

# Neutrinos: masses, mixing and symmetries

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- 1 Neutrinos: a Curriculum Vitae
  - The multifaceted neutrino
  - The knowns and the unknowns
- 2  $\mathcal{PR}$ -neutrino interaction (> 20 years)
  - Light Dirac neutrinos from SUSY GUT
  - Resolving the LSND anomaly
  - Neutrino mass models
  - Oscillation phenomenology
  - Quark-lepton symmetries and their radiative breaking
- 3 Parting shots

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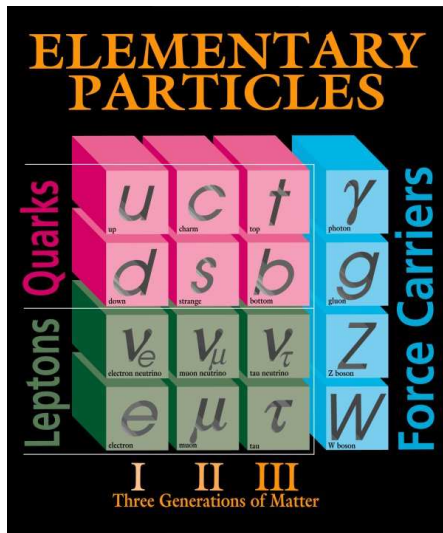
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# Aspects of neutrinos

- Particles that accompany radioactive  $\beta$  decay
- Byproducts of nuclear reactions
- The most abundant particles
- The most weakly interacting particles
- The lightest massive particles
- Particles that break left-right (mirror) symmetry maximally
- Particles that may be their own antiparticles
- Particles that may have created the matter-antimatter asymmetry

# The niche of neutrinos in the Standard Model



Fermilab 95-759

- 3 neutrinos:  
 $\nu_e, \nu_\mu, \nu_\tau$
- chargeless
- spin 1/2
- almost massless

# A brief history of neutrinos

- Postulated: 1932 (Pauli)
- Discovery of electron neutrino: 1956  
Reines-Cowan: Nobel prize 1995
- Muon neutrino  $\nu_\mu$ : 1962  
Steinberger-Schwartz-Lederman: Nobel prize 1988
- Tau neutrino  $\nu_\tau$ : 2000 (CERN)
- Solar neutrino observations: 1960's –  
Supernova neutrino observation: 1987  
Davis and Koshiba: Nobel prize 2001
- Solar neutrino puzzle: 1960's – 2002  
 $\nu_e$  mixes with  $\nu_\mu$  and  $\nu_\tau$
- Atmospheric neutrino problem: 1980's – 1998  
 $\nu_\mu$  and  $\nu_\tau$  mix almost maximally



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# Our current knowledge about neutrinos

$$(\nu_e, \nu_\mu, \nu_\tau) \leftrightarrow (\nu_1, \nu_2, \nu_3)$$

Solar, Atmospheric and Reactor neutrino experiments  $\Rightarrow$

- Mass squared differences:  $\Delta m_{21}^2 \ll \Delta m_{31}^2 \approx \Delta m_{32}^2$

$$\Delta m_{\odot}^2 \approx (7.0 - 9.3) \times 10^{-5} \text{eV}^2, \quad \Delta m_{\text{atm}}^2 \approx (1.3 - 4.2) \times 10^{-3} \text{eV}^2$$

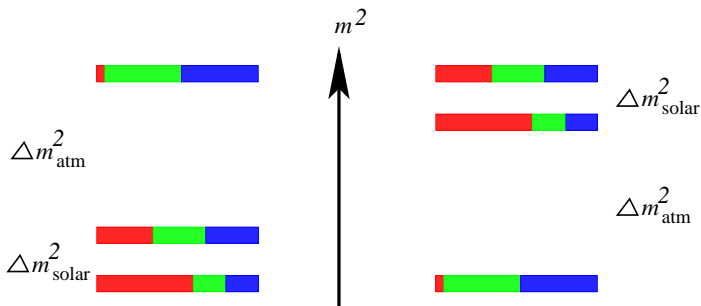
- Mixing matrix:  $U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} \end{pmatrix}$

$$|U_{e1}|^2 \approx 0.7, \quad |U_{e2}|^2 \approx 0.3, \quad |U_{\mu 3}|^2 \approx 0.5, \quad |U_{e3}|^2 < 0.05$$

Two large angles and one small angle (vanishing ??)

# Open questions in neutrino physics

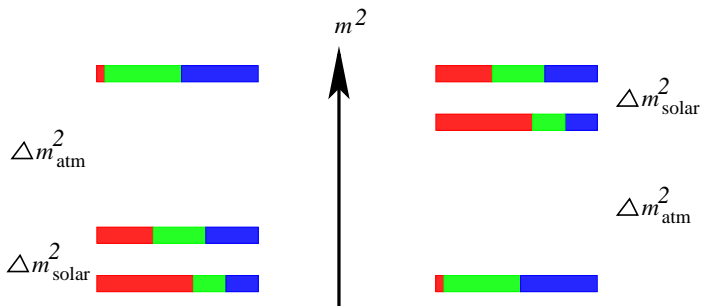
- Mass hierarchy: Normal or Inverted ? ( $\nu_e, \nu_\mu, \nu_\tau$ )



- Absolute neutrino masses
- CP violation  $\stackrel{?}{\Rightarrow}$  Leptogenesis
- Are there more than three neutrinos ?
- Origin of neutrino masses

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# Need for light Dirac neutrinos

- Seesaw mechanism for generating small neutrino masses:

$$m_\nu \approx m_D \frac{1}{M_R} m_D^T \Rightarrow \text{Neutrinos are necessarily Majorana}$$

- Experimental results in 1984:
  - Neutrinoless double beta decay  $\Rightarrow m_{ee} < 10$  eV
  - Tritium beta decay  $\Rightarrow m_{\bar{\nu}_e} > 20$  eV (Ruled out later)
- The only way to resolve: neutrinos are Dirac particles (no lepton number violation).

# Light Dirac neutrinos from SUSY SO(10) GUT

$$\begin{array}{l} \text{SO}(10) \xrightarrow{M_{GUT}} SU(2)_L \times SU(2)_R \times SU(4) \quad (10^{16} \text{ GeV}) \\ \xrightarrow{M_{SUSY}} SU(3)_C \times SU(2)_L \times U(1)_Y \quad (10^{10} \text{ GeV}) \end{array}$$

- Four chiral neutral fermions  $\equiv$  two physical Dirac neutrinos

$$M_\nu \sim \begin{pmatrix} 0 & 0 & A & 0 \\ 0 & 0 & B & C \\ A & B & 0 & 0 \\ 0 & C & 0 & 0 \end{pmatrix}$$

- Global symmetries to restrict Yukawa couplings and keep radiative corrections under control
- The mass relation  $m_\nu \sim m_u M_{SUSY}/M_{GUT}$
- $m_{\nu_e} : m_{\nu_\mu} : m_{\nu_\tau} = m_u : m_c : m_t, \quad m_{\nu_e} \approx 20\text{--}55 \text{ eV}$

*PR*, O. Shanker: PRL 1984, PRD 1984

Explicit construction of a globally SUSY SO(10) superpotential

Anjan S. Joshipura, *PR*, O. Shanker, Utpal Sarkar: PLB 1985

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# The LSND problem

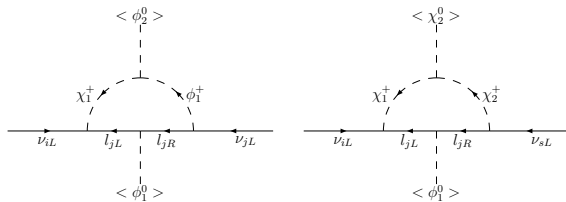
- Solar neutrino experiments  $\Rightarrow$  oscillations with  $\Delta m^2 \sim 10^{-4} \text{ eV}^2$
- Atmospheric neutrino experiments  $\Rightarrow$  oscillations with  $\Delta m^2 \sim 10^{-3} \text{ eV}^2$
- LSND experiment ( $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ )  $\Rightarrow$  oscillations with  $\Delta m^2 \sim 1 \text{ eV}^2$
- **Only 3 neutrinos  $\Rightarrow$  only 2 independent  $\Delta m^2$**
- Fourth neutrino species ? Or any other solution ?

# Discrete $Z_5$ and seesaw

- Three active and one sterile neutrino, each with left and right chiral components
- Discrete  $Z_5$  symmetry to generate hierarchy in elements of neutrino mass matrix
- Atmospheric neutrino solution through  $\nu_\mu \leftrightarrow \nu_\tau$   
Maximal  $\mu - \tau$  mixing and small mass difference from the pseudo-Dirac structure  $\begin{pmatrix} a & b \\ b & a \end{pmatrix}$
- Solar neutrino solution through  $\nu_e \leftrightarrow \nu_s \oplus \nu_e \leftrightarrow \nu_\mu$

Ernest Ma, *PR*: PRD 1995

# Radiative neutrino mass generation for 4 neutrinos



- An extension of the **Zee model**: radiative generation of  $m_{\text{active-active}}$  and  $m_{\text{active-sterile}}$  from charged Higgs exchange
- Solar:  $\nu_e \leftrightarrow \nu_s$ , Atmospheric:  $\nu_\mu \leftrightarrow \nu_\tau$  (bimaximal mixing), LSND anomaly:  $\nu_e \leftrightarrow \nu_\mu$

- Approximate relationship  $\Delta m_{\text{atm}}^2 \approx 2\sqrt{\Delta m_{\text{sol}}^2 \Delta m_{\text{LSND}}^2}$

Naveen Gaur, Ambar Ghosal, Ernest Ma, *PR*: PRD 1998

With non-maximal  $\theta_{12}$ , a modified relation

$$\sin^2 2\theta_{12} \approx 1 - [\Delta m_{\text{atm}}^2 / (4\Delta m_{\text{sol}}^2 \Delta m_{\text{LSND}}^2)]^2$$

*PR*, Sudhir K, Vempati: PRD 2002

# Solar, atmospheric and LSND from 3 neutrinos

- Atmospheric neutrinos:  $\nu_\mu \leftrightarrow \nu_\tau$  oscillations  
LSND:  $\nu_\mu \leftrightarrow \nu_e$  oscillations
- Solar neutrino conversions through new  $\nu_\tau$ -quark neutral current interactions:

$$\mathcal{L}_{\text{new}} = -\sqrt{2}\bar{\nu}_{\tau L}\gamma^\mu\nu_{\tau L}(G_{\tau V}^q\bar{q}\gamma^\mu q + G_{\tau A}^q\bar{q}\gamma^\mu\gamma^5 q)$$

- Zenith angle dependence predicted, but smaller for sub-GeV atmospheric data

Ernest Ma, *PR*: PRL 1998

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# Higher dimensional models of light Majorana neutrinos

- ADD models with a “SM” brane inside the 5-d bulk
- **No-go theorem**, using solar, atmospheric, reactor and cosmological data, for the following class of models:
  - Three or four light Majorana neutrinos on the brane
  - One or more right chiral neutrinos in the bulk
  - Flavour blind bulk - brane couplings
- **Extra dimensions, if relevant to neutrino mixing, must discriminate between neutrino flavours**

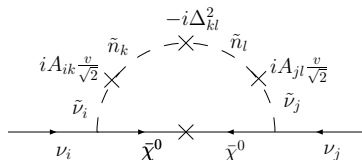
JoAnne L. Hewett, *PR*, Sourov Roy: PRD 2004

# Bi-large neutrino mixing from SUSY

- Nonlinear terms in the hidden sector generate Majorana mass terms for (s)neutrinos

$$\mathcal{L}_{\text{eff}} = \frac{1}{M_P} ([X_{ij}^\dagger N^i N^j]_D + [X_{ij}^\dagger L^i N^j H_u]_F) + H.c.$$

- Nondiagonal  $\Delta L = 2$  mass terms, almost diagonal SUSY A-terms.



- Radiatively induced masses + seesaw  $\Rightarrow$  bi-large mixing

Biswarup Mukhopadhyaya, *PR*, Raghavendra Srikanth: *PRD* 2006

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# CP violation in long baseline experiments

- Disentangling “real” CP violation from “fake” CP violation
- Lowest order analytic calculations of neutrino conversion probabilities for a **variable earth density**
- For maximal mixing, matter effects on the survival probability  $P_{\nu_\mu \rightarrow \nu_\mu}$  vanish identically

Biswajoy Brahmachari, Sandhya Choubey, *PR*: NPB 2003

# Deviation of atmospheric mixing angle from maximality

- $\theta_{23} \in (40^\circ, 60^\circ)$  at  $3\sigma$ , best fit at  $45^\circ$
- Deviation from maximality:  $D \equiv 1/2 - \sin^2 \theta_{23}$  x
- In vacuum,  $\Delta P \equiv P_{\nu_\mu \rightarrow \nu_\mu} - P_{\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu} \propto D^2$
- In matter, linear  $\Delta P$  dependence on D:  
 $\Delta P \propto |U_{e3}|^2(1 - 2|U_{\mu 3}|^2) \propto \theta_{13}^2 D$
- With  $\sin^2 2\theta_{13} > 0.08$  and  $|D| > 0.1$ , sign of D may be determined to  $3\sigma$  with 1000 kt-yr at INO
- Sign of D  $\Rightarrow$  resolution of “octant ambiguity”

Sandhya Choubey and  $\mathcal{PR}$ , PRL 2004, PRD 2006

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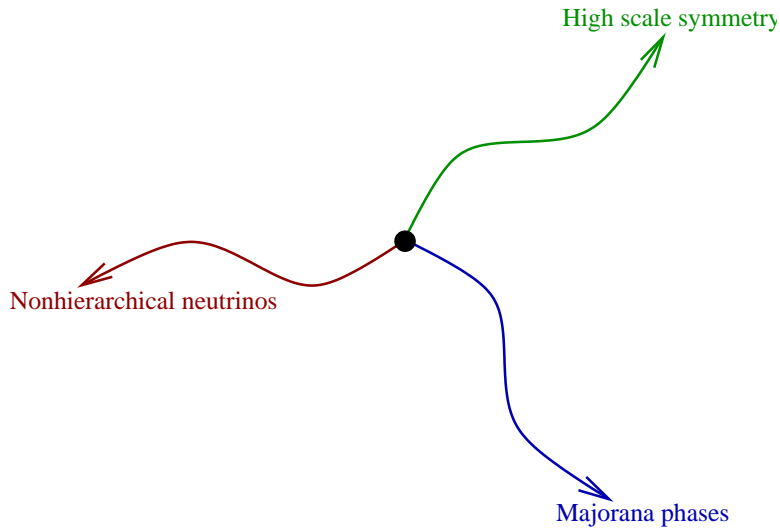
# Quark-lepton symmetries

- Quark mixing angles:  $\theta_{12}^q \equiv \theta_C \approx 12^\circ$ ,  $\theta_{23}^q \equiv |V_{cb}| \approx 2^\circ$
- Neutrino mixing angles:  $\theta_{12} \approx 34^\circ \pm 1.5^\circ$ ,  $\theta_{23} \approx 45^\circ \pm 5^\circ$
- A possible relation: “Quark-lepton complementarity (QLC)”

$$\theta_{12}^q + \theta_{12} = 45^\circ \quad (\text{Also } \theta_{23}^q + \theta_{23} \approx 45^\circ)$$

- Can be implemented in two steps:
  - Symmetry of neutrino mass matrix:  
( $\mu - \tau$  exchange/  $L_\mu - L_\tau$  gauge/  $S_3$  permutation)  $\Rightarrow$   
 $U_\nu \equiv U_{bimax} : \theta_{12} = \theta_{23} = 45^\circ, \theta_{13} = 0^\circ$
  - SO(10) GUT  $\Rightarrow U_{PMNS} = U_\nu^\dagger U_\ell$  (QLC2)
- SU(5) GUT  $\Rightarrow U_{PMNS} = U_\ell^\dagger U_\nu$  (QLC1)  
 $\Rightarrow \theta_{12} + \theta_{12}^q / \sqrt{2} = 45^\circ$
- $A_4$  or  $S_3$  permutation symmetry  $\Rightarrow$   
 $U_\nu \equiv U_{tribimax} : \theta_{12} = \sin^{-1} \frac{1}{\sqrt{3}}, \theta_{23} = 45^\circ, \theta_{13} = 0^\circ$   
Tri-bimaximal mixing (TBM)

# Interconnections



# Radiative corrections to symmetry relations

- QLC and TBM give **distinct predictions for neutrino mixing angles**, but only at the high scale where the symmetry is unbroken
- **Renormalization group evolution** can change the predictions, making it impossible to distinguish between the symmetry scenarios, especially for **quasidegenerate scenarios**
- Symmetries can be preserved with proper choice of **Majorana phases**, e.g.  $m_1 \approx -m_2$
- Correlations between the evolutions of mixing angles help in distinguishing between high scale symmetries **in spite of large RG evolution**

Amol Dighe, Srubabati Goswami, *PR*: PRD 2006, PRD 2007

# In the words of Mark Antony

*Friends, physicists and TIFR-folk, lend me your ears;*

*I came to review his works, not to just praise him;*

*The good papers that men write live after them,*

*The not-so-good ones are interred in the arXiv's*

*So let it be...*

*It's said that he is loquacious*

*But he is (also) an honourable man.*

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