

# Neutrino Physics: Lecture 12

## Sterile neutrinos

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# Outline

- 1 Short baseline experiments and LSND anomaly
- 2 Adding a fourth neutrino
- 3 Constraining the sterile neutrino
- 4 Sterile neutrino in astrophysics and cosmology

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# SBLs: When only one $\Delta m^2$ matters

No CP violation, any number of neutrinos:

$$P_{\alpha\beta} = \delta_{\alpha\beta} - \sum_{i < j} 4\text{Re}(\square_{\alpha\beta ij}) \sin^2(\Delta_{ji})$$

$$\square_{\alpha\beta ij} \equiv U_{\alpha i} U_{\beta j} U_{\alpha j}^* U_{\beta i}^*$$

Approximation of single mass-squared dominance

- All significant  $\Delta_{ji}$  nearly equal,  $\approx \Delta$
- All other  $\Delta_{ji}$  negligible,  $\approx 0$

$$P_{\alpha\alpha} = 1 - \sin^2 2\theta_{\text{eff}} \sin^2(\Delta)$$

$$P_{\alpha\beta} = \sin^2 2\theta_{\text{eff}} \sin^2(\Delta) \quad (\alpha \neq \beta)$$

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## Approximation of single mass-squared dominance

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# Equi-probability contours

$$\sin^2 2\theta_{eff} \sin^2(\Delta) = \text{Constant}$$

# Short baseline and sensitivity to $\Delta m^2$

$$\Delta \sim 1.27 \frac{\Delta m^2 (\text{eV}^2) L (\text{km})}{E (\text{GeV})}$$

Nontrivial  $P_{\alpha\alpha}$  or  $P_{\alpha\beta}$  only when  $\Delta \gtrsim 1$

- Atmospheric neutrinos:

$$E \sim 1 \text{ GeV}, L \sim 10^3 \text{ km} \Rightarrow \Delta m^2 \gtrsim 10^{-3} \text{ eV}^2$$

- Reactor neutrinos:

$$E \sim 1 \text{ MeV}, L \sim 1 \text{ km} \Rightarrow \Delta m^2 \gtrsim 10^{-3} \text{ eV}^2$$

- Long baseline experiments:

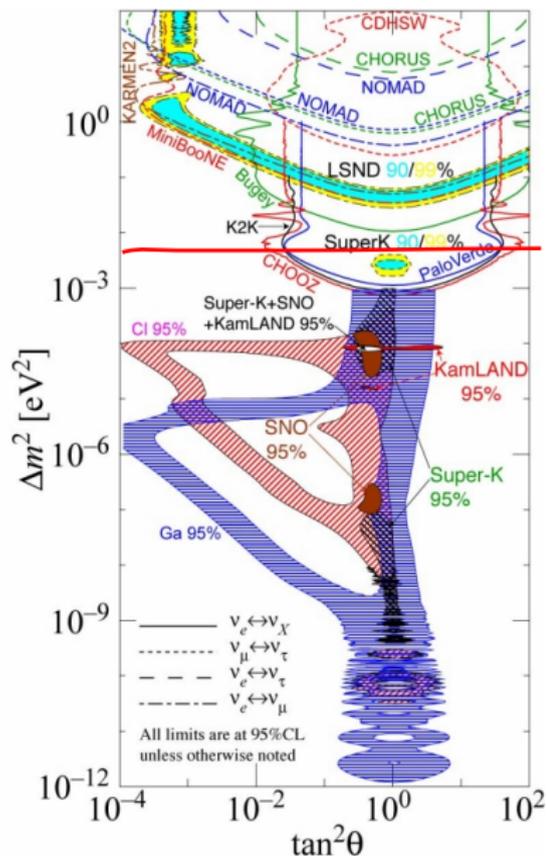
$$E \sim 1\text{--}10 \text{ GeV}, L \sim 10^3\text{--}10^4 \text{ km} \Rightarrow \Delta m^2 \gtrsim 10^{-3} \text{ eV}^2$$

- Accelerator (short baseline) experiments:

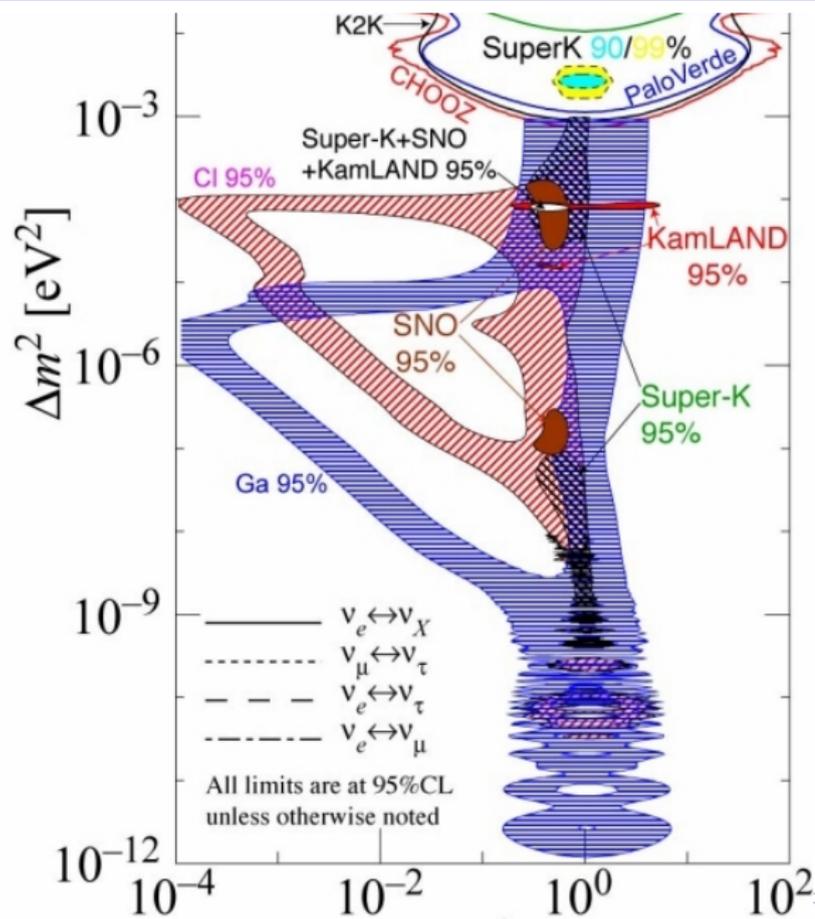
$$E \sim 10\text{--}100 \text{ MeV}, L \sim 1 \text{ km} \Rightarrow \Delta m^2 \gtrsim 10^{-2}\text{--}10^{-1} \text{ eV}^2$$

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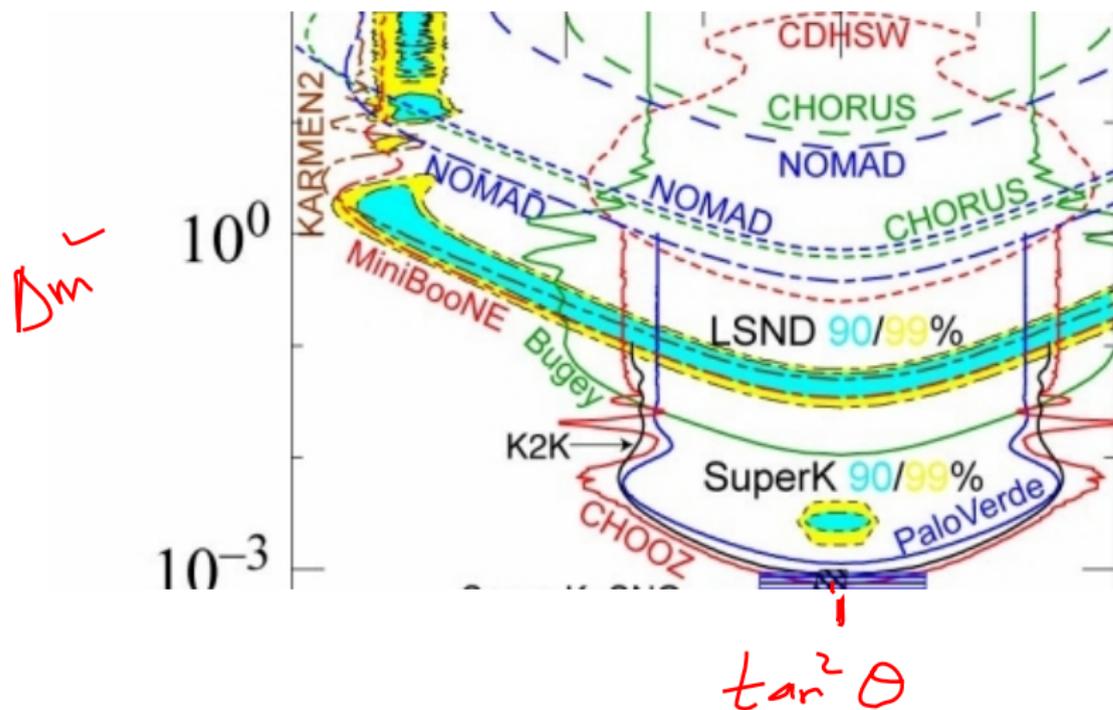
# Neutrino experiments with $2\nu$ approximation



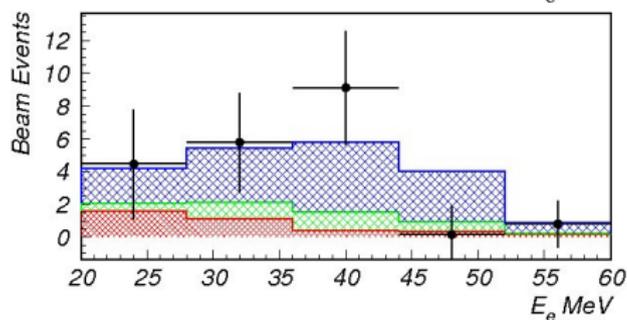
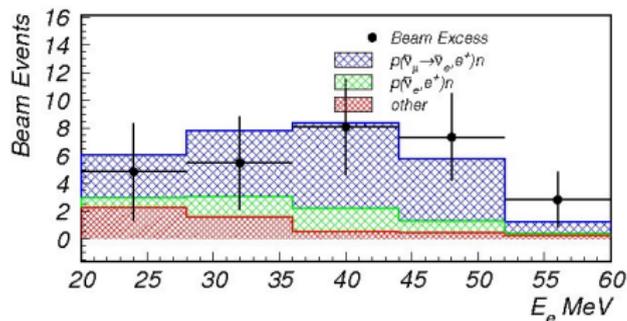
# Solar and atmospheric experiments



# Results from short baseline experiments



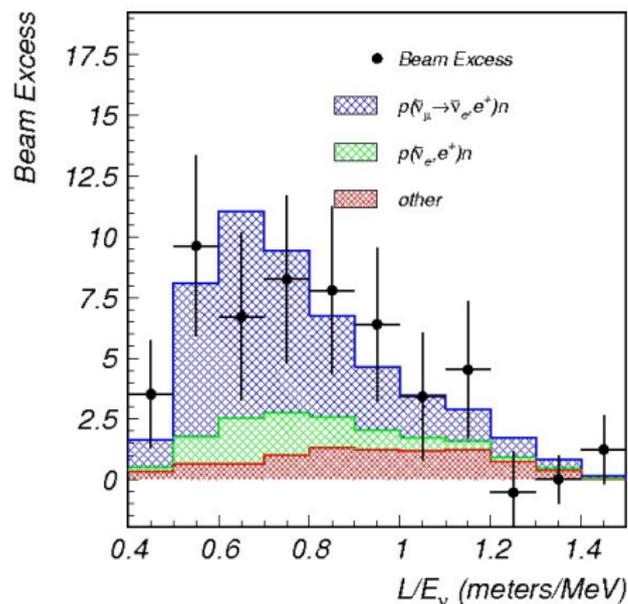
# The LSND excess



●  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  oscillations !

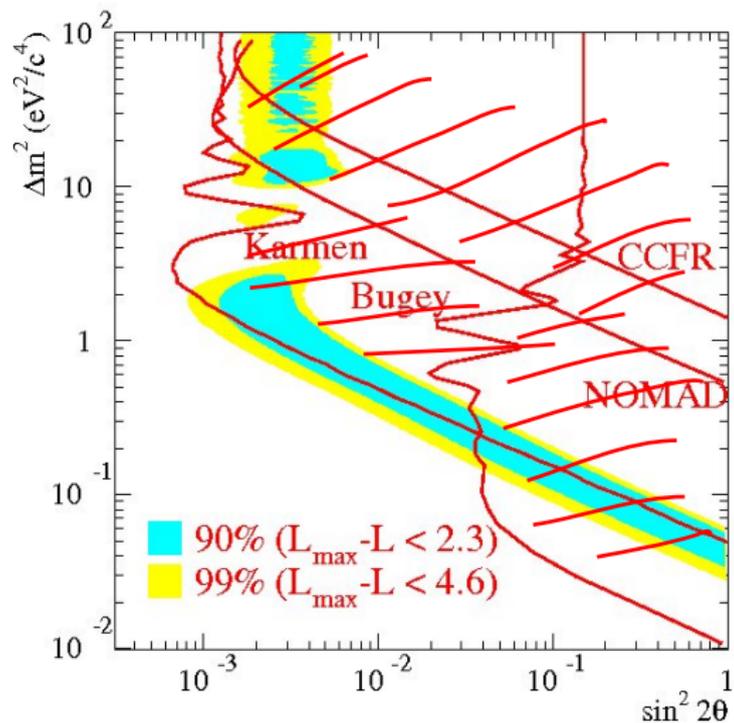
● Excess =  $87.9 \pm 22.4 \pm 6.0$  events

# $L/E$ oscillations in LSND



- Oscillation probability  $0.264 \pm 0.067 \pm 0.045$
- $\Delta m^2 \approx \underline{0.2-10 \text{ eV}^2}$

# The LSND parameter space



$\Delta m^2 \sim 1 \text{ eV}^2$   
 $\sin^2 2\theta \sim 10^{-2}$

# A fourth neutrino ?

Three independent  $\Delta m^2$ :

- $\Delta m_{\odot}^2 \approx 8 \times 10^{-5} \text{ eV}^2$  ✓

- $\Delta m_{atm}^2 \approx 2.5 \times 10^{-3} \text{ eV}^2$  ✓

- $\Delta m_{\odot}^2 \approx 0.2\text{--}10 \text{ eV}^2$  ✓

Not possible with only three neutrino masses !

A fourth neutrino species must be present

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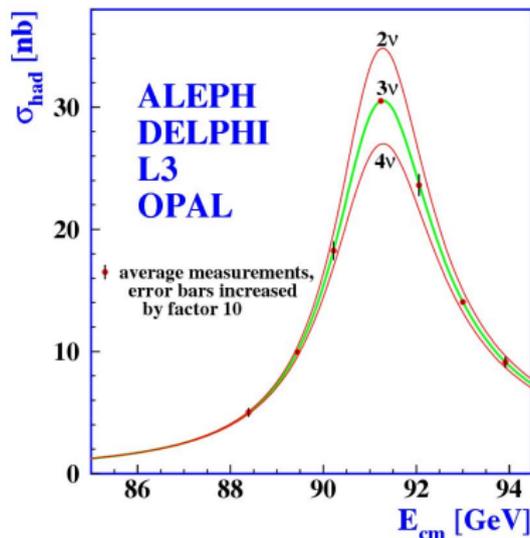
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# A fourth generation neutrino ?



- LEP:  $e^+e^- \rightarrow Z \rightarrow f\bar{f}$
- Effective number of neutrinos:  $N_\nu = 2.985 \pm 0.008$
- Only three light neutrinos interact with Z
- The fourth neutrino has to be sterile !

# What is a (light) sterile neutrino

- A fermion without electric charge
- Does not have electroweak interactions  
(Does not interact with  $W, Z, \gamma$ )
- Can have interactions beyond the Standard Model (BSM)
- Can mix with “active” neutrinos due to the BSM interactions
- NOT the right-handed partner of active neutrinos

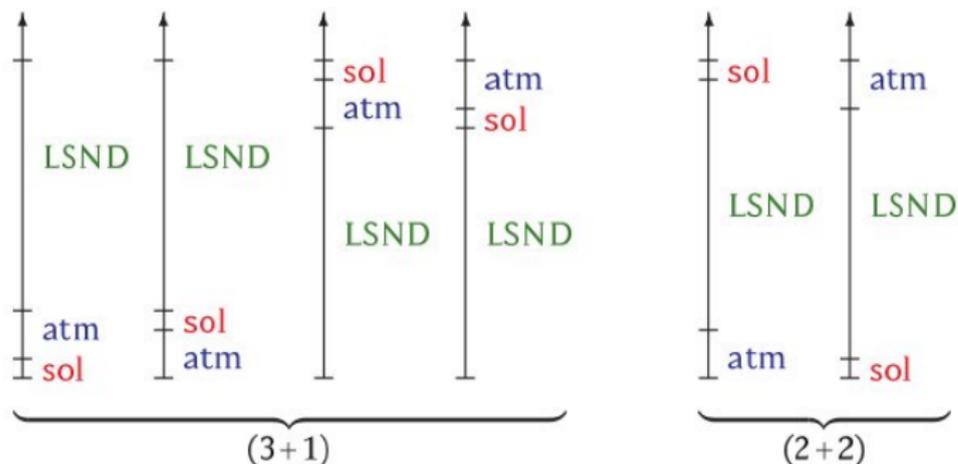
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# What would the neutrino mass spectrum look like ?



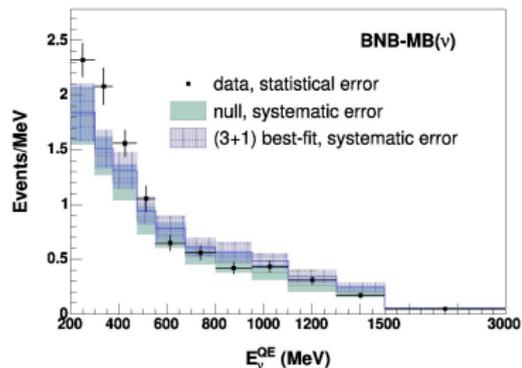
Mixing matrix: 6 angles and 10 phases

$$\begin{aligned}
 \mathcal{U} = & \Phi(\chi_1, \chi_2, \chi_3, \chi_4) U_{14}(\theta_{14}, \delta_{14}) U_{34}(\theta_{34}, 0) U_{24}(\theta_{24}, \delta_{24}) \\
 & \times U_{23}(\theta_{23}, 0) U_{13}(\theta_{13}, \delta_{13}) U_{12}(\theta_{12}, 0) \Phi(\phi_1, \phi_2, \phi_3, 0)
 \end{aligned}$$

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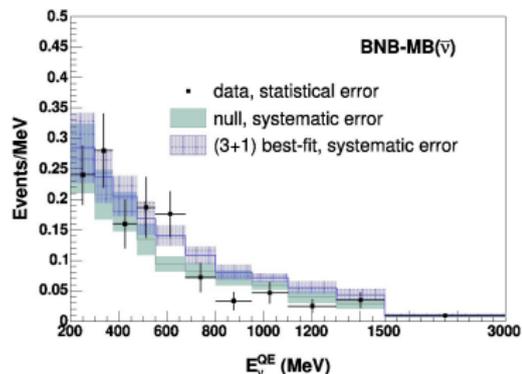
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# Testing the LSND anomaly

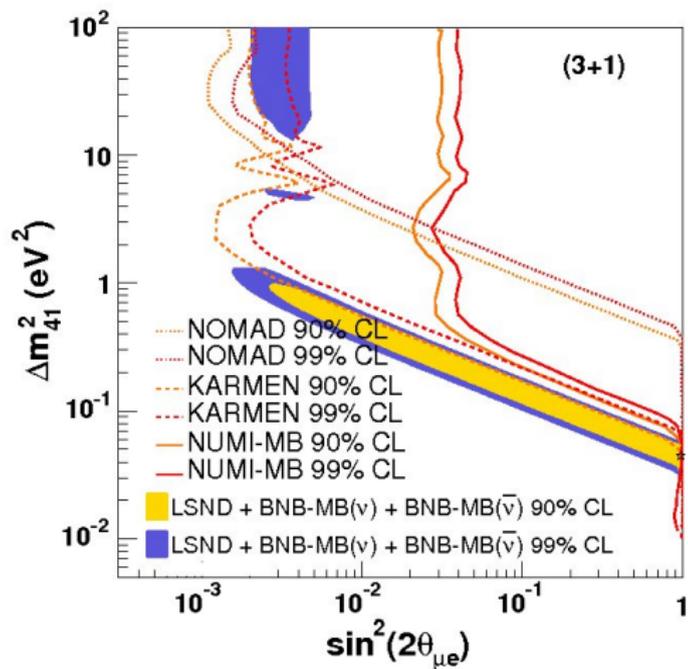


MiniBOONE:

- $E \sim 1$  GeV,  $L \sim 1$  km
- $\nu_{\mu}$  as well as  $\bar{\nu}_{\mu}$  beams



# Constraining sterile $\nu$ from appearance experiments



# Constraints from disappearance experiments

## Solar neutrinos

- SNO indicates that most  $\nu_e$  go to  $\nu_\mu$  or  $\nu_\tau$   
⇒ bound on  $\nu_e$ - $\nu_s$  mixing

## Atmospheric neutrinos

- Extra contribution to atmospheric oscillations:

$$P_{\mu\mu} \approx P_{\mu\mu}(3\nu) - \frac{1}{2} \sin^2 2\theta_{\mu s}$$

⇒ bound on  $\nu_\mu$ - $\nu_s$  mixing

## Reactor experiments

- $\Delta m_{LSND}^2$  would contribute to KamLAND, K2K, MINOS  
⇒ bound on  $\nu_e$ - $\nu_s$  and  $\nu_\mu$ - $\nu_s$  mixing
- $\Delta m_{LSND}^2$  would contribute to CHOOZ  
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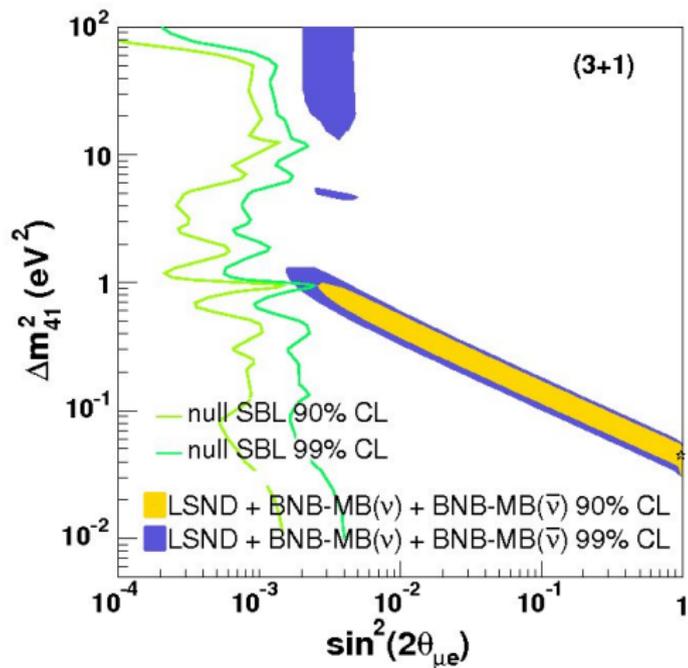
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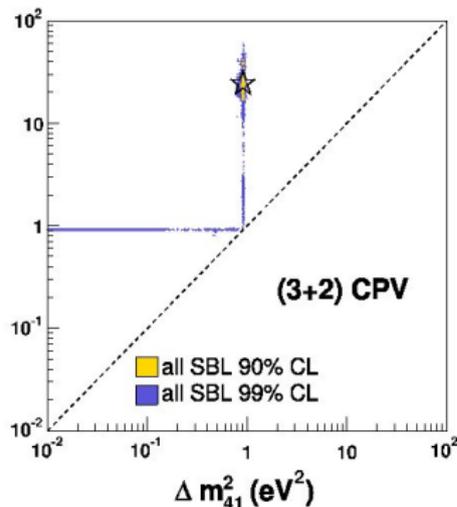
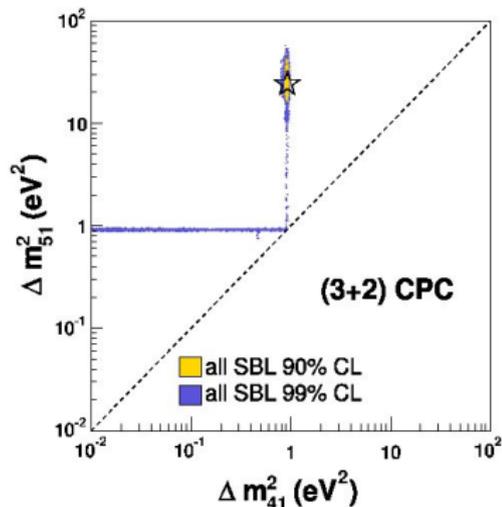
# LSND parameter space ruled out



include  
disappearance  
expts

ArXiv:0906.1997

# Can more than one sterile neutrinos help ?



- Need 2 neutrinos of masses  $\gtrsim$  eV
- Constraints from cosmology

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# Sterile neutrinos in astrophysics

- Nucleosynthesis of heavy elements (r-process)
  - Heavy elements need more neutrons
  - $\nu_e$  tend to reduce number of neutrons:  $\nu_e + n \rightarrow e^- + p$
  - $\nu_e \rightarrow \nu_s$  conversion can allow heavy elements to be formed, if  $\Delta m^2 \sim 10\text{--}100 \text{ eV}^2$
- Supernova explosions
  - Conversions to  $\nu_s$  carry away energy efficiently  
⇒ May affect explosion dynamics
  - Can create large asymmetries in  $\nu$  emission  
⇒ May explain large pulsar velocities

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# Sterile neutrinos in cosmology

- keV neutrinos are viable dark matter candidates
- Can help in producing supermassive black holes
- Predicted by some models (e.g.  $\nu$ MSM) that explain baryon asymmetry

# (Not) the last word on sterile neutrinos

- eV-neutrinos not required for explaining oscillation data,  
Not ruled out either (only mixing constrained)
- Can help some astrophysical phenomena  
if  $\Delta m^2 \sim 10\text{--}100 \text{ eV}^2$ , very small mixing
- keV-neutrinos may play a role in cosmology,  
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