

# STRANGE MESONS ( $S = \pm 1, C = B = 0$ )

$K^+ = u\bar{s}$ ,  $K^0 = d\bar{s}$ ,  $\bar{K}^0 = \bar{d}s$ ,  $K^- = \bar{u}s$ , similarly for  $K^*$ 's

**$K^\pm$**

$$I(J^P) = \frac{1}{2}(0^-)$$

Mass  $m = 493.677 \pm 0.016$  MeV [a] ( $S = 2.8$ )

Mean life  $\tau = (1.2380 \pm 0.0021) \times 10^{-8}$  s ( $S = 1.9$ )

$$c\tau = 3.712 \text{ m}$$

**Slope parameter  $g$**  [b]

(See Particle Listings for quadratic coefficients and alternative parametrization related to  $\pi\pi$  scattering)

$$K^\pm \rightarrow \pi^\pm \pi^+ \pi^- g = -0.21134 \pm 0.00017$$

$$(g_+ - g_-) / (g_+ + g_-) = (-1.5 \pm 2.2) \times 10^{-4}$$

$$K^\pm \rightarrow \pi^\pm \pi^0 \pi^0 g = 0.626 \pm 0.007$$

$$(g_+ - g_-) / (g_+ + g_-) = (1.8 \pm 1.8) \times 10^{-4}$$

**$K^\pm$  decay form factors** [c,d]

Assuming  $\mu$ -e universality

$$\lambda_+(K_{\mu 3}^+) = \lambda_+(K_{e3}^+) = (2.97 \pm 0.05) \times 10^{-2}$$

$$\lambda_0(K_{\mu 3}^+) = (1.95 \pm 0.12) \times 10^{-2}$$

Not assuming  $\mu$ -e universality

$$\lambda_+(K_{e3}^+) = (2.98 \pm 0.05) \times 10^{-2}$$

$$\lambda_+(K_{\mu 3}^+) = (2.96 \pm 0.17) \times 10^{-2}$$

$$\lambda_0(K_{\mu 3}^+) = (1.96 \pm 0.13) \times 10^{-2}$$

→  $K_{e3}$  form factor quadratic fit

$$\lambda'_+(K_{e3}^\pm) \text{ linear coeff.} = (2.49 \pm 0.17) \times 10^{-2}$$

$$\lambda''_+(K_{e3}^\pm) \text{ quadratic coeff.} = (0.19 \pm 0.09) \times 10^{-2}$$

$$K_{e3}^+ |f_S/f_+| = (-0.3^{+0.8}_{-0.7}) \times 10^{-2}$$

$$K_{e3}^+ |f_T/f_+| = (-1.2 \pm 2.3) \times 10^{-2}$$

$$K_{\mu 3}^+ |f_S/f_+| = (0.2 \pm 0.6) \times 10^{-2}$$

$$K_{\mu 3}^+ |f_T/f_+| = (-0.1 \pm 0.7) \times 10^{-2}$$

$$K^+ \rightarrow e^+ \nu_e \gamma |F_A + F_V| = 0.133 \pm 0.008 \quad (S = 1.3)$$

$$K^+ \rightarrow \mu^+ \nu_\mu \gamma |F_A + F_V| = 0.165 \pm 0.013$$

$$K^+ \rightarrow e^+ \nu_e \gamma |F_A - F_V| < 0.49$$

$$K^+ \rightarrow \mu^+ \nu_\mu \gamma |F_A - F_V| = -0.24 \text{ to } 0.04, \text{ CL} = 90\%$$

## Charge Radius

$$\langle r \rangle = 0.560 \pm 0.031 \text{ fm}$$

## CP violation parameters

$$\Delta(K_{\pi ee}^\pm) = (-2.2 \pm 1.6) \times 10^{-2}$$

$$\Delta(K_{\pi \mu \mu}^\pm) = 0.010 \pm 0.023$$

$$\Delta(K_{\pi \pi \gamma}^\pm) = (0.0 \pm 1.2) \times 10^{-3}$$

$$A_{FB}(K_{\pi \mu \mu}^\pm) = \frac{\Gamma(\cos(\theta_{K\mu}) > 0) - \Gamma(\cos(\theta_{K\mu}) < 0)}{\Gamma(\cos(\theta_{K\mu}) > 0) + \Gamma(\cos(\theta_{K\mu}) < 0)} < 2.3 \times 10^{-2}, \text{ CL} = 90\%$$

## T violation parameters

$$K^+ \rightarrow \pi^0 \mu^+ \nu_\mu \quad P_T = (-1.7 \pm 2.5) \times 10^{-3}$$

$$K^+ \rightarrow \mu^+ \nu_\mu \gamma \quad P_T = (-0.6 \pm 1.9) \times 10^{-2}$$

$$K^+ \rightarrow \pi^0 \mu^+ \nu_\mu \quad \text{Im}(\xi) = -0.006 \pm 0.008$$

$K^-$  modes are charge conjugates of the modes below.

$K^+$ DECAY MODES	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level (MeV/c)	$p$
<b>Leptonic and semileptonic modes</b>			
$e^+ \nu_e$	$(1.581 \pm 0.008) \times 10^{-5}$		247
$\mu^+ \nu_\mu$	$(63.55 \pm 0.11) \%$	S=1.2	236
$\pi^0 e^+ \nu_e$	$(5.07 \pm 0.04) \%$	S=2.1	228
Called $K_{e3}^+$ .			
$\pi^0 \mu^+ \nu_\mu$	$(3.353 \pm 0.034) \%$	S=1.8	215
Called $K_{\mu 3}^+$ .			
$\pi^0 \pi^0 e^+ \nu_e$	$(2.2 \pm 0.4) \times 10^{-5}$		206
$\pi^+ \pi^- e^+ \nu_e$	$(4.254 \pm 0.032) \times 10^{-5}$		203
$\pi^+ \pi^- \mu^+ \nu_\mu$	$(1.4 \pm 0.9) \times 10^{-5}$		151
$\pi^0 \pi^0 \pi^0 e^+ \nu_e$	$< 3.5 \times 10^{-6}$ CL=90%		135
<b>Hadronic modes</b>			
$\pi^+ \pi^0$	$(20.66 \pm 0.08) \%$	S=1.2	205
$\pi^+ \pi^0 \pi^0$	$(1.761 \pm 0.022) \%$	S=1.1	133
$\pi^+ \pi^+ \pi^-$	$(5.59 \pm 0.04) \%$	S=1.3	125
<b>Leptonic and semileptonic modes with photons</b>			
$\mu^+ \nu_\mu \gamma$	[e,f] $(6.2 \pm 0.8) \times 10^{-3}$		236
$\mu^+ \nu_\mu \gamma (\text{SD}^+)$	[c,g] $(1.33 \pm 0.22) \times 10^{-5}$		-
$\mu^+ \nu_\mu \gamma (\text{SD}^+ \text{INT})$	[c,g] $< 2.7 \times 10^{-5}$ CL=90%		-
$\mu^+ \nu_\mu \gamma (\text{SD}^- + \text{SD}^- \text{INT})$	[c,g] $< 2.6 \times 10^{-4}$ CL=90%		-

$e^+ \nu_e \gamma$	(	9.4	$\pm 0.4$	) $\times 10^{-6}$	247	
$\pi^0 e^+ \nu_e \gamma$	[e,f]	(	2.56	$\pm 0.16$	) $\times 10^{-4}$	228
$\pi^0 e^+ \nu_e \gamma$ (SD)	[c,g]	<	5.3	$\times 10^{-5}$	CL=90%	228
$\pi^0 \mu^+ \nu_\mu \gamma$	[e,f]	(	1.25	$\pm 0.25$	) $\times 10^{-5}$	215
$\pi^0 \pi^0 e^+ \nu_e \gamma$	<	5	$\times 10^{-6}$	CL=90%	206	

**Hadronic modes with photons or  $\ell\bar{\ell}$  pairs**

$\pi^+ \pi^0 \gamma$ (INT)	(	-4.2	$\pm 0.9$	) $\times 10^{-6}$	-	
$\pi^+ \pi^0 \gamma$ (DE)	[e,h]	(	6.0	$\pm 0.4$	) $\times 10^{-6}$	205
$\pi^+ \pi^0 \pi^0 \gamma$	[e,f]	(	7.6	$+6.0$ $-3.0$	) $\times 10^{-6}$	133
$\pi^+ \pi^+ \pi^- \gamma$	[e,f]	(	1.04	$\pm 0.31$	) $\times 10^{-4}$	125
$\pi^+ \gamma \gamma$	[e]	(	1.10	$\pm 0.32$	) $\times 10^{-6}$	227
$\pi^+ 3\gamma$	[e]	<	1.0	$\times 10^{-4}$	CL=90%	227
$\pi^+ e^+ e^- \gamma$	(	1.19	$\pm 0.13$	) $\times 10^{-8}$	227	

**Leptonic modes with  $\ell\bar{\ell}$  pairs**

$e^+ \nu_e \nu \bar{\nu}$	<	6	$\times 10^{-5}$	CL=90%	247
$\mu^+ \nu_\mu \nu \bar{\nu}$	<	6.0	$\times 10^{-6}$	CL=90%	236
$e^+ \nu_e e^+ e^-$	(	2.48	$\pm 0.20$	) $\times 10^{-8}$	247
$\mu^+ \nu_\mu e^+ e^-$	(	7.06	$\pm 0.31$	) $\times 10^{-8}$	236
$e^+ \nu_e \mu^+ \mu^-$	(	1.7	$\pm 0.5$	) $\times 10^{-8}$	223
$\mu^+ \nu_\mu \mu^+ \mu^-$	<	4.1	$\times 10^{-7}$	CL=90%	185

**Lepton Family number (*LF*), Lepton number (*L*),  $\Delta S = \Delta Q$  (*SQ*)  
violating modes, or  $\Delta S = 1$  weak neutral current (*S1*) modes**

$\pi^+ \pi^+ e^- \bar{\nu}_e$	SQ	<	1.3	$\times 10^{-8}$	CL=90%	203	
$\pi^+ \pi^+ \mu^- \bar{\nu}_\mu$	SQ	<	3.0	$\times 10^{-6}$	CL=95%	151	
$\pi^+ e^+ e^-$	S1	(	3.00	$\pm 0.09$	) $\times 10^{-7}$	227	
$\pi^+ \mu^+ \mu^-$	S1	(	9.4	$\pm 0.6$	) $\times 10^{-8}$	S=2.6	172
$\pi^+ \nu \bar{\nu}$	S1	(	1.7	$\pm 1.1$	) $\times 10^{-10}$	227	
$\pi^+ \pi^0 \nu \bar{\nu}$	S1	<	4.3	$\times 10^{-5}$	CL=90%	205	
$\mu^- \nu e^+ e^+$	LF	<	2.1	$\times 10^{-8}$	CL=90%	236	
$\mu^+ \nu_e$	LF	[i] <	4	$\times 10^{-3}$	CL=90%	236	
$\pi^+ \mu^+ e^-$	LF	<	1.3	$\times 10^{-11}$	CL=90%	214	
$\pi^+ \mu^- e^+$	LF	<	5.2	$\times 10^{-10}$	CL=90%	214	
$\pi^- \mu^+ e^+$	L	<	5.0	$\times 10^{-10}$	CL=90%	214	
$\pi^- e^+ e^+$	L	<	6.4	$\times 10^{-10}$	CL=90%	227	
$\pi^- \mu^+ \mu^+$	L	[i] <	1.1	$\times 10^{-9}$	CL=90%	172	
$\mu^+ \bar{\nu}_e$	L	[i] <	3.3	$\times 10^{-3}$	CL=90%	236	
$\pi^0 e^+ \bar{\nu}_e$	L	<	3	$\times 10^{-3}$	CL=90%	228	
$\pi^+ \gamma$	[j] <	2.3	$\times 10^{-9}$	CL=90%	227		

## $K^0$

$$I(J^P) = \frac{1}{2}(0^-)$$

50%  $K_S$ , 50%  $K_L$

Mass  $m = 497.614 \pm 0.024$  MeV ( $S = 1.6$ )

$m_{K^0} - m_{K^\pm} = 3.937 \pm 0.028$  MeV ( $S = 1.8$ )

### Mean Square Charge Radius

$$\langle r^2 \rangle = -0.077 \pm 0.010 \text{ fm}^2$$

### T-violation parameters in $K^0$ - $\bar{K}^0$ mixing [d]

Asymmetry  $A_T$  in  $K^0$ - $\bar{K}^0$  mixing =  $(6.6 \pm 1.6) \times 10^{-3}$

### CPT-violation parameters [d]

→  $\text{Re } \delta = (2.5 \pm 2.3) \times 10^{-4}$

→  $\text{Im } \delta = (-1.5 \pm 1.6) \times 10^{-5}$

$\text{Re}(y)$ ,  $K_{e3}$  parameter =  $(0.4 \pm 2.5) \times 10^{-3}$

$\text{Re}(x_-)$ ,  $K_{e3}$  parameter =  $(-2.9 \pm 2.0) \times 10^{-3}$

→  $|m_{K^0} - m_{\bar{K}^0}| / m_{\text{average}} < 6 \times 10^{-19}$ , CL = 90% [k]

→  $(\Gamma_{K^0} - \Gamma_{\bar{K}^0}) / m_{\text{average}} = (8 \pm 8) \times 10^{-18}$

### Tests of $\Delta S = \Delta Q$

$\text{Re}(x_+)$ ,  $K_{e3}$  parameter =  $(-0.9 \pm 3.0) \times 10^{-3}$

## $K_S^0$

$$I(J^P) = \frac{1}{2}(0^-)$$

Mean life  $\tau = (0.8954 \pm 0.0004) \times 10^{-10}$  s ( $S = 1.1$ ) Assuming CPT

Mean life  $\tau = (0.89564 \pm 0.00033) \times 10^{-10}$  s Not assuming CPT

$c\tau = 2.6844$  cm Assuming CPT

### CP-violation parameters [l]

→  $\text{Im}(\eta_{+-0}) = -0.002 \pm 0.009$

→  $\text{Im}(\eta_{000}) = (-0.1 \pm 1.6) \times 10^{-2}$

→  $|\eta_{000}| = |A(K_S^0 \rightarrow 3\pi^0)/A(K_L^0 \rightarrow 3\pi^0)| < 0.018$ , CL = 90%  
CP asymmetry  $A$  in  $\pi^+\pi^-e^+e^-$  =  $(-0.4 \pm 0.8)\%$

<b><math>K_S^0</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	$p$ (MeV/c)
<b>Hadronic modes</b>			
$\pi^0 \pi^0$	( $30.69 \pm 0.05$ ) %		209
$\pi^+ \pi^-$	( $69.20 \pm 0.05$ ) %		206
$\pi^+ \pi^- \pi^0$	( $3.5 \pm 1.1$ ) $\times 10^{-7}$		133
<b>Modes with photons or <math>\ell\bar{\ell}</math> pairs</b>			
$\pi^+ \pi^- \gamma$	[ $f,n$ ] ( $1.79 \pm 0.05$ ) $\times 10^{-3}$		206
$\pi^+ \pi^- e^+ e^-$	( $4.79 \pm 0.15$ ) $\times 10^{-5}$		206
$\pi^0 \gamma\gamma$	[ $n$ ] ( $4.9 \pm 1.8$ ) $\times 10^{-8}$		231
$\gamma\gamma$	( $2.63 \pm 0.17$ ) $\times 10^{-6}$	S=3.0	249
<b>Semileptonic modes</b>			
$\rightarrow \pi^\pm e^\mp \nu_e$	[ $\sigma$ ] ( $7.04 \pm 0.08$ ) $\times 10^{-4}$		229
<b><math>CP</math> violating (<math>CP</math>) and <math>\Delta S = 1</math> weak neutral current (<math>S1</math>) modes</b>			
$3\pi^0$	$CP$ < 1.2 $\times 10^{-7}$	CL=90%	139
$\mu^+ \mu^-$	$S1$ < 9 $\times 10^{-9}$	CL=90%	225
$e^+ e^-$	$S1$ < 9 $\times 10^{-9}$	CL=90%	249
$\pi^0 e^+ e^-$	$S1$ [ $n$ ] ( $3.0 \pm 1.5$ ) $\times 10^{-9}$		230
$\pi^0 \mu^+ \mu^-$	$S1$ ( $2.9 \pm 1.5$ ) $\times 10^{-9}$		177

**$K_L^0$**

$$I(J^P) = \frac{1}{2}(0^-)$$

$$\begin{aligned}
 m_{K_L} - m_{K_S} \\
 &= (0.5293 \pm 0.0009) \times 10^{10} \text{ } \hbar \text{ s}^{-1} \quad (S = 1.3) \quad \text{Assuming CPT} \\
 &= (3.484 \pm 0.006) \times 10^{-12} \text{ MeV} \quad \text{Assuming CPT} \\
 &= (0.5289 \pm 0.0010) \times 10^{10} \text{ } \hbar \text{ s}^{-1} \quad \text{Not assuming CPT} \\
 \rightarrow &\text{ Mean life } \tau = (5.116 \pm 0.021) \times 10^{-8} \text{ s} \quad (S = 1.1) \\
 &c\tau = 15.34 \text{ m}
 \end{aligned}$$

### Slope parameter $g$ <sup>[b]</sup>

(See Particle Listings for quadratic coefficients)

$$K_L^0 \rightarrow \pi^+ \pi^- \pi^0: g = 0.678 \pm 0.008 \quad (S = 1.5)$$

### $K_L$ decay form factors <sup>[d]</sup>

Linear parametrization assuming  $\mu$ -e universality

$$\begin{aligned}
 \lambda_+(K_{\mu 3}^0) &= \lambda_+(K_{e 3}^0) = (2.82 \pm 0.04) \times 10^{-2} \quad (S = 1.1) \\
 \lambda_0(K_{\mu 3}^0) &= (1.38 \pm 0.18) \times 10^{-2} \quad (S = 2.2)
 \end{aligned}$$

Quadratic parametrization assuming  $\mu$ -e universality

$$\lambda'_+(K_{\mu 3}^0) = \lambda'_+(K_{e3}^0) = (2.40 \pm 0.12) \times 10^{-2} \quad (S = 1.2)$$

$$\lambda''_+(K_{\mu 3}^0) = \lambda''_+(K_{e3}^0) = (0.20 \pm 0.05) \times 10^{-2} \quad (S = 1.2)$$

$$\lambda_0(K_{\mu 3}^0) = (1.16 \pm 0.09) \times 10^{-2} \quad (S = 1.2)$$

Pole parametrization assuming  $\mu$ -e universality

$$M_V^\mu(K_{\mu 3}^0) = M_V^e(K_{e3}^0) = 878 \pm 6 \text{ MeV} \quad (S = 1.1)$$

$$M_S^\mu(K_{\mu 3}^0) = 1252 \pm 90 \text{ MeV} \quad (S = 2.6)$$

Dispersive parametrization assuming  $\mu$ -e universality

$$\Lambda_+ = (0.251 \pm 0.006) \times 10^{-1} \quad (S = 1.5)$$

$$\ln(C) = (1.75 \pm 0.18) \times 10^{-1} \quad (S = 2.0)$$

$$K_{e3}^0 \quad |f_S/f_+| = (1.5^{+1.4}_{-1.6}) \times 10^{-2}$$

$$K_{e3}^0 \quad |f_T/f_+| = (5^{+4}_{-5}) \times 10^{-2}$$

$$K_{\mu 3}^0 \quad |f_T/f_+| = (12 \pm 12) \times 10^{-2}$$

$$K_L \rightarrow \ell^+ \ell^- \gamma, K_L \rightarrow \ell^+ \ell^- \ell'^+ \ell'^-: \alpha_{K^*} = -0.205 \pm 0.022 \quad (S = 1.8)$$

$$K_L^0 \rightarrow \ell^+ \ell^- \gamma, K_L^0 \rightarrow \ell^+ \ell^- \ell'^+ \ell'^-: \alpha_{DIP} = -1.69 \pm 0.08 \quad (S = 1.7)$$

$$K_L \rightarrow \pi^+ \pi^- e^+ e^-: a_1/a_2 = -0.737 \pm 0.014 \text{ GeV}^2$$

$$K_L \rightarrow \pi^0 2\gamma: a_V = -0.43 \pm 0.06 \quad (S = 1.5)$$



### **CP-violation parameters [1]**

$$A_L = (0.332 \pm 0.006)\%$$

$$|\eta_{00}| = (2.220 \pm 0.011) \times 10^{-3} \quad (S = 1.8)$$

$$|\eta_{+-}| = (2.232 \pm 0.011) \times 10^{-3} \quad (S = 1.8)$$

$$|\epsilon| = (2.228 \pm 0.011) \times 10^{-3} \quad (S = 1.8)$$

$$|\eta_{00}/\eta_{+-}| = 0.9950 \pm 0.0007 [p] \quad (S = 1.6)$$

$$\text{Re}(\epsilon'/\epsilon) = (1.66 \pm 0.23) \times 10^{-3} [p] \quad (S = 1.6)$$

Assuming CPT

$$\phi_{+-} = (43.51 \pm 0.05)^\circ \quad (S = 1.2)$$

$$\phi_{00} = (43.52 \pm 0.05)^\circ \quad (S = 1.3)$$

$$\phi_\epsilon = \phi_{SW} = (43.52 \pm 0.05)^\circ \quad (S = 1.2)$$

$$\text{Im}(\epsilon'/\epsilon) = -(\phi_{00} - \phi_{+-})/3 = (-0.002 \pm 0.005)^\circ \quad (S = 1.7)$$

Not assuming *CPT*

$$\phi_{+-} = (43.4 \pm 0.5)^\circ \quad (S = 1.2)$$

$$\phi_{00} = (43.7 \pm 0.6)^\circ \quad (S = 1.2)$$

$$\phi_\epsilon = (43.5 \pm 0.5)^\circ \quad (S = 1.3)$$

*CP* asymmetry  $A$  in  $K_L^0 \rightarrow \pi^+ \pi^- e^+ e^- = (13.7 \pm 1.5)\%$

$\beta_{CP}$  from  $K_L^0 \rightarrow e^+ e^- e^+ e^- = -0.19 \pm 0.07$

$\gamma_{CP}$  from  $K_L^0 \rightarrow e^+ e^- e^+ e^- = 0.01 \pm 0.11 \quad (S = 1.6)$

$j$  for  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 = 0.0012 \pm 0.0008$

$f$  for  $K_L^0 \rightarrow \pi^+ \pi^- \pi^0 = 0.004 \pm 0.006$

$$|\eta_{+-\gamma}| = (2.35 \pm 0.07) \times 10^{-3}$$

$$\phi_{+-\gamma} = (44 \pm 4)^\circ$$

$$|\epsilon'_{+-\gamma}|/\epsilon < 0.3, \text{ CL} = 90\%$$

$$|g_{E1}| \text{ for } K_L^0 \rightarrow \pi^+ \pi^- \gamma < 0.21, \text{ CL} = 90\%$$

### **T-violation parameters**

$$\text{Im}(\xi) \text{ in } K_{\mu 3}^0 = -0.007 \pm 0.026$$

### **CPT invariance tests**

$$\phi_{00} - \phi_{+-} = (0.34 \pm 0.32)^\circ$$

$$\text{Re}(\frac{2}{3}\eta_{+-} + \frac{1}{3}\eta_{00}) - \frac{A_L}{2} = (-3 \pm 35) \times 10^{-6}$$

### **$\Delta S = -\Delta Q$ in $K_{\ell 3}^0$ decay**

$$\text{Re } x = -0.002 \pm 0.006$$

$$\text{Im } x = 0.0012 \pm 0.0021$$

<b><math>K_L^0</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level(MeV/c)	$p$
<b>Semileptonic modes</b>			
$\pi^\pm e^\mp \nu_e$ Called $K_{e3}^0$ .	[o] $(40.55 \pm 0.11) \%$	S=1.7	229
$\pi^\pm \mu^\mp \nu_\mu$ Called $K_{\mu 3}^0$ .	[o] $(27.04 \pm 0.07) \%$	S=1.1	216
$(\pi \mu \text{atom}) \nu$	$(1.05 \pm 0.11) \times 10^{-7}$		188
$\pi^0 \pi^\pm e^\mp \nu$	[o] $(5.20 \pm 0.11) \times 10^{-5}$		207
$\pi^\pm e^\mp \nu e^+ e^-$	[o] $(1.26 \pm 0.04) \times 10^{-5}$		229
<b>Hadronic modes, including Charge conjugation <math>\times</math> Parity Violating (CPV) modes</b>			
$3\pi^0$	$(19.52 \pm 0.12) \%$	S=1.6	139
$\pi^+ \pi^- \pi^0$	$(12.54 \pm 0.05) \%$		133
$\pi^+ \pi^-$	CPV [q] $(1.967 \pm 0.010) \times 10^{-3}$	S=1.5	206
$\pi^0 \pi^0$	CPV $(8.64 \pm 0.06) \times 10^{-4}$	S=1.8	209
<b>Semileptonic modes with photons</b>			
$\pi^\pm e^\mp \nu_e \gamma$	[f,o,r] $(3.79 \pm 0.06) \times 10^{-3}$		229
$\pi^\pm \mu^\mp \nu_\mu \gamma$	$(5.65 \pm 0.23) \times 10^{-4}$		216
<b>Hadronic modes with photons or <math>\ell \bar{\ell}</math> pairs</b>			
$\pi^0 \pi^0 \gamma$	$< 2.43 \times 10^{-7}$	CL=90%	209
$\pi^+ \pi^- \gamma$	[f,r] $(4.15 \pm 0.15) \times 10^{-5}$	S=2.8	206
$\pi^+ \pi^- \gamma$ (DE)	$(2.84 \pm 0.11) \times 10^{-5}$	S=2.0	206
$\pi^0 2\gamma$	[r] $(1.273 \pm 0.033) \times 10^{-6}$		231
$\pi^0 \gamma e^+ e^-$	$(1.62 \pm 0.17) \times 10^{-8}$		230
<b>Other modes with photons or <math>\ell \bar{\ell}</math> pairs</b>			
$2\gamma$	$(5.47 \pm 0.04) \times 10^{-4}$	S=1.1	249
$3\gamma$	$< 7.4 \times 10^{-8}$	CL=90%	249
$e^+ e^- \gamma$	$(9.4 \pm 0.4) \times 10^{-6}$	S=2.0	249
$\mu^+ \mu^- \gamma$	$(3.59 \pm 0.11) \times 10^{-7}$	S=1.3	225
$e^+ e^- \gamma \gamma$	[r] $(5.95 \pm 0.33) \times 10^{-7}$		249
$\mu^+ \mu^- \gamma \gamma$	[r] $(1.0 \pm 0.8) \times 10^{-8}$		225
<b>Charge conjugation <math>\times</math> Parity (CP) or Lepton Family number (LF) violating modes, or <math>\Delta S = 1</math> weak neutral current (S1) modes</b>			
$\mu^+ \mu^-$	S1 $(6.84 \pm 0.11) \times 10^{-9}$		225
$e^+ e^-$	S1 $(9 \pm 6) \times 10^{-12}$		249
$\pi^+ \pi^- e^+ e^-$	S1 [r] $(3.11 \pm 0.19) \times 10^{-7}$		206
$\pi^0 \pi^0 e^+ e^-$	S1 $< 6.6 \times 10^{-9}$	CL=90%	209
$\pi^0 \pi^0 \mu^+ \mu^-$	S1 $< 9.2 \times 10^{-11}$	CL=90%	57
$\mu^+ \mu^- e^+ e^-$	S1 $(2.69 \pm 0.27) \times 10^{-9}$		225

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$e^+ e^- e^+ e^-$	$S1$	$( 3.56 \pm 0.21 ) \times 10^{-8}$		249
$\pi^0 \mu^+ \mu^-$	$CP, S1$	$[s] < 3.8 \times 10^{-10}$	CL=90%	177
$\pi^0 e^+ e^-$	$CP, S1$	$[s] < 2.8 \times 10^{-10}$	CL=90%	230
$\pi^0 \nu \bar{\nu}$	$CP, S1$	$[t] < 2.6 \times 10^{-8}$	CL=90%	231
$\pi^0 \pi^0 \nu \bar{\nu}$	$S1$	$< 8.1 \times 10^{-7}$	CL=90%	209
$e^\pm \mu^\mp$	$LF$	$[o] < 4.7 \times 10^{-12}$	CL=90%	238
$e^\pm e^\pm \mu^\mp \mu^\mp$	$LF$	$[o] < 4.12 \times 10^{-11}$	CL=90%	225
$\pi^0 \mu^\pm e^\mp$	$LF$	$[o] < 7.6 \times 10^{-11}$	CL=90%	217
$\pi^0 \pi^0 \mu^\pm e^\mp$	$LF$	$< 1.7 \times 10^{-10}$	CL=90%	159

**K\*(892)**

$$I(J^P) = \frac{1}{2}(1^-)$$

$K^*(892)^\pm$  hadroproduced mass  $m = 891.66 \pm 0.26$  MeV

$K^*(892)^\pm$  in  $\tau$  decays mass  $m = 895.5 \pm 0.8$  MeV

$K^*(892)^0$  mass  $m = 895.81 \pm 0.19$  MeV (S = 1.4)

$K^*(892)^\pm$  hadroproduced full width  $\Gamma = 50.8 \pm 0.9$  MeV

$K^*(892)^\pm$  in  $\tau$  decays full width  $\Gamma = 46.2 \pm 1.3$  MeV

$K^*(892)^0$  full width  $\Gamma = 47.4 \pm 0.6$  MeV (S = 2.2)

<b>K*(892) DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$p$ (MeV/c)
$K\pi$	$\sim 100$ %		289
$K^0 \gamma$	$( 2.46 \pm 0.21 ) \times 10^{-3}$		307
$K^\pm \gamma$	$( 9.9 \pm 0.9 ) \times 10^{-4}$		309
$K\pi\pi$	$< 7 \times 10^{-4}$	95%	223

**K<sub>1</sub>(1270)**

$$I(J^P) = \frac{1}{2}(1^+)$$

Mass  $m = 1272 \pm 7$  MeV [u]

Full width  $\Gamma = 90 \pm 20$  MeV [u]

<b>K<sub>1</sub>(1270) DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\rho$	$(42 \pm 6) \%$	46
$K_0^*(1430)\pi$	$(28 \pm 4) \%$	†
$K^*(892)\pi$	$(16 \pm 5) \%$	302
$K\omega$	$(11.0 \pm 2.0) \%$	†
$Kf_0(1370)$	$( 3.0 \pm 2.0 ) \%$	†
$\gamma K^0$	seen	539

**$K_1(1400)$** 

$$I(J^P) = \frac{1}{2}(1^+)$$

Mass  $m = 1403 \pm 7$  MeVFull width  $\Gamma = 174 \pm 13$  MeV ( $S = 1.6$ )

<b><math>K_1(1400)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K^*(892)\pi$	(94 $\pm 6$ ) %	402
$K\rho$	( 3.0 $\pm 3.0$ ) %	293
$Kf_0(1370)$	( 2.0 $\pm 2.0$ ) %	†
$K\omega$	( 1.0 $\pm 1.0$ ) %	284
$K_0^*(1430)\pi$	not seen	†
$\gamma K^0$	seen	613

 **$K^*(1410)$** 

$$I(J^P) = \frac{1}{2}(1^-)$$

Mass  $m = 1414 \pm 15$  MeV ( $S = 1.3$ )Full width  $\Gamma = 232 \pm 21$  MeV ( $S = 1.1$ )

<b><math>K^*(1410)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$p$ (MeV/c)
$K^*(892)\pi$	> 40 %	95%	410
$K\pi$	( 6.6 $\pm 1.3$ ) %	612	
$K\rho$	< 7 %	95%	305
$\gamma K^0$	seen		619

 **$K_0^*(1430)^{[v]}$** 

$$I(J^P) = \frac{1}{2}(0^+)$$

Mass  $m = 1425 \pm 50$  MeVFull width  $\Gamma = 270 \pm 80$  MeV

<b><math>K_0^*(1430)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi$	(93 $\pm 10$ ) %	619

 **$K_2^*(1430)$** 

$$I(J^P) = \frac{1}{2}(2^+)$$

 $K_2^*(1430)^{\pm}$  mass  $m = 1425.6 \pm 1.5$  MeV ( $S = 1.1$ ) $K_2^*(1430)^0$  mass  $m = 1432.4 \pm 1.3$  MeV $K_2^*(1430)^{\pm}$  full width  $\Gamma = 98.5 \pm 2.7$  MeV ( $S = 1.1$ ) $K_2^*(1430)^0$  full width  $\Gamma = 109 \pm 5$  MeV ( $S = 1.9$ )

<b><math>K_2^*(1430)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Scale factor/ Confidence level	$p$ (MeV/c)
$K\pi$	$(49.9 \pm 1.2) \%$		619
$K^*(892)\pi$	$(24.7 \pm 1.5) \%$		419
$K^*(892)\pi\pi$	$(13.4 \pm 2.2) \%$		372
$K\rho$	$(8.7 \pm 0.8) \%$	S=1.2	318
$K\omega$	$(2.9 \pm 0.8) \%$		311
$K^+\gamma$	$(2.4 \pm 0.5) \times 10^{-3}$	S=1.1	627
$K\eta$	$(1.5^{+3.4}_{-1.0}) \times 10^{-3}$	S=1.3	486
$K\omega\pi$	$< 7.2 \times 10^{-4}$	CL=95%	100
$K^0\gamma$	$< 9 \times 10^{-4}$	CL=90%	626

### **$K^*(1680)$**

$$I(J^P) = \frac{1}{2}(1^-)$$

Mass  $m = 1717 \pm 27$  MeV (S = 1.4)

Full width  $\Gamma = 322 \pm 110$  MeV (S = 4.2)

<b><math>K^*(1680)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi$	$(38.7 \pm 2.5) \%$	781
$K\rho$	$(31.4^{+5.0}_{-2.1}) \%$	571
$K^*(892)\pi$	$(29.9^{+2.2}_{-5.0}) \%$	618

### **$K_2(1770)$ [x]**

$$I(J^P) = \frac{1}{2}(2^-)$$

Mass  $m = 1773 \pm 8$  MeV

Full width  $\Gamma = 186 \pm 14$  MeV

<b><math>K_2(1770)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi\pi$		794
$K_2^*(1430)\pi$	dominant	288
$K^*(892)\pi$	seen	654
$Kf_2(1270)$	seen	55
$K\phi$	seen	441
$K\omega$	seen	607

### **$K_3^*(1780)$**

$$I(J^P) = \frac{1}{2}(3^-)$$

Mass  $m = 1776 \pm 7$  MeV ( $S = 1.1$ )  
 Full width  $\Gamma = 159 \pm 21$  MeV ( $S = 1.3$ )

<b><math>K_3^*(1780)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	Confidence level	$p$ (MeV/c)
$K\rho$	(31 $\pm$ 9) %		613
$K^*(892)\pi$	(20 $\pm$ 5) %		656
$K\pi$	(18.8 $\pm$ 1.0) %		813
$K\eta$	(30 $\pm$ 13) %		719
$K_2^*(1430)\pi$	< 16 %	95%	291

### **$K_2(1820)^{[y]}$**

$$I(J^P) = \frac{1}{2}(2^-)$$

Mass  $m = 1816 \pm 13$  MeV  
 Full width  $\Gamma = 276 \pm 35$  MeV

<b><math>K_2(1820)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K_2^*(1430)\pi$	seen	327
$K^*(892)\pi$	seen	681
$Kf_2(1270)$	seen	186
$K\omega$	seen	638

### **$K_4^*(2045)$**

$$I(J^P) = \frac{1}{2}(4^+)$$

Mass  $m = 2045 \pm 9$  MeV ( $S = 1.1$ )  
 Full width  $\Gamma = 198 \pm 30$  MeV

<b><math>K_4^*(2045)</math> DECAY MODES</b>	Fraction ( $\Gamma_i/\Gamma$ )	$p$ (MeV/c)
$K\pi$	(9.9 $\pm$ 1.2) %	958
$K^*(892)\pi\pi$	(9 $\pm$ 5) %	802
$K^*(892)\pi\pi\pi$	(7 $\pm$ 5) %	768
$\rho K\pi$	(5.7 $\pm$ 3.2) %	741
$\omega K\pi$	(5.0 $\pm$ 3.0) %	738
$\phi K\pi$	(2.8 $\pm$ 1.4) %	594
$\phi K^*(892)$	(1.4 $\pm$ 0.7) %	363

## NOTES

- [a] See the note in the  $K^\pm$  Particle Listings.
- [b] The definition of the slope parameter  $g$  of the  $K \rightarrow 3\pi$  Dalitz plot is as follows (see also “Note on Dalitz Plot Parameters for  $K \rightarrow 3\pi$  Decays” in the  $K^\pm$  Particle Listings):
 
$$|M|^2 = 1 + g(s_3 - s_0)/m_{\pi^+}^2 + \dots$$
- [c] See the “Note on  $\pi^\pm \rightarrow \ell^\pm \nu \gamma$  and  $K^\pm \rightarrow \ell^\pm \nu \gamma$  Form Factors” in the  $\pi^\pm$  Particle Listings for definitions and details.
- [d] For more details and definitions of parameters see the Particle Listings.
- [e] See the  $K^\pm$  Particle Listings for the energy limits used in this measurement.
- [f] Most of this radiative mode, the low-momentum  $\gamma$  part, is also included in the parent mode listed without  $\gamma$ 's.
- [g] Structure-dependent part.
- [h] Direct-emission branching fraction.
- [i] Derived from an analysis of neutrino-oscillation experiments.
- [j] Violates angular-momentum conservation.
- [k] Derived from measured values of  $\phi_{+-}$ ,  $\phi_{00}$ ,  $|\eta|$ ,  $|m_{K_L^0} - m_{K_S^0}|$ , and  $\tau_{K_S^0}$ , as described in the introduction to “Tests of Conservation Laws.”
- [l] The  $CP$ -violation parameters are defined as follows (see also “Note on  $CP$  Violation in  $K_S \rightarrow 3\pi$ ” and “Note on  $CP$  Violation in  $K_L^0$  Decay” in the Particle Listings):

$$\begin{aligned}\eta_{+-} &= |\eta_{+-}| e^{i\phi_{+-}} = \frac{A(K_L^0 \rightarrow \pi^+ \pi^-)}{A(K_S^0 \rightarrow \pi^+ \pi^-)} = \epsilon + \epsilon' \\ \eta_{00} &= |\eta_{00}| e^{i\phi_{00}} = \frac{A(K_L^0 \rightarrow \pi^0 \pi^0)}{A(K_S^0 \rightarrow \pi^0 \pi^0)} = \epsilon - 2\epsilon' \\ \delta &= \frac{\Gamma(K_L^0 \rightarrow \pi^- \ell^+ \nu) - \Gamma(K_L^0 \rightarrow \pi^+ \ell^- \nu)}{\Gamma(K_L^0 \rightarrow \pi^- \ell^+ \nu) + \Gamma(K_L^0 \rightarrow \pi^+ \ell^- \nu)}, \\ \text{Im}(\eta_{+-0})^2 &= \frac{\Gamma(K_S^0 \rightarrow \pi^+ \pi^- \pi^0)^{CP \text{ viol.}}}{\Gamma(K_L^0 \rightarrow \pi^+ \pi^- \pi^0)}, \\ \text{Im}(\eta_{000})^2 &= \frac{\Gamma(K_S^0 \rightarrow \pi^0 \pi^0 \pi^0)}{\Gamma(K_L^0 \rightarrow \pi^0 \pi^0 \pi^0)}.\end{aligned}$$

where for the last two relations  $CPT$  is assumed valid, *i.e.*,  $\text{Re}(\eta_{+-0}) \simeq 0$  and  $\text{Re}(\eta_{000}) \simeq 0$ .

- [n] See the  $K_S^0$  Particle Listings for the energy limits used in this measurement.
- [o] The value is for the sum of the charge states or particle/antiparticle states indicated.
- [p]  $\text{Re}(\epsilon'/\epsilon) = \epsilon'/\epsilon$  to a very good approximation provided the phases satisfy  $CPT$  invariance.
- [q] This mode includes gammas from inner bremsstrahlung but not the direct emission mode  $K_L^0 \rightarrow \pi^+ \pi^- \gamma(\text{DE})$ .
- [r] See the  $K_L^0$  Particle Listings for the energy limits used in this measurement.
- [s] Allowed by higher-order electroweak interactions.
- [t] Violates  $CP$  in leading order. Test of direct  $CP$  violation since the indirect  $CP$ -violating and  $CP$ -conserving contributions are expected to be suppressed.
- [u] This is only an educated guess; the error given is larger than the error on the average of the published values. See the Particle Listings for details.
- [v] See the “Note on  $f_0(1370)$ ” in the  $f_0(1370)$  Particle Listings and in the 1994 edition.
- [x] See the note in the  $L(1770)$  Particle Listings in Reviews of Modern Physics **56** S1 (1984), p. S200. See also the “Note on  $K_2(1770)$  and the  $K_2(1820)$ ” in the  $K_2(1770)$  Particle Listings .
- [y] See the “Note on  $K_2(1770)$  and the  $K_2(1820)$ ” in the  $K_2(1770)$  Particle Listings .