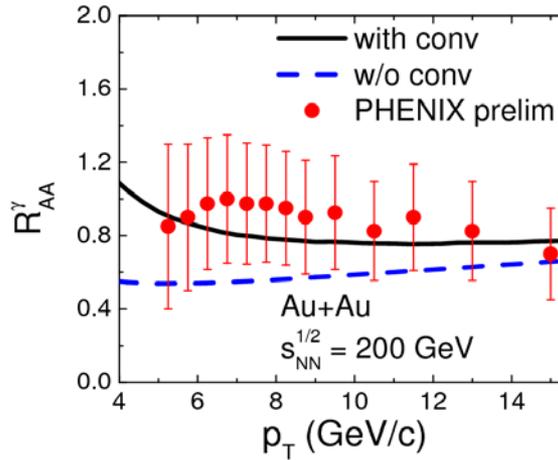
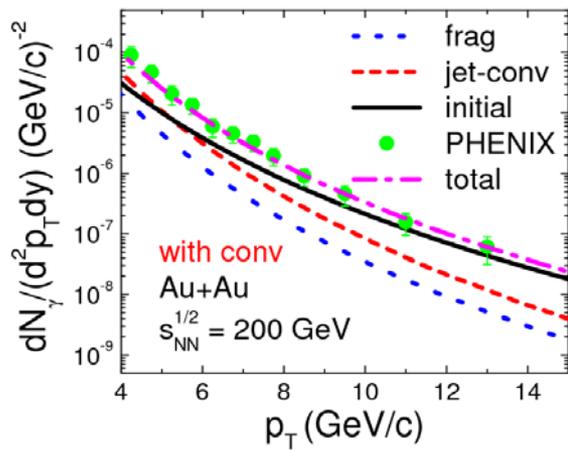
$$\tilde{D}_{q/h}(z_h, \mu^2) = D_{q/h}(z_h, \mu^2) + \int_0^{\mu^2} \frac{dl_T^2}{l_T^2} \frac{\alpha_s}{2\pi} \int_{z_h}^1 \frac{dz}{z} \times \left[ \Delta\gamma_{q \rightarrow qg}(z, x, l_T^2) D_{q/h}\left(\frac{z_h}{z}\right) + \Delta\gamma_{q \rightarrow gq}(z, x, l_T^2) D_{g/h}\left(\frac{z_h}{z}\right) \right]$$



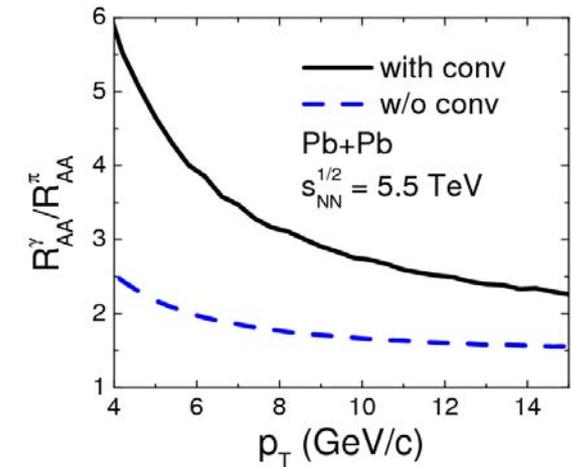
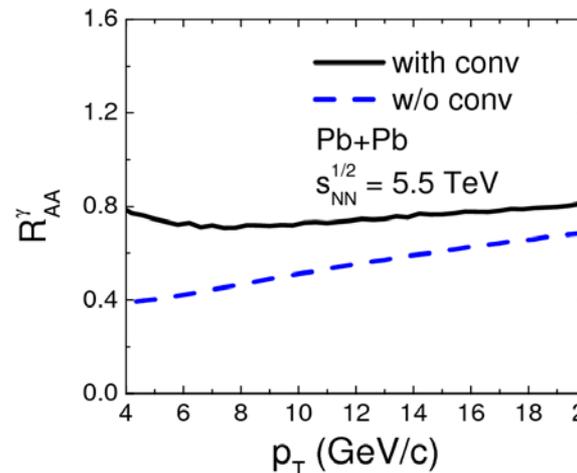
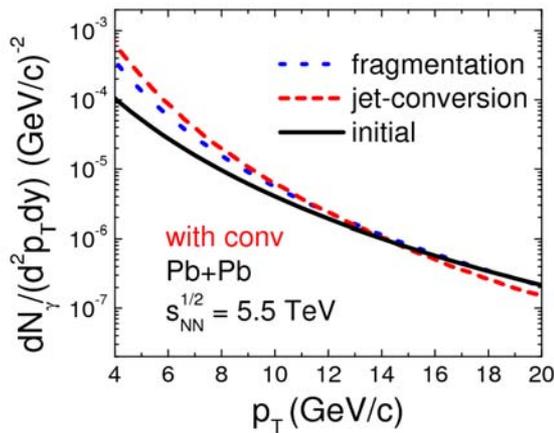
# Numerical Results: Photons

[Liu, RJF]

## Real photons (RHIC):



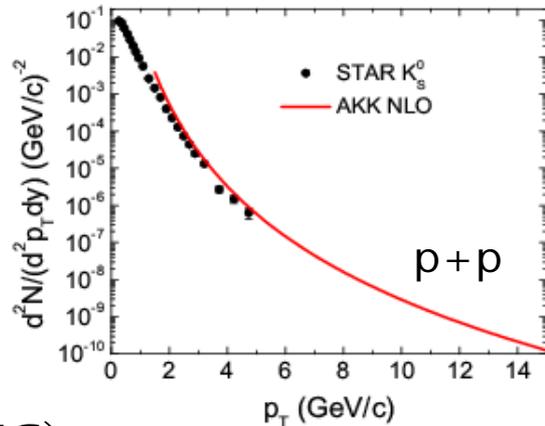
## Real photons (LHC):



# Numerical Results: Strangeness

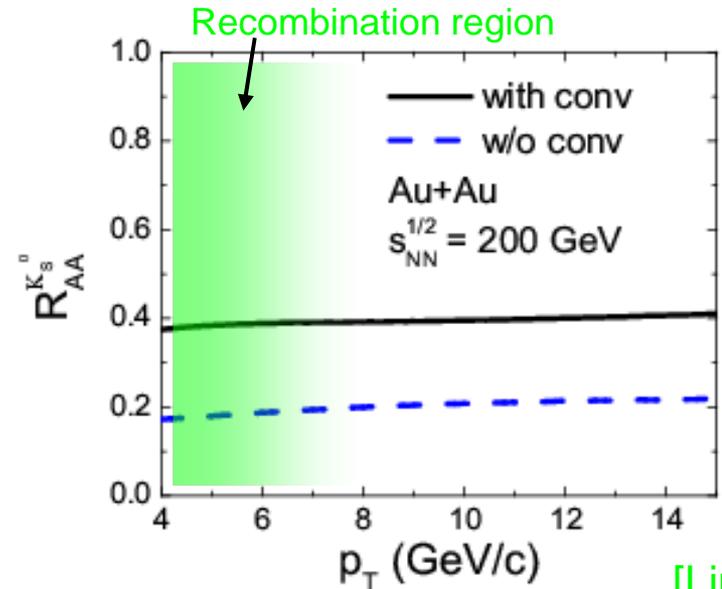
## ■ Kaons (RHIC):

- See expected enhancement
- Outside the recombination region!

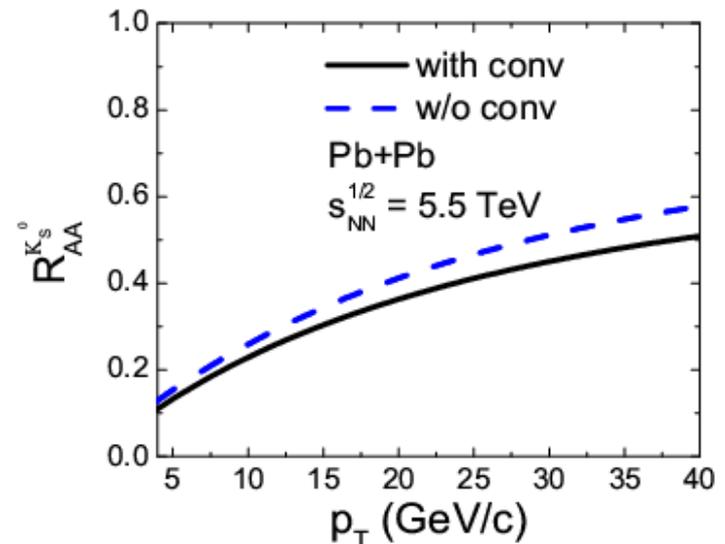


## ■ Kaons (LHC):

- No enhancement
- Too much initial strangeness!
- Maybe it works with charm?

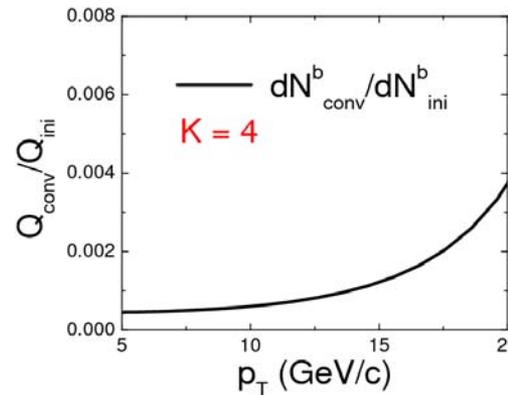
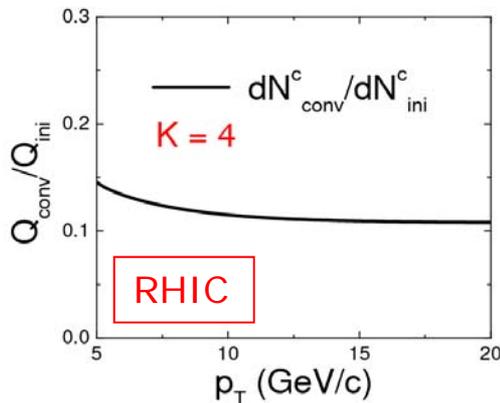


[Liu, RJF]



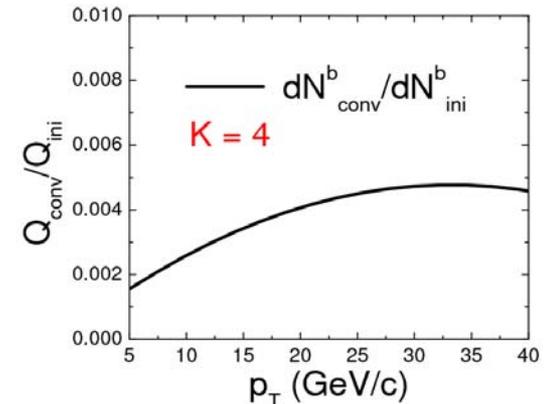
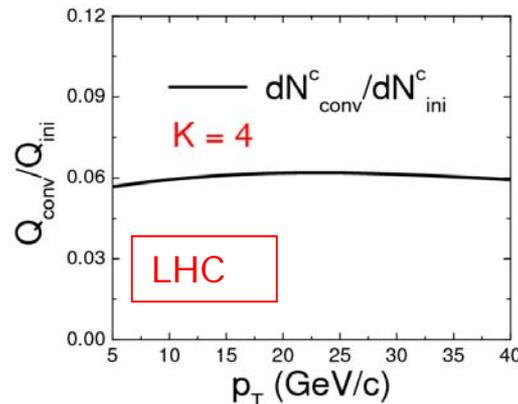
# Numerical Results: Heavy Quarks

- Have to take into account threshold effect
- At RHIC: additional heavy quark production marginal



[Liu, RJF]

- LHC: not at all the strangeness at RHIC, additional yield small
  - Reason: small gradient between jet and medium charm
  - Threshold effect



# Propagating Particles in a Medium (PPM)

- Developing flexible code to simulate N jets in a fireball.
  - Part of a NSF project; authors: R. Rodriguez, R.J. Fries, E. Ramirez
- Input:
  - initial phase space distribution
  - background (aka fireball)
  - specifics of dynamics (energy loss model, fragmentation)
- What it should do:
  - Evolution of particle distributions; (modified) fragmentation and hadronization; analysis of results in terms of experimentally relevant observables
- E.g. leading particle energy loss + fragmentation:

