

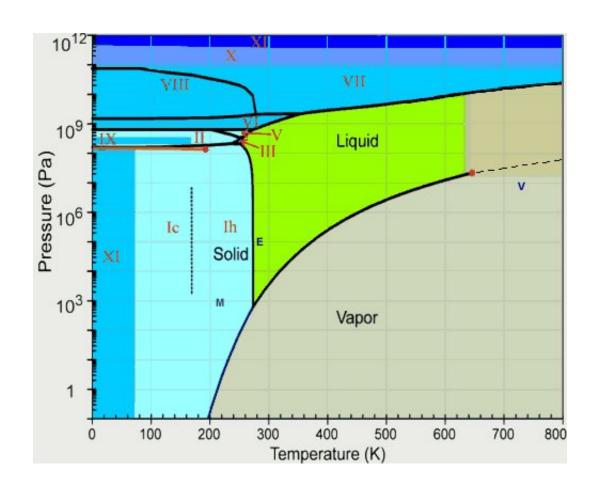
Rajiv V. Gavai T. I. F. R., Mumbai, India

Importance of Being Critical

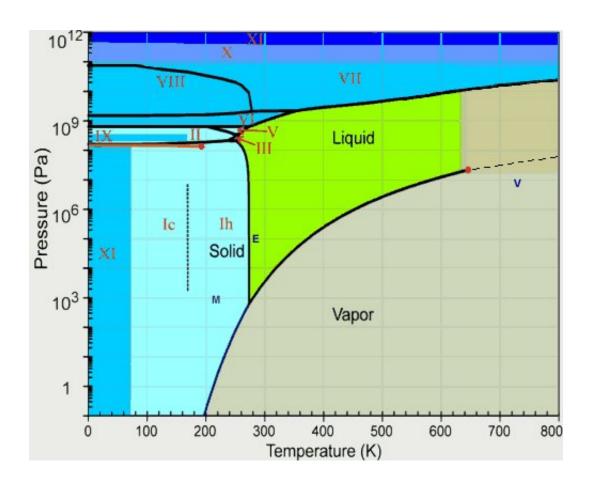
Lattice QCD Results

Searching Experimentally

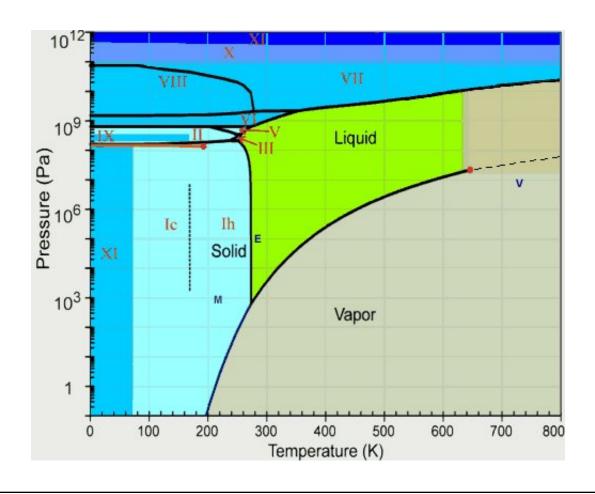
Summary



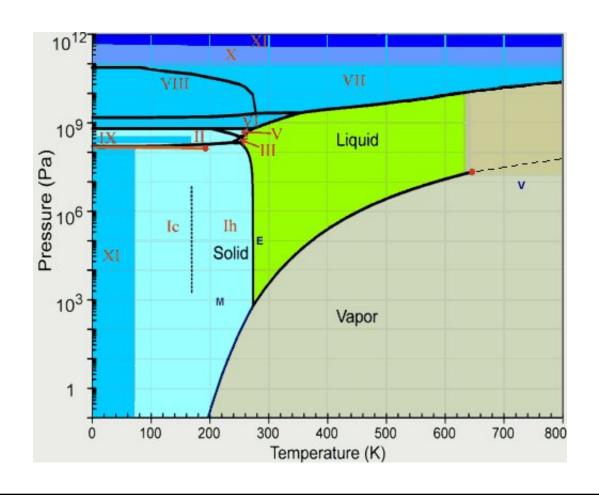
Phase Diagram of Water



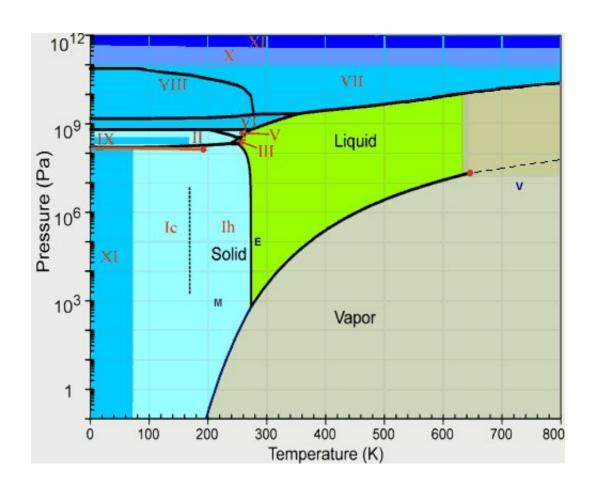
 One, possibly two, critical points



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- Extreme density fluctuations
 Opalescent turbidity

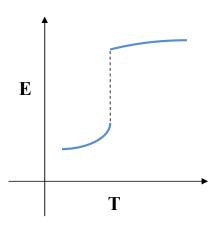


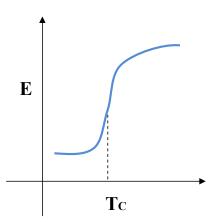
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- Dielectric constant
 & Viscosity \(\psi \).

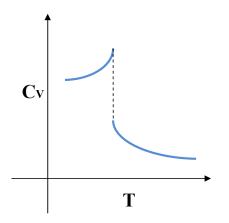


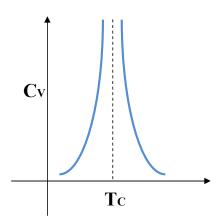
- One, possibly two, critical points
- Extreme density fluctuations
 Opalescent turbidity
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 & Viscosity \(\psi \).
- Many liquid fueled engines exploit such supercritical transitions.

SECOND ORDER



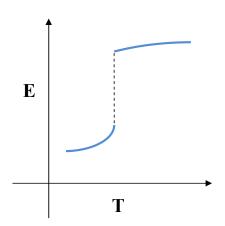


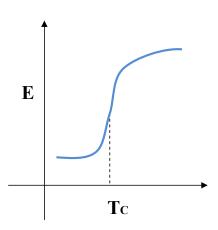




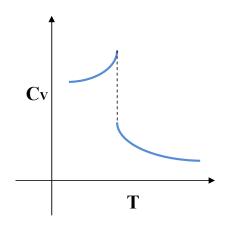
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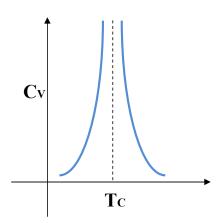
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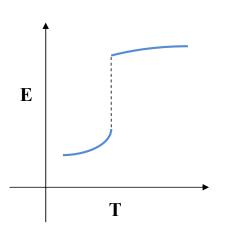


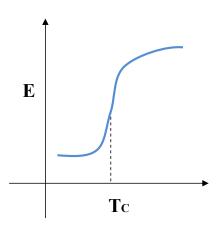
• Discontinuous ϵ - Nonzero Latent Heat- & finite C_v \rightarrow First order PT.



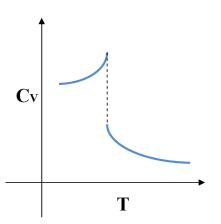


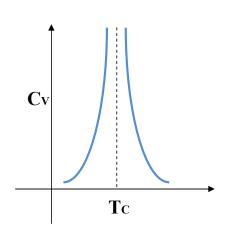
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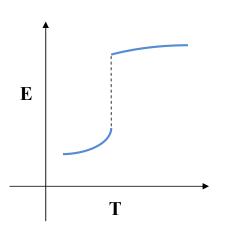
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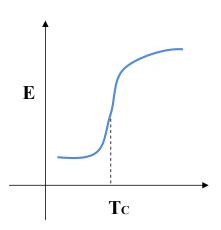




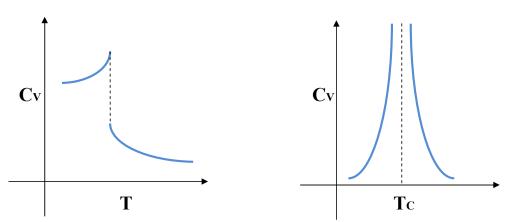
• In(Finite) Correleation Length at 2nd (1st) Order transition.

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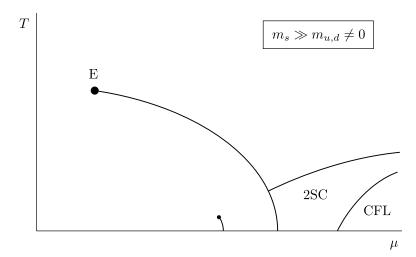


- In(Finite) Correleation Length at 2nd (1st) Order transition.
- "Cross-over" mere rapid change in ϵ , with maybe a sharp peaked C_v .

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Expected QCD Phase Diagram

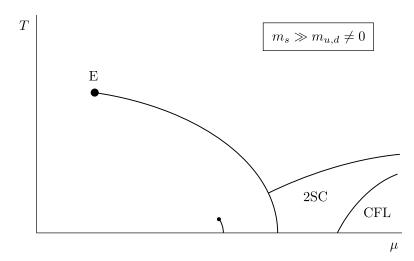


From Rajagopal-Wilczek Review

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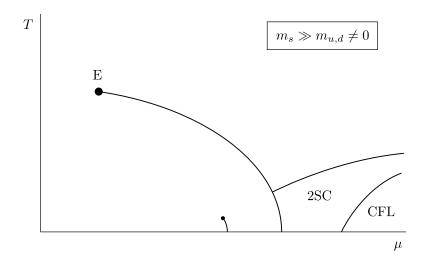


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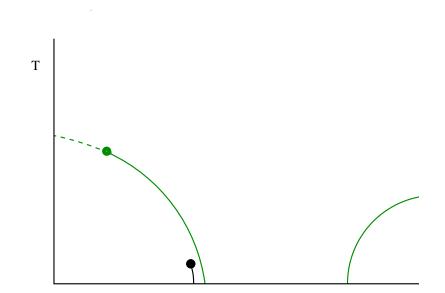
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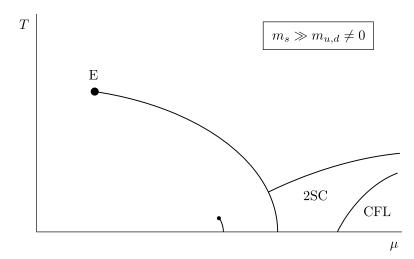
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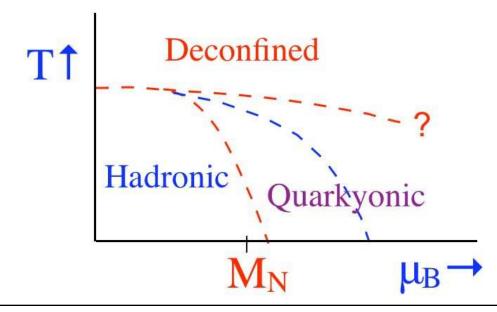
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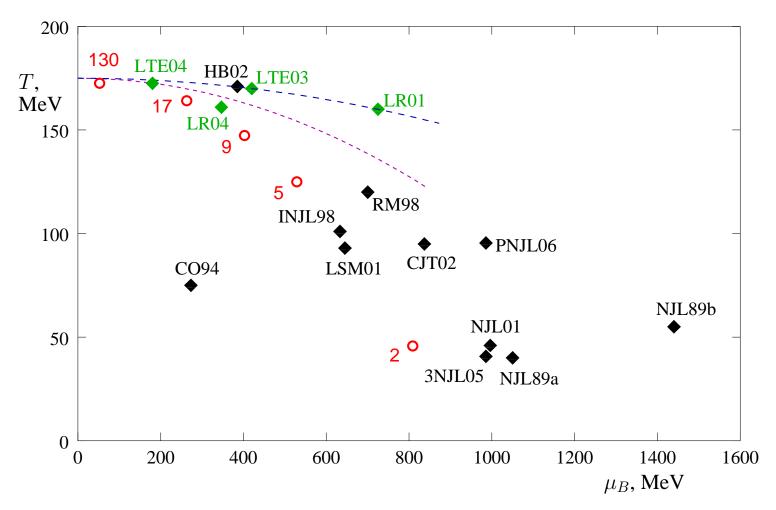
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From M. Stephanov, Lattice 2007 Plenary.

 QCD defined on a space time lattice – Best and Most Reliable way to extract non-perturbative physics.

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- Mostly staggered quarks used in these simulations. Broken flavour and spin symmetry on lattice $\Longrightarrow N_f=2$ simulations may be fine in $a\to 0$ limit but 3 or 2+1 problematic.
- Domain Wall or Overlap Fermions better. BUT Computationally expensive and introduction of μ unfortunately breaks chiral symmetry! (Banerjee, Gavai & Sharma PRD 2008; arXiv:0809.4535 & arXiv:0811.3026)

The $\mu \neq 0$ problem

Assuming N_f flavours of quarks, and denoting by μ_f the corresponding chemical potentials, the QCD partition function is

$$\mathcal{Z} = \int {\it D} U \exp(-S_G) \prod_f {
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and the thermal expectation value of an observable $\mathcal O$ is

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However, det M is a complex number for any $\mu \neq 0$: The Phase/sign problem

Several Approaches proposed in the past two decades : None as satisfactory as the usual $T \neq 0$ simulations. Still scope for a good/great idea !

• Two parameter Re-weighting (z. Fodor & S. Katz, JHEP 0203 (2002) 014).

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- Canonical Ensemble (K. -F. Liu, IJMP B16 (2002) 2017, S. Kratochvila and P. de Forcrand, Pos LAT2005 (2006) 167.)
- Complex Langevin (G. Aarts and I. O. Stamatescu, arXiv:0809.5227 and its references for earlier work).

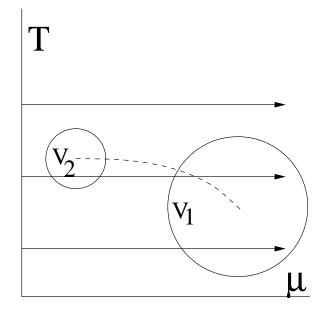
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We study volume dependence at several T to i) bracket the critical region and then to ii) track its change as a function of volume.

How Do We Do This Expansion?

Canonical definitions yield various number densities and susceptibilities :

$$n_i = \frac{T}{V} \frac{\partial \ln \mathcal{Z}}{\partial \mu_i}$$
 and $\chi_{ij} = \frac{T}{V} \frac{\partial^2 \ln \mathcal{Z}}{\partial \mu_i \partial \mu_j}$.

These are also useful by themselves both theoretically and for Heavy Ion Physics (Flavour correlations, $\lambda_s \dots$)

Denoting higher order susceptibilities by χ_{n_u,n_d} , the pressure P has the expansion in μ :

$$\frac{\Delta P}{T^4} \equiv \frac{P(\mu, T)}{T^4} - \frac{P(0, T)}{T^4} = \sum_{n_u, n_d} \chi_{n_u, n_d} \frac{1}{n_u!} \left(\frac{\mu_u}{T}\right)^{n_u} \frac{1}{n_d!} \left(\frac{\mu_d}{T}\right)^{n_d} \tag{1}$$

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- From this expansion, a series for baryonic susceptibility can be constructed. Its radius of convergence gives the nearest critical point.
- Successive estimates for the radius of convergence can be obtained from these using $\sqrt{\frac{n(n+1)\chi_B^{(n+1)}}{\chi_B^{(n+3)}}}$ or $\left(n!\frac{\chi_B^{(2)}}{\chi_B^{(n+2)}}\right)^{1/n}$. We use both and terms up to 8th order in μ .
- All coefficients of the series must be POSITIVE for the critical point to be at real μ , and thus physical.
- Coefficients for the off-diagonal susceptibility, χ_{11} , can be constructed similarly.
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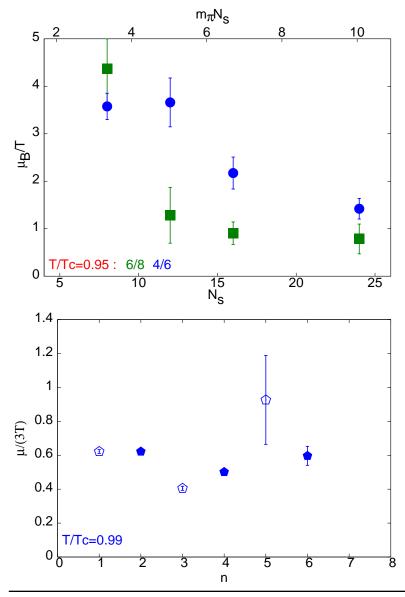
CRAY X1 of I L G T I, T I F R, Mumbai

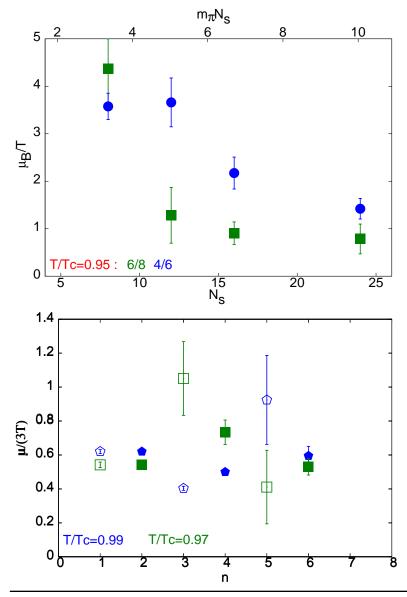
Our Simulations & Results

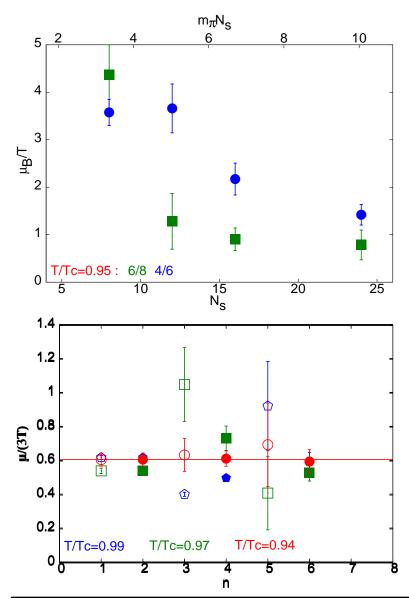
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- Earlier Lattice : $4 \times N_s^3$, $N_s = 8$, 10, 12, 16, 24 (Gavai-Gupta, PRD 2005)
- Lattice used : $6 \times N_s^3$, $N_s = 12$, 18, 24 (Gavai-Gupta, arXiv:0806.2233, PRD in press). Needed to determine β_c . Our result $(\beta_c = 5.425(5))$ well bracketed by MILC for $m/T_c = 0.075$ and 0.15.

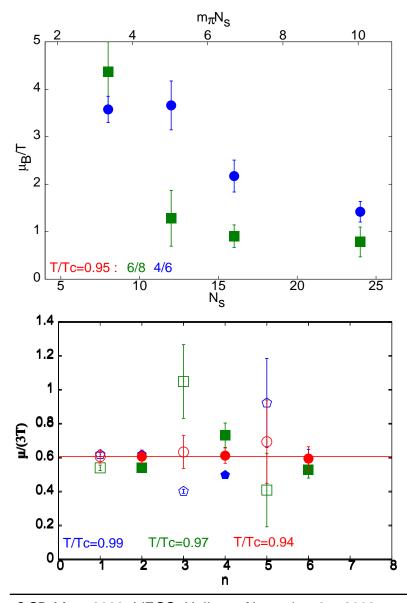
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- New Simulations made at $T/T_c = 0.89(1)$, 0.92(1), 0.94(1), 0.97(1), 0.99(1) 1.00(1), 1.21(1), 1.33(1), 1.48(3) and 1.92(5)
- Typical stat. 50-200 in max autocorrelation units.

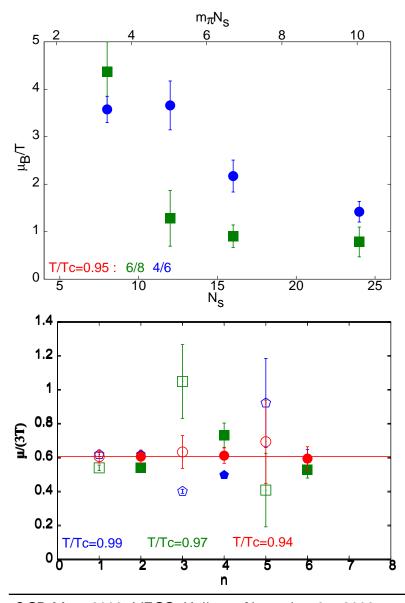




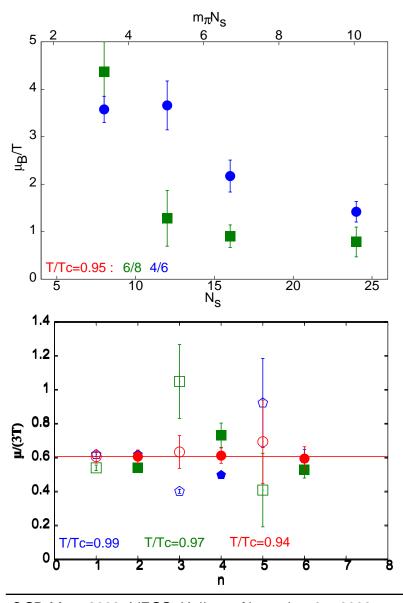




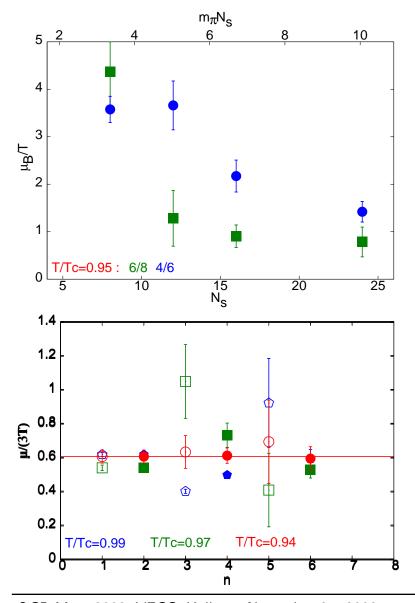
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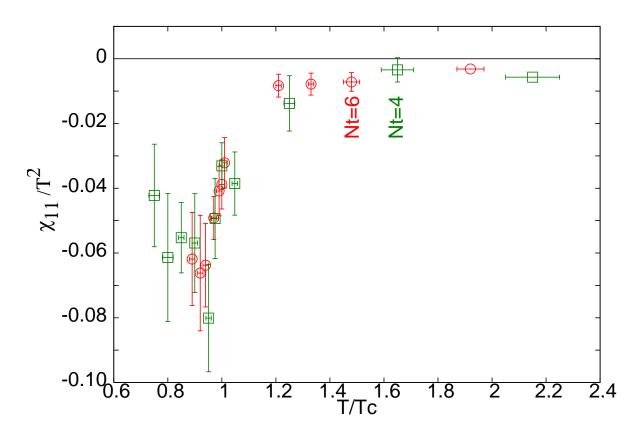
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- $\frac{T^E}{T_c} = 0.94 \pm 0.01$, and $\frac{\mu_B^E}{T^E} = 1.8 \pm 0.1$ for finer lattice: Our earlier coarser lattice result was $\mu_B^E/T^E = 1.3 \pm 0.3$. Infinite volume result: \downarrow to 1.1(1)



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- Critical point shifted to smaller $\mu_B/T \sim 1-2.$

More Details

Measure of the seriousness of sign problem : χ_{11} ; $N_t=4$ & 6 agree.

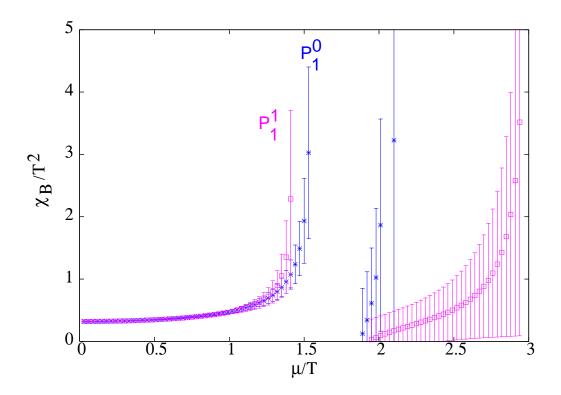


Cross Check on μ^E/T^E

♠ Use Padé approximants for the series to estimate the radius of convergence.

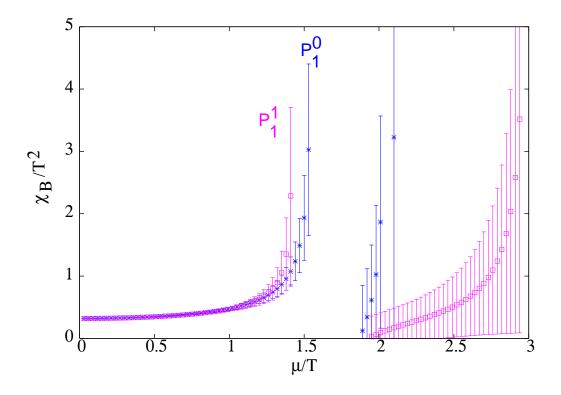
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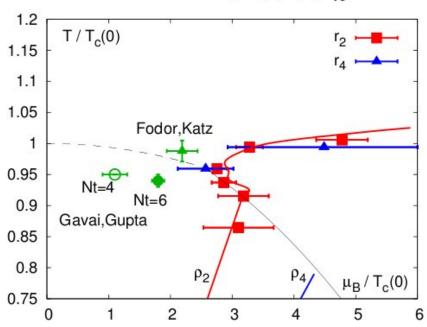
○ Consistent Window with our other estimates.

Estimating $T_c(\mu_c)$ and μ_c/T

Status of the RBC-BI project

- $m ext{ iny }$ calculations for $N_ au=4$ and $6;\,N_\sigma=4N_ au$
- uses an $\mathcal{O}(a^2)$ improved staggered action (p4fat3)
- ullet estimator for μ_c :

$$\left(rac{\mu_c(T)}{T_c(0)}
ight)_n \equiv
ho_n = rac{T}{T_c(0)} \sqrt{rac{c_n}{c_{n+2}}}$$

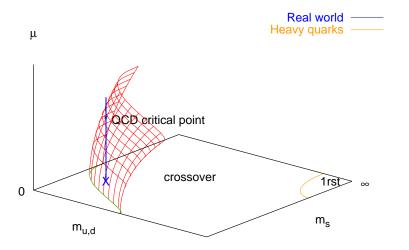


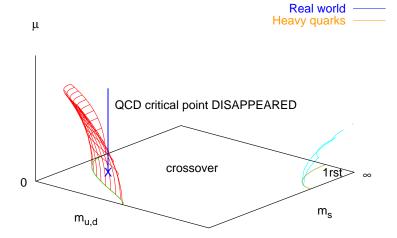
- slight quark mass dependence
- weak cut-off dependence
 - $\mathcal{O}(\mu^6)$ requires more statistics

INT. Seattle 2008. F. Karsch - p. 20/3

Imaginary Chemical Potential

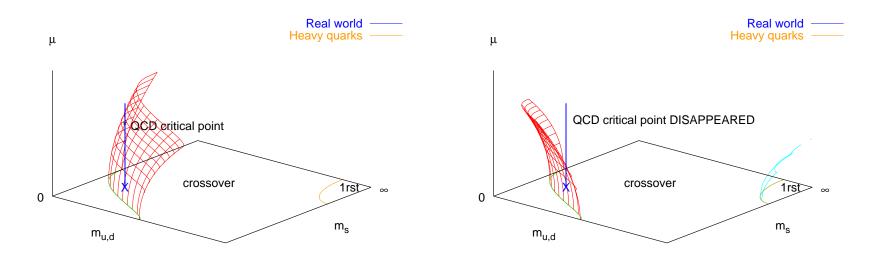
deForcrand-Philpsen JHEP 0811





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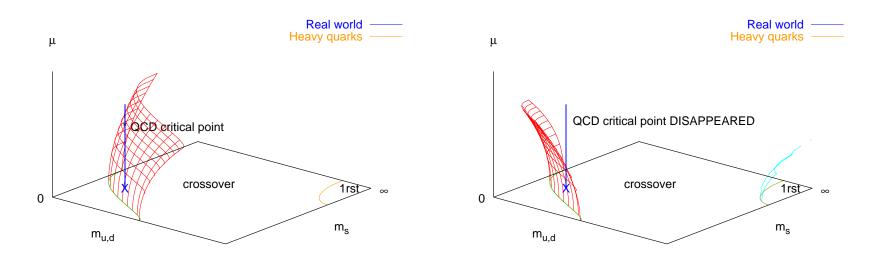
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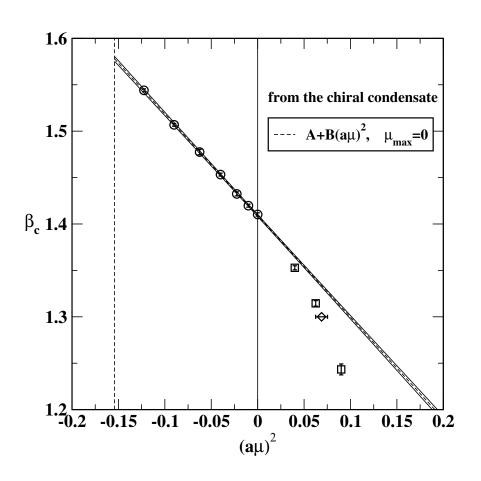
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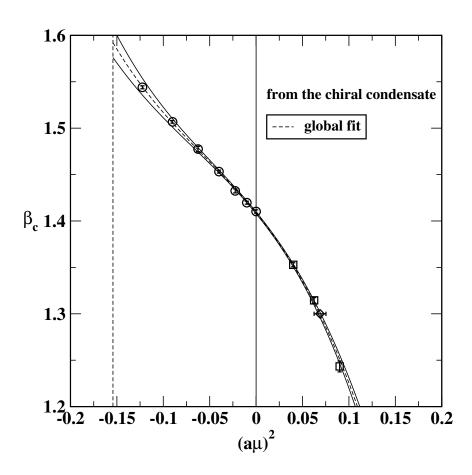


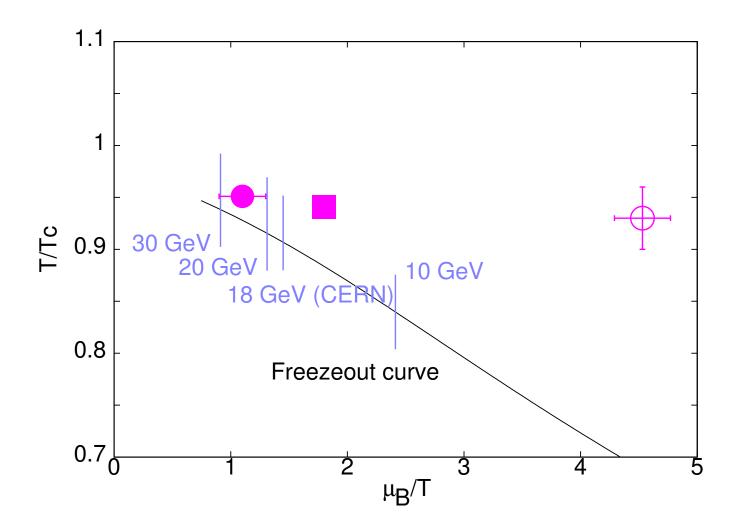
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Problems : i) $N_f = 3 \rightarrow$ Anomaly and Staggered quarks ? ii) Known examples where shapes are different in real/imaginary μ ,

"The Critical line from imaginary to real baryonic chemical potentials in two-color QCD", P. Cea, L. Cosmai, M. D'Elia, A. Papa, PR D77, 2008





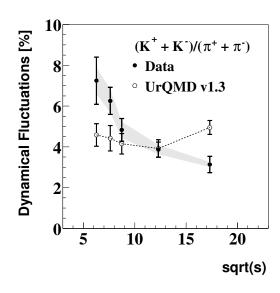


Searching Experimentally

- Exploit the facts i) susceptibilities diverge near the critical point and ii) decreasing \sqrt{s} increases μ_B (Rajagopal, Shuryak & Stephanov PRD 1999)
- Look for nonmontonic dependence of the event-by-event fluctuations with colliding energy.

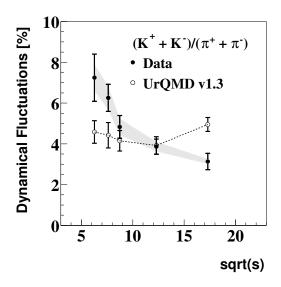
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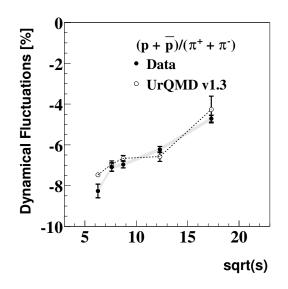
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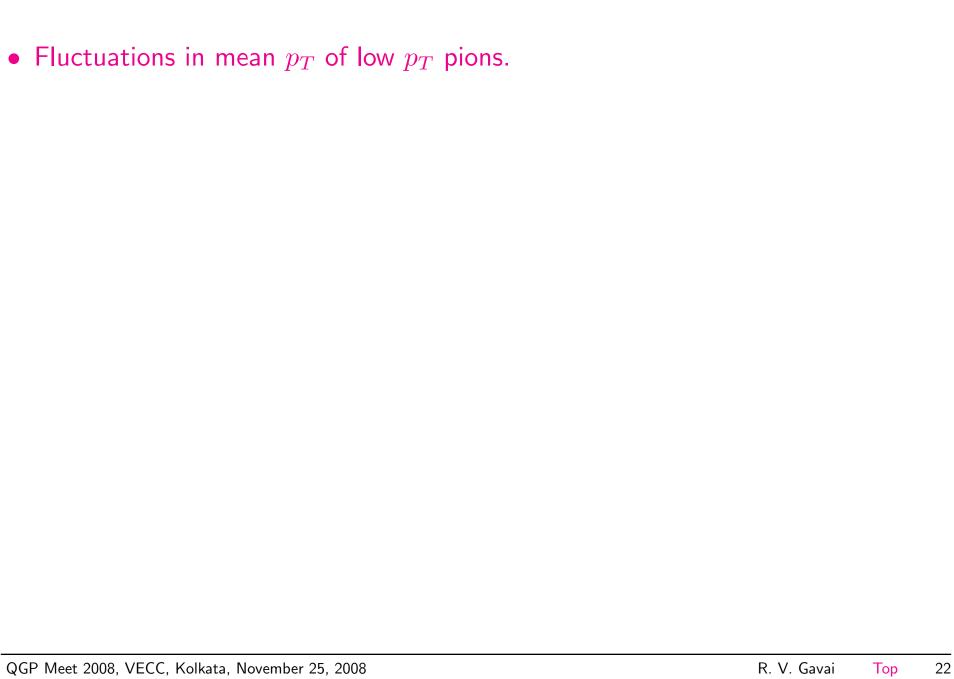


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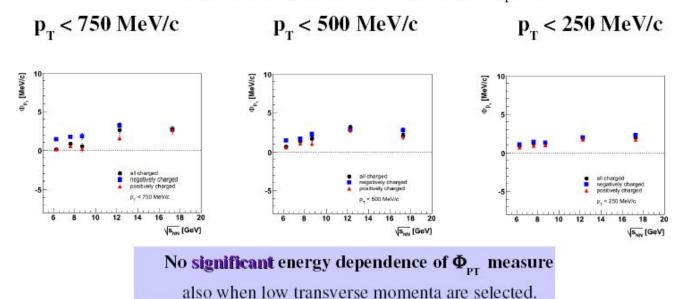




ullet Fluctuations in mean p_T of low p_T pions. (K. Grebieszkow, CPOD workshop 2007, GSI, Darmstadt)

Fluctuations due to the critical point should be dominated by fluctuations of pions with $p_r \le 500$ MeV/c

M. Stephanov, K. Rajagopal, E. V. Shuryak (Phys. Rev. **D60**, 114028, 1999): suggestion to do analysis with several upper $p_{_{\rm T}}$ cuts

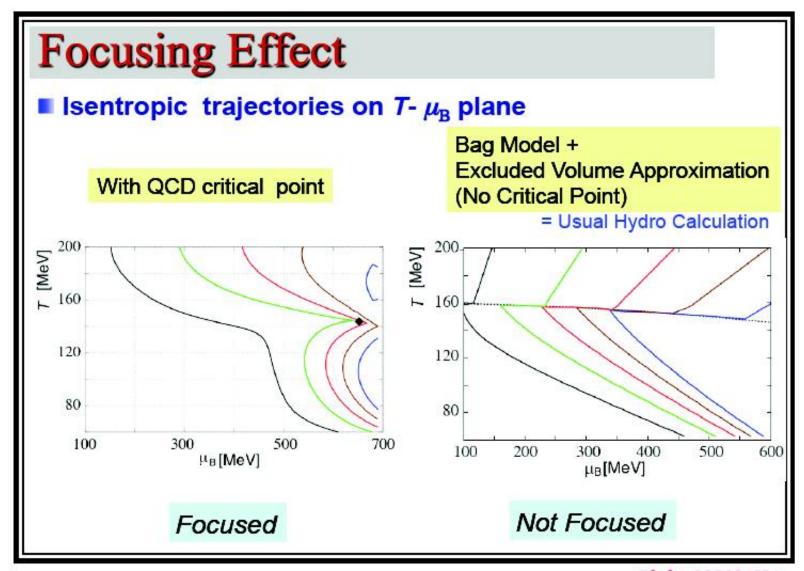


Remark: predicted fluctuations at the critical point should result in $\Phi_{PT} \cong 20$ MeV/c, the effect of limited acceptance of NA49 reduces them to $\Phi_{PT} \cong 10$ MeV/c

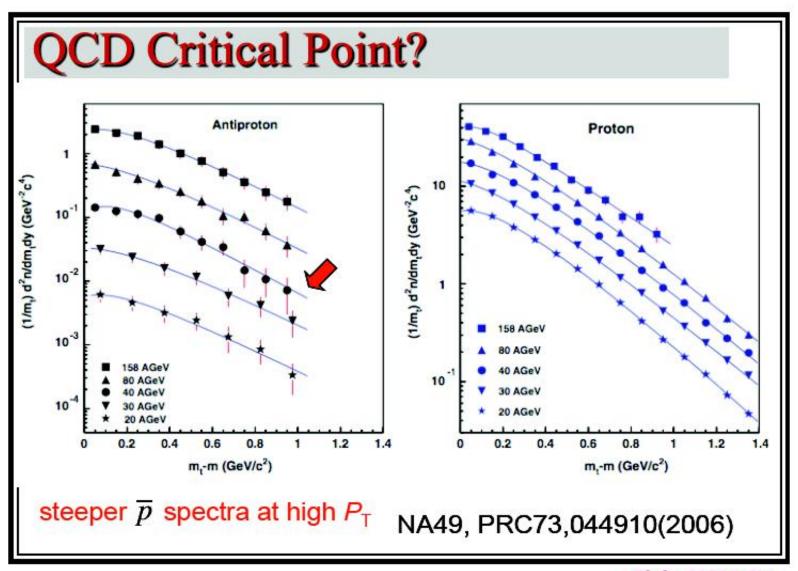
- Proton number fluctuations (Hatta-Stephenov, PRL 2003)
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- Assuming protons, neutrons, pions to dominate, both χ_Q and χ_B can be shown to be proton number fluctuations only.
- Isentropic trajectories focus at the critical point (Asakawa-Nonaka, PRC 2005).
- This leads to the emission of high p_T particles at earlier times. (Asakawa-Bass-Nonaka-Müller, INT 2008 workshop).
- Note this is NOT a fluctuations signal but model (EoS) dependent?



Chiho NONAKA



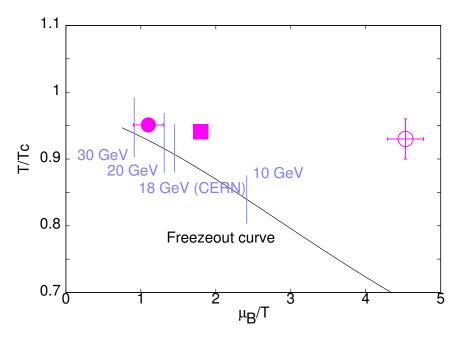
Chiho NONAKA

• Phase diagram in $T-\mu$ on $N_t=4$ has begun to emerge: Different methods, \leadsto similar qualitative picture.

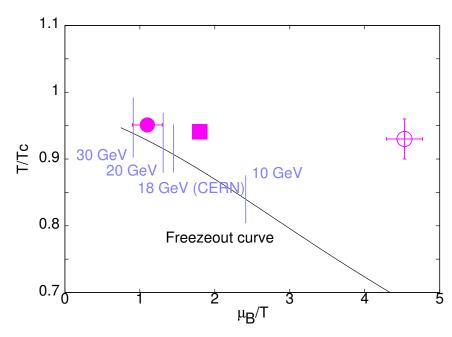
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So far no signs of a critical point in the experimental results at CERN. Will RHIC deliver it for us?