

# New Phases of Strongly Interacting Matter

*Rajiv V. Gavai*  
*T. I. F. R., Mumbai, India*

# New Phases of Strongly Interacting Matter

*Rajiv V. Gavai*  
*T. I. F. R., Mumbai, India*

Introduction : What and Why

QCD Phase Diagram

Heavy Ion Collisions

$J/\psi$  Suppression

Speed of Sound

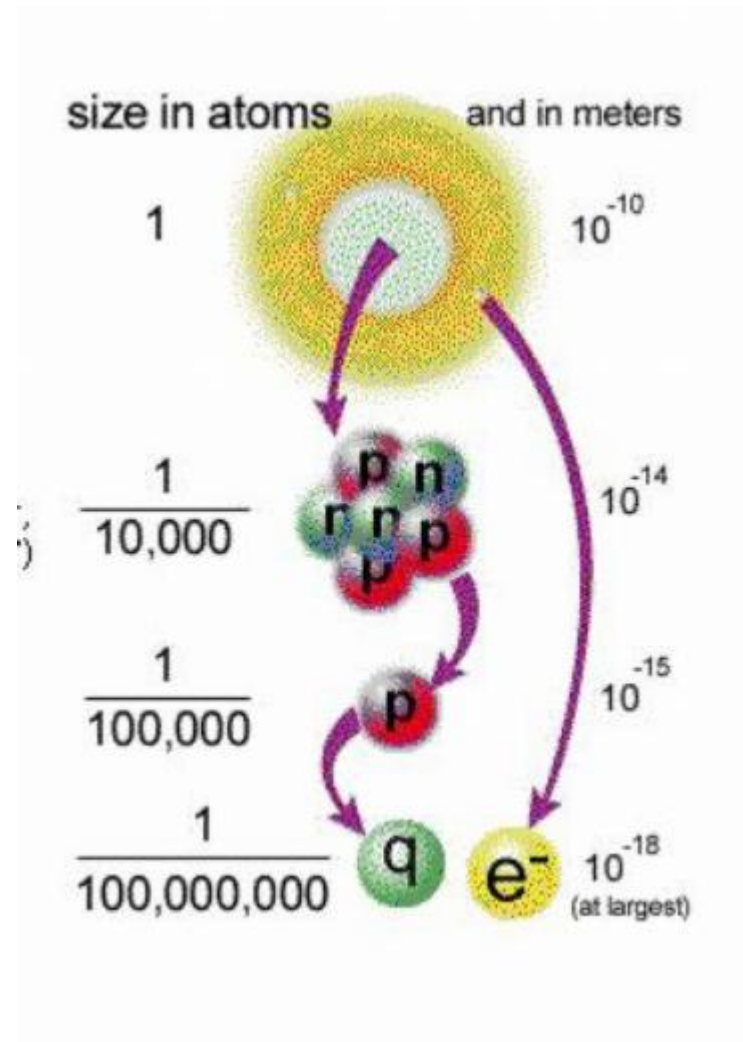
Summary

# Introduction

- Known Interactions and Particles a century ago: Electromagnetism, Gravity and Electrons, Atoms.

- Known Interactions and Particles a century ago: Electromagnetism, Gravity and Electrons, Atoms.
- Rutherford's Scattering Experiment  
→ various layers that have since been discovered.

- Known Interactions and Particles a century ago: Electromagnetism, Gravity and Electrons, Atoms.
- Rutherford's Scattering Experiment → various layers that have since been discovered.
- Quarks and Leptons – Basic building blocks : Proton ( $uud$ ), Neutron ( $udd$ ), Pion ( $u\bar{d}$ )....
- A Variety of Vector Bosons : Carriers of forces.





	Gravity	Weak (Electroweak)	Electromagnetic	Strong
Carried By	Graviton (not yet observed)	$W^+ W^- Z^0$	Photon	Gluon
Acts on	All	Quarks and Leptons	Quarks and Charged Leptons and $W^+ W^-$	Quarks and Gluons

Strengths in a ratio  $10^{-39} : 10^{-5} : 10^{-2} : 1$



	Gravity	Weak (Electroweak)	Electromagnetic	Strong
Carried By	Graviton (not yet observed)	$W^+ W^- Z^0$	Photon	Gluon
Acts on	All	Quarks and Leptons	Quarks and Charged Leptons and $W^+ W^-$	Quarks and Gluons

Strengths in a ratio  $10^{-39} : 10^{-5} : 10^{-2} : 1$

Red	Green	Blue	Quarks	Color
Anti-Red	Anti-Green	Anti-Blue	Anti-Quarks	Anti-Color



(Anti-)Quarks come in three (anti-)colours, making gluons also coloured.



# Quantum Chromo Dynamics (QCD)

- (Gauge) Theory of interactions of quarks-gluons.
- Similar to structure in theory of electrons & photons (QED).

# Quantum Chromo Dynamics (QCD)

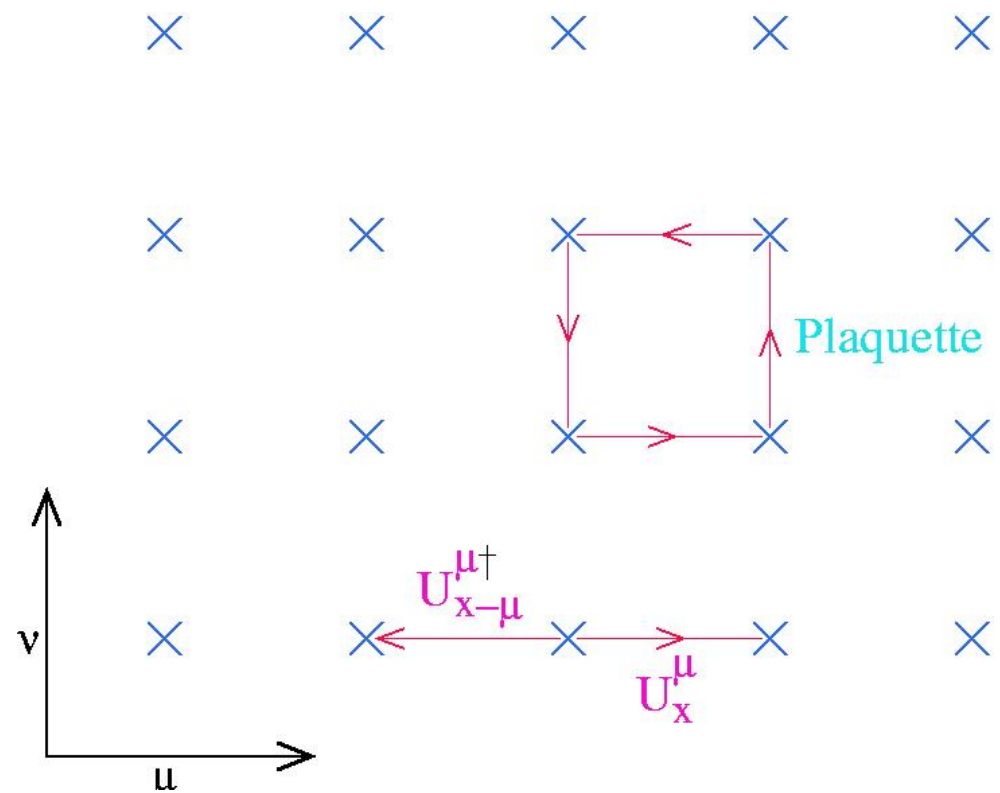
- (Gauge) Theory of interactions of quarks-gluons.
- Similar to structure in theory of electrons & photons (QED).
- Many more “photons” (Eight) which carry colour charge & hence interact amongst themselves.
- *Unlike QED*, the coupling is usually very large.

# Quantum Chromo Dynamics (QCD)

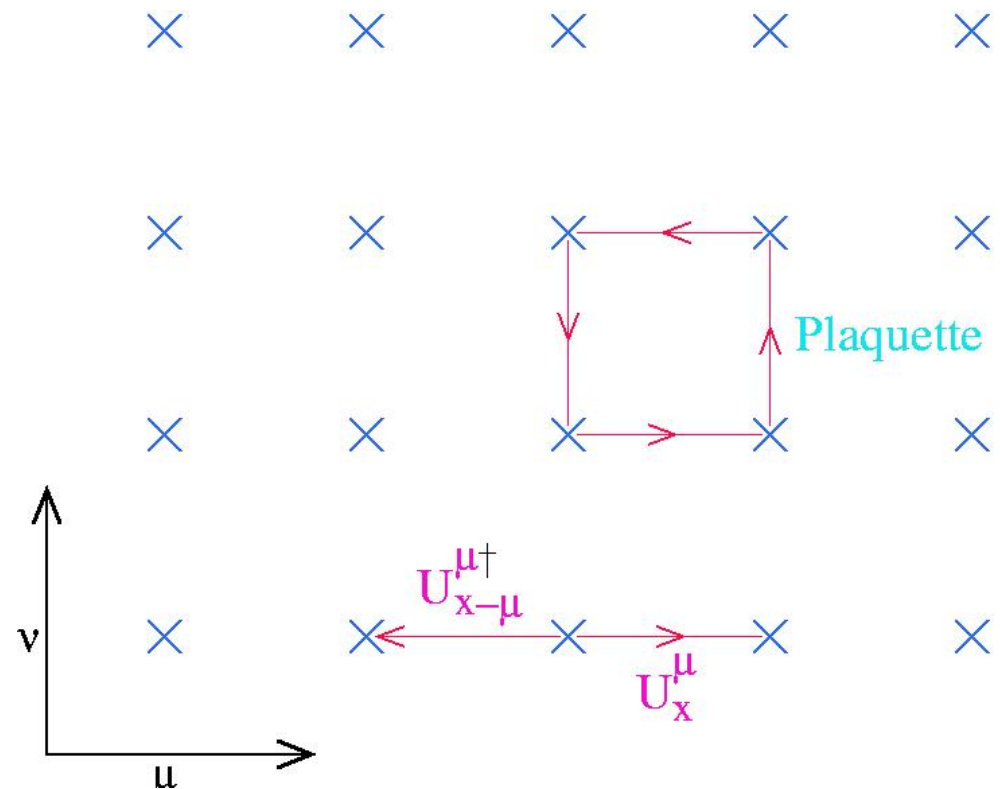
- (Gauge) Theory of interactions of quarks-gluons.
- Similar to structure in theory of electrons & photons (QED).
- Many more “photons” (Eight) which carry colour charge & hence interact amongst themselves.
- *Unlike QED*, the coupling is usually very large.
- Much richer structure : Quark Confinement, Dynamical Symmetry Breaking..
- Very high interaction (binding) energies. E.g.,  $M_{Proton} \gg (2m_u + m_d)$ , by a factor of 100  $\rightarrow$  Understanding it is knowing where the Visible mass of Universe comes from.

# Basic Lattice Gauge Theory

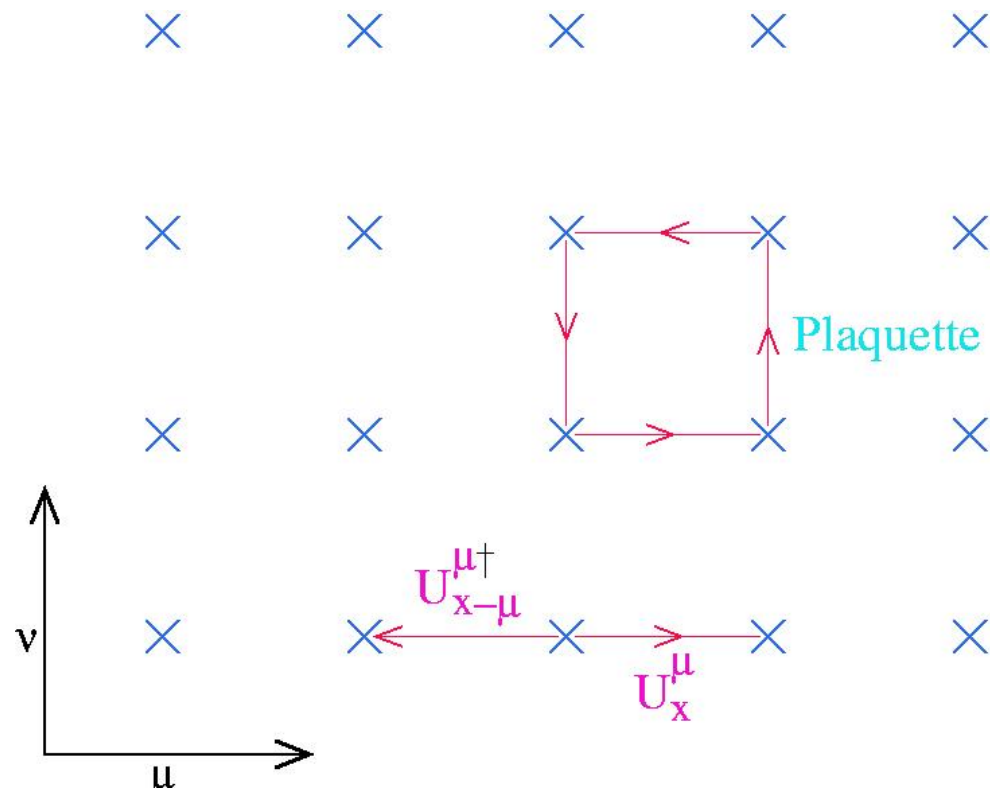
- Discrete space-time : Lattice spacing  $a$  UV Cut-off.



- Discrete space-time : Lattice spacing  $a$  UV Cut-off.
- Quark fields  $\psi(x)$ ,  $\bar{\psi}(x)$  on lattice sites.
- Gluon Fields on links :  $U_\mu(x)$



- Discrete space-time : Lattice spacing  $a$  UV Cut-off.
- Quark fields  $\psi(x)$ ,  $\bar{\psi}(x)$  on lattice sites.
- Gluon Fields on links :  $U_\mu(x)$
- Gauge transform  $V_x \in SU(3)$   
 $\Rightarrow \psi'(x) = V_x \psi(x)$ ,  
 $U'_\mu(x) = V_x U_\mu(x) V_{x+\hat{\mu}}^{-1}$ .
- Gauge invariance : Actions from Closed Wilson loops, e.g., plaquette.



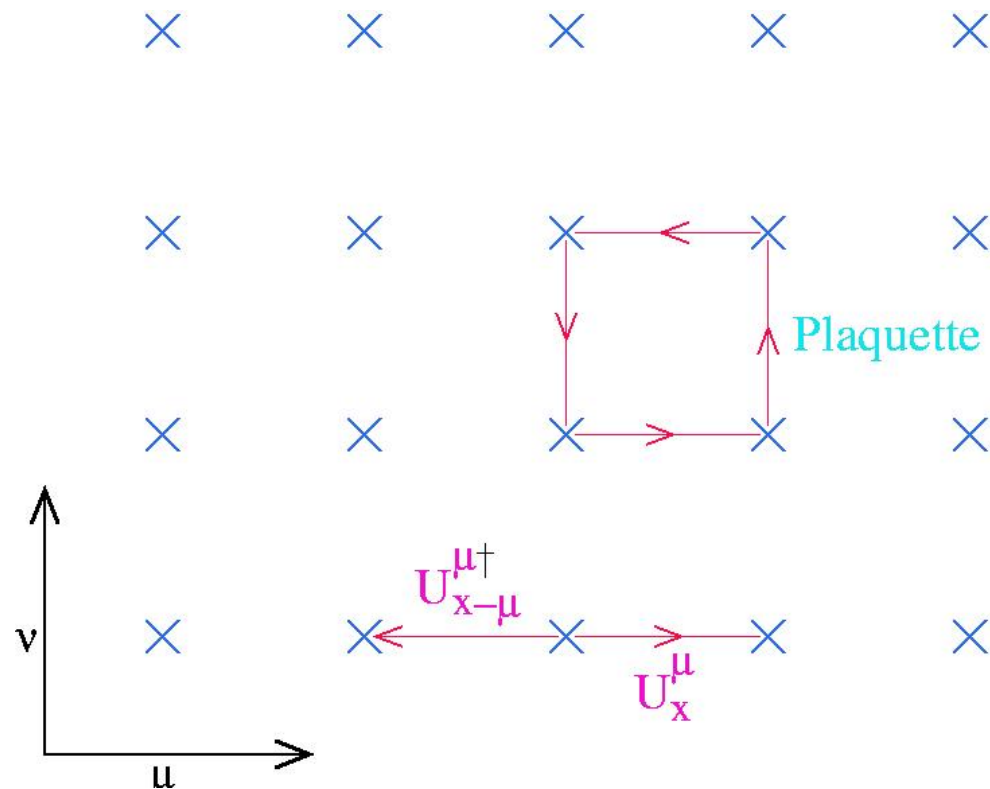
- Discrete space-time : Lattice spacing  $a$  UV Cut-off.

- Quark fields  $\psi(x)$ ,  $\bar{\psi}(x)$  on lattice sites.

- Gluon Fields on links :  $U_\mu(x)$

- Gauge transform  $V_x \in SU(3)$   
 $\Rightarrow \psi'(x) = V_x \psi(x)$ ,  
 $U'_\mu(x) = V_x U_\mu(x) V_{x+\hat{\mu}}^{-1}$ .

- Gauge invariance : Actions from Closed Wilson loops, e.g., plaquette.



- Fermion Actions : Staggered, Wilson, Overlap..



Typically, we need to evaluate

$$\langle \Theta(m_v) \rangle = \frac{\int DU \exp(-S_G) \Theta(m_v) \text{Det } M(m_s)}{\int DU \exp(-S_G) \text{Det } M(m_s)} , \quad (1)$$

where  $M$  is the Dirac matrix in  $x$ , colour, spin, flavour space for fermions of mass  $m_s$ ,  $S_G$  is the gluonic action, and the observable  $\Theta$  may contain fermion propagators of mass  $m_v$ .

Typically, we need to evaluate

$$\langle \Theta(m_v) \rangle = \frac{\int DU \exp(-S_G) \Theta(m_v) \text{Det } M(m_s)}{\int DU \exp(-S_G) \text{Det } M(m_s)}, \quad (1)$$

where  $M$  is the Dirac matrix in  $x$ , colour, spin, flavour space for fermions of mass  $m_s$ ,  $S_G$  is the gluonic action, and the observable  $\Theta$  may contain fermion propagators of mass  $m_v$ .

Lattice scaffolding must be removed : Continuum limit  $a \rightarrow 0$ .

$\rightsquigarrow$  Computer Simulations,  $\langle \Theta \rangle$  is computed by averaging over a set of configurations  $\{U_\mu(x)\}$  which occur with probability  $\propto \exp(-S_G) \cdot \text{Det } M$ .

Typically, we need to evaluate

$$\langle \Theta(m_v) \rangle = \frac{\int DU \exp(-S_G) \Theta(m_v) \text{Det } M(m_s)}{\int DU \exp(-S_G) \text{Det } M(m_s)}, \quad (1)$$

where  $M$  is the Dirac matrix in  $x$ , colour, spin, flavour space for fermions of mass  $m_s$ ,  $S_G$  is the gluonic action, and the observable  $\Theta$  may contain fermion propagators of mass  $m_v$ .

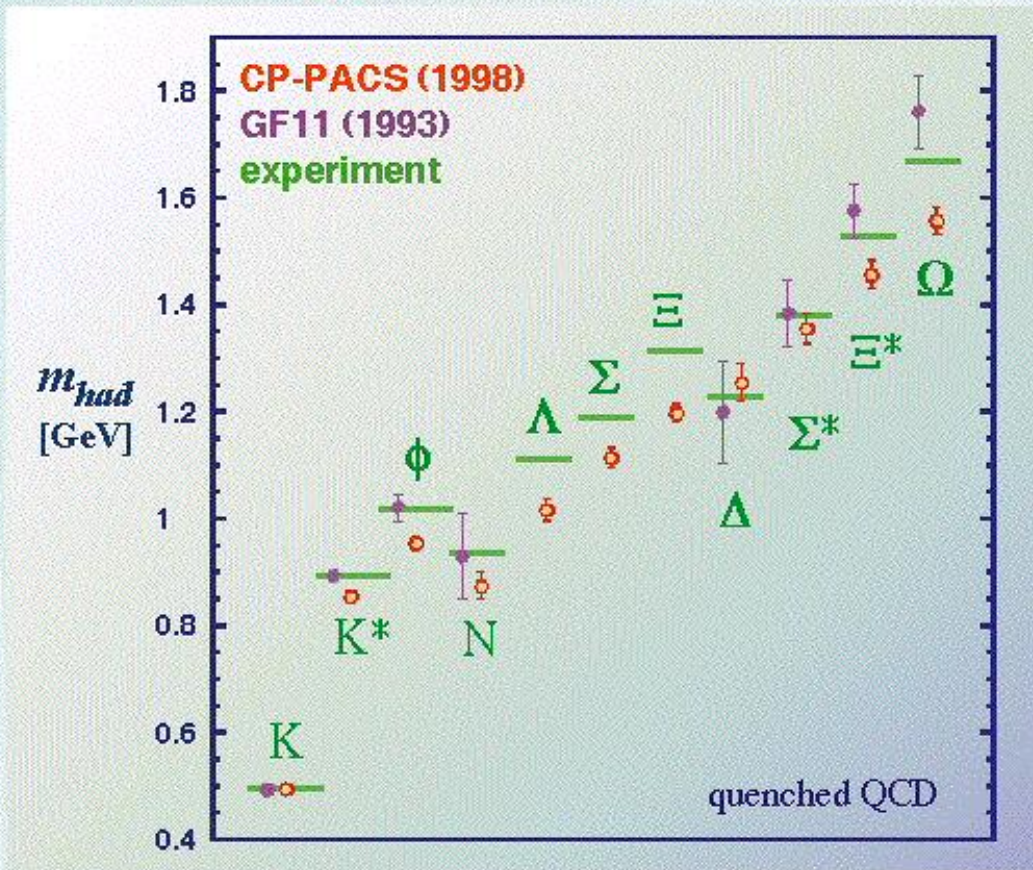
Lattice scaffolding must be removed : Continuum limit  $a \rightarrow 0$ .

$\rightsquigarrow$  Computer Simulations,  $\langle \Theta \rangle$  is computed by averaging over a set of configurations  $\{U_\mu(x)\}$  which occur with probability  $\propto \exp(-S_G) \cdot \text{Det } M$ .

Complexity of evaluation of  $\text{Det } M \implies$  approximations : Quenched (  $m_s = \infty$  limit) and Full ( low  $m_s = m_u = m_d$  ).

Q  $\rightarrow$  Full  $\rightsquigarrow$  Computer time  $\uparrow$  and Precision  $\downarrow$ .

# Hadron Mass Spectrum from Quarks and Gluons

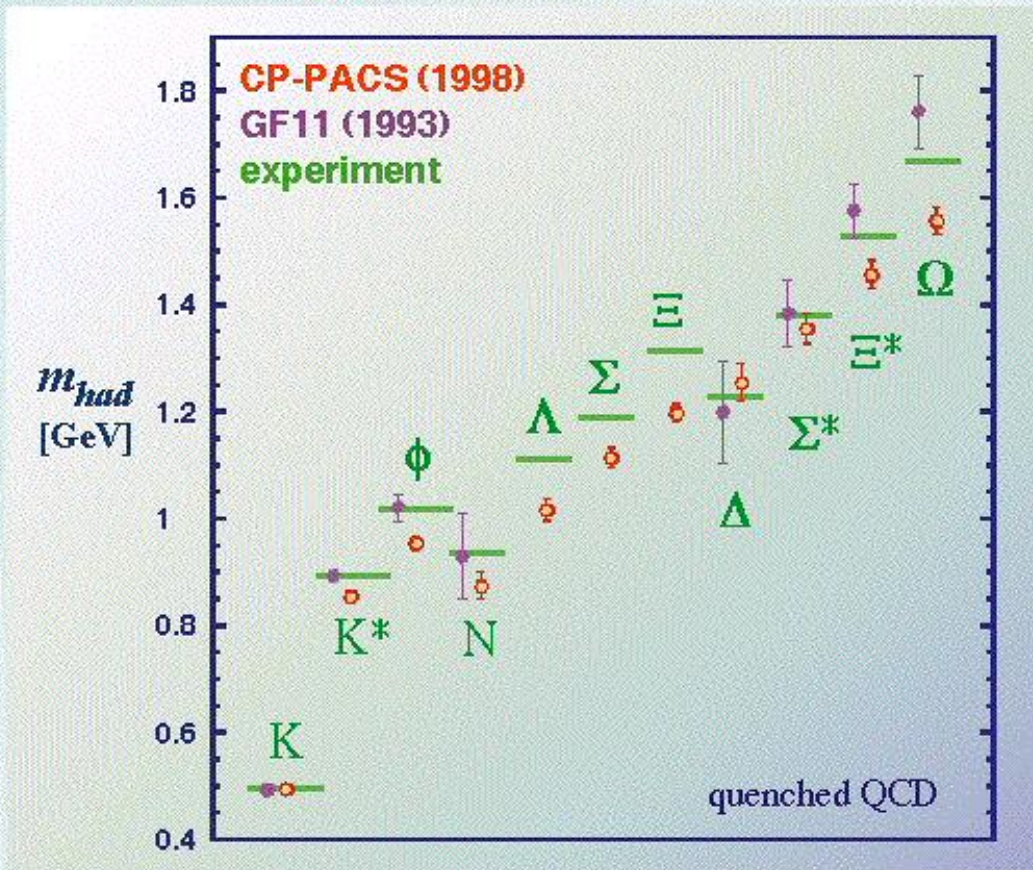


♡ Baryon mass comes out (almost) right.

(From CP-PACS Collaboration, Japan)



# Hadron Mass Spectrum from Quarks and Gluons



♡ Baryon mass comes out (almost) right.

(From CP-PACS Collaboration, Japan)

♡ Massless quarks acquire mass dynamically : Vacuum breaks Chiral Symmetry, i.e,  $\langle \bar{\psi}\psi \rangle \neq 0$ .

♡ Goldstone nature of Pion established:

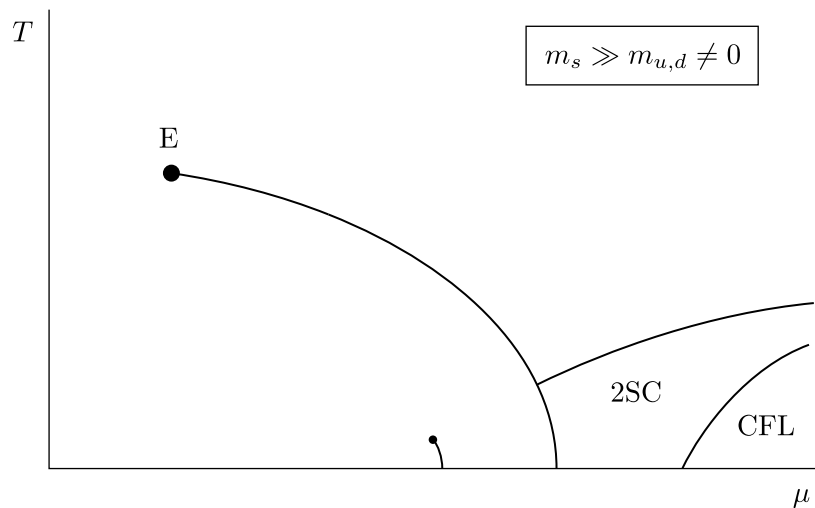
$$m_{\pi}^2 \propto m_q.$$

# QCD Phase Diagram

QCD defined on a space time lattice – Best and Most Reliable way to extract **Predictions** for non-perturbative physics.

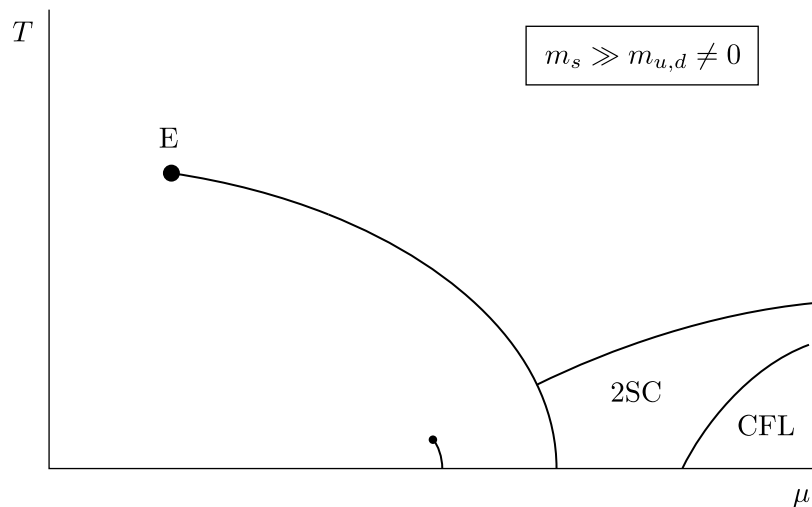
# QCD Phase Diagram

QCD defined on a space time lattice – Best and Most Reliable way to extract **Predictions** for non-perturbative physics.



# QCD Phase Diagram

QCD defined on a space time lattice – Best and Most Reliable way to extract **Predictions** for non-perturbative physics.

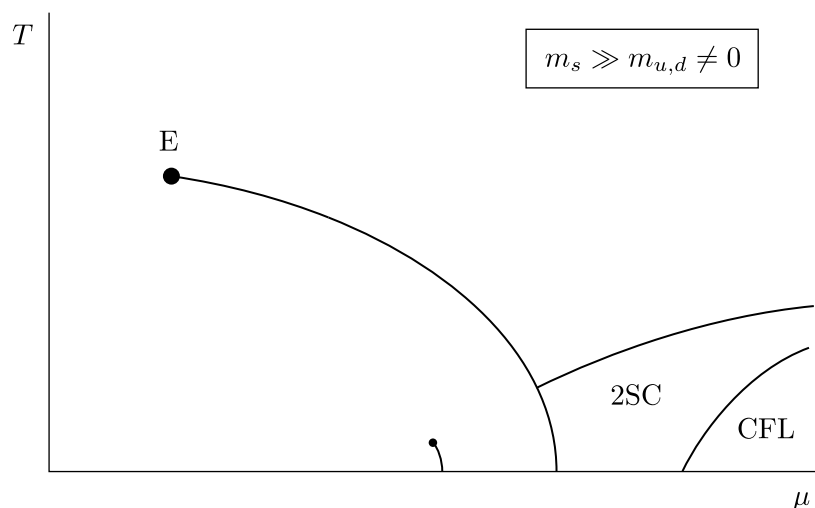


- New States at High Temperatures/Density expected on basis of models.



# QCD Phase Diagram

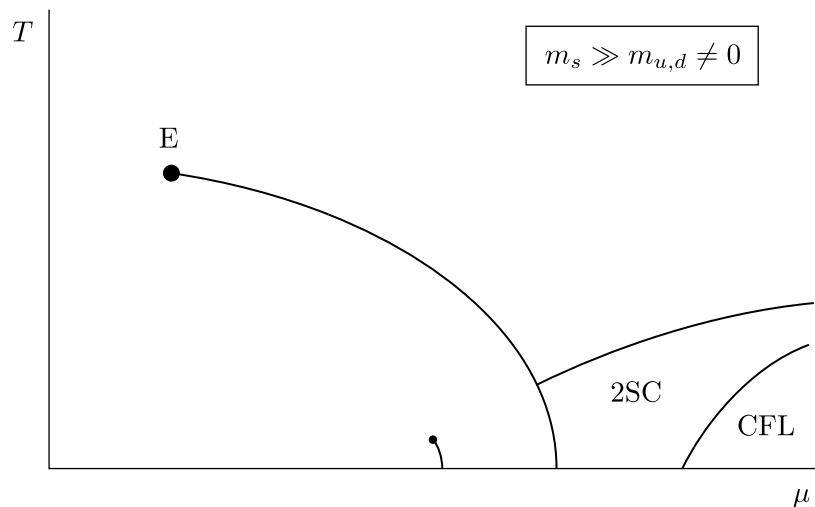
QCD defined on a space time lattice – Best and Most Reliable way to extract **Predictions** for non-perturbative physics.



- New States at High Temperatures/Density expected on basis of models.
- Lattice ideal tool to establish the phase diagram and properties of the phases.

# QCD Phase Diagram

QCD defined on a space time lattice – Best and Most Reliable way to extract **Predictions** for non-perturbative physics.



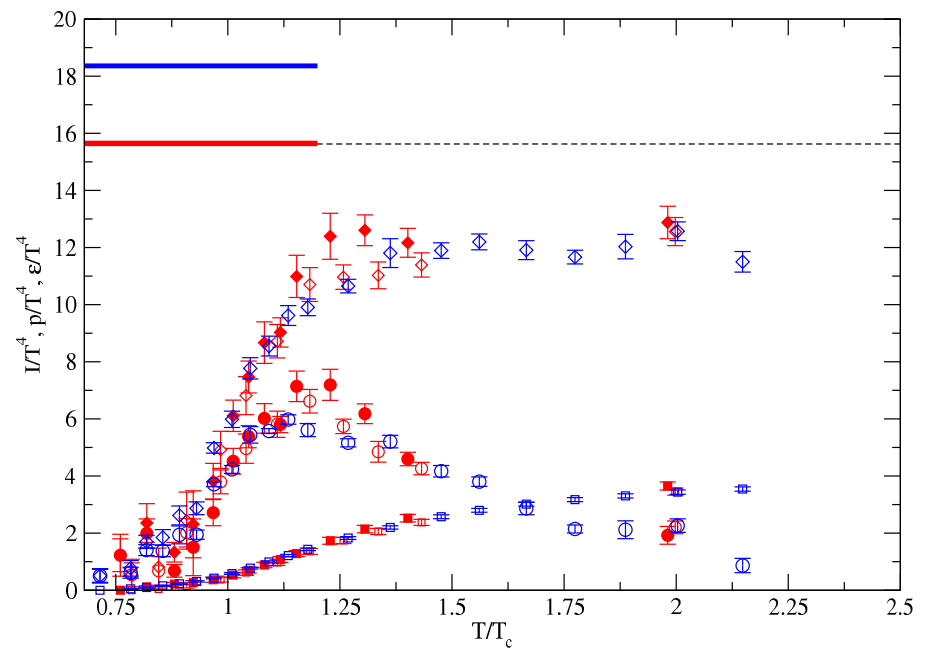
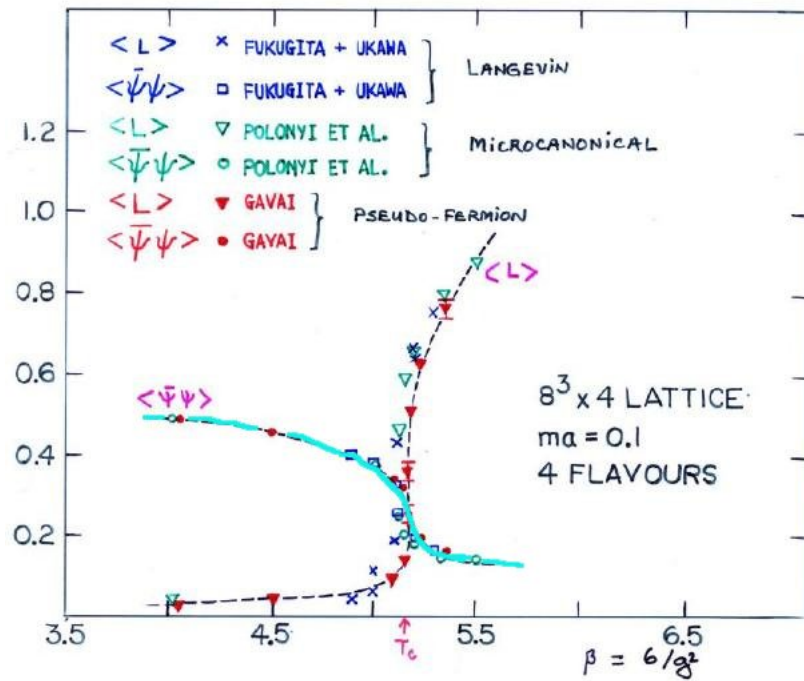
- New States at High Temperatures/Density expected on basis of models.
- Lattice ideal tool to establish the phase diagram and properties of the phases.
- Quark-Gluon Plasma, such a new phase, expected in Heavy ion Collisions.

## Expected QCD Phase Diagram and Lattice Approaches to unravel it.

- The Transition Temperature  $T_c$  and Equation of State (EOS) have been predicted by lattice QCD.

## Expected QCD Phase Diagram and Lattice Approaches to unravel it.

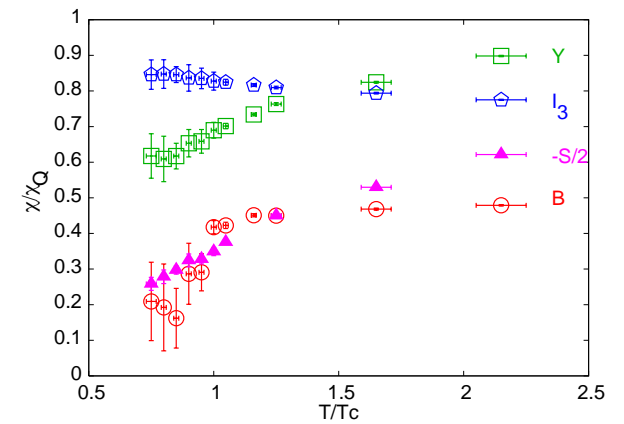
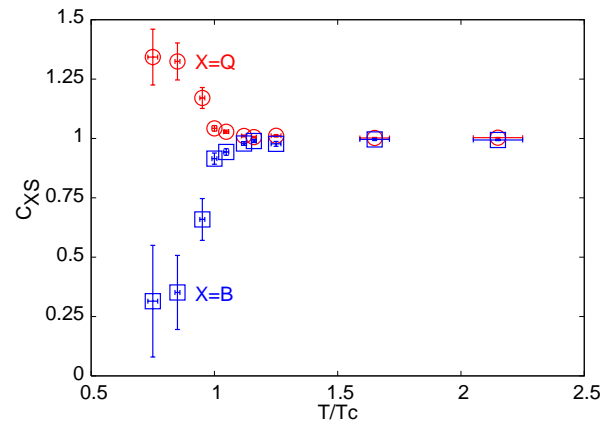
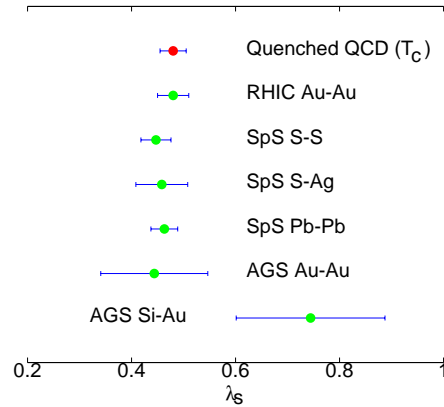
- The Transition Temperature  $T_c$  and Equation of State (EOS) have been predicted by lattice QCD.



Bernard et al., MILC hep-lat/0509053.

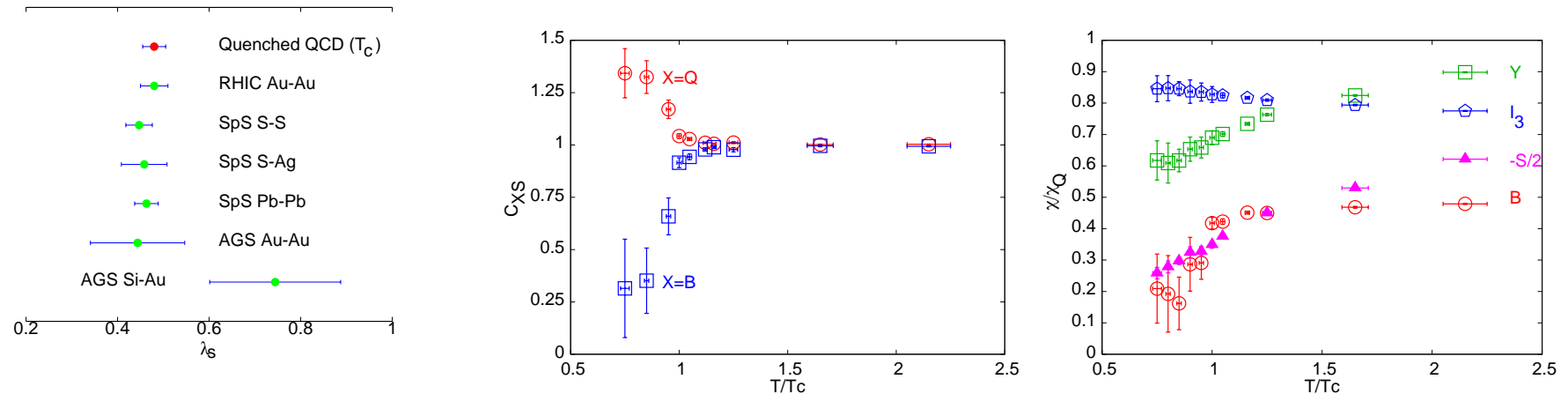
- Other quantities: notably the Wróblewski Parameter  $\lambda_s$  and other correlations for Heavy Ion Physics.

- Other quantities: notably the Wróblewski Parameter  $\lambda_s$  and other correlations for Heavy Ion Physics.



Gavai and Gupta, Phys Rev D65, 2002 and hep-lat/0510044.

- Other quantities: notably the Wróblewski Parameter  $\lambda_s$  and other correlations for Heavy Ion Physics.



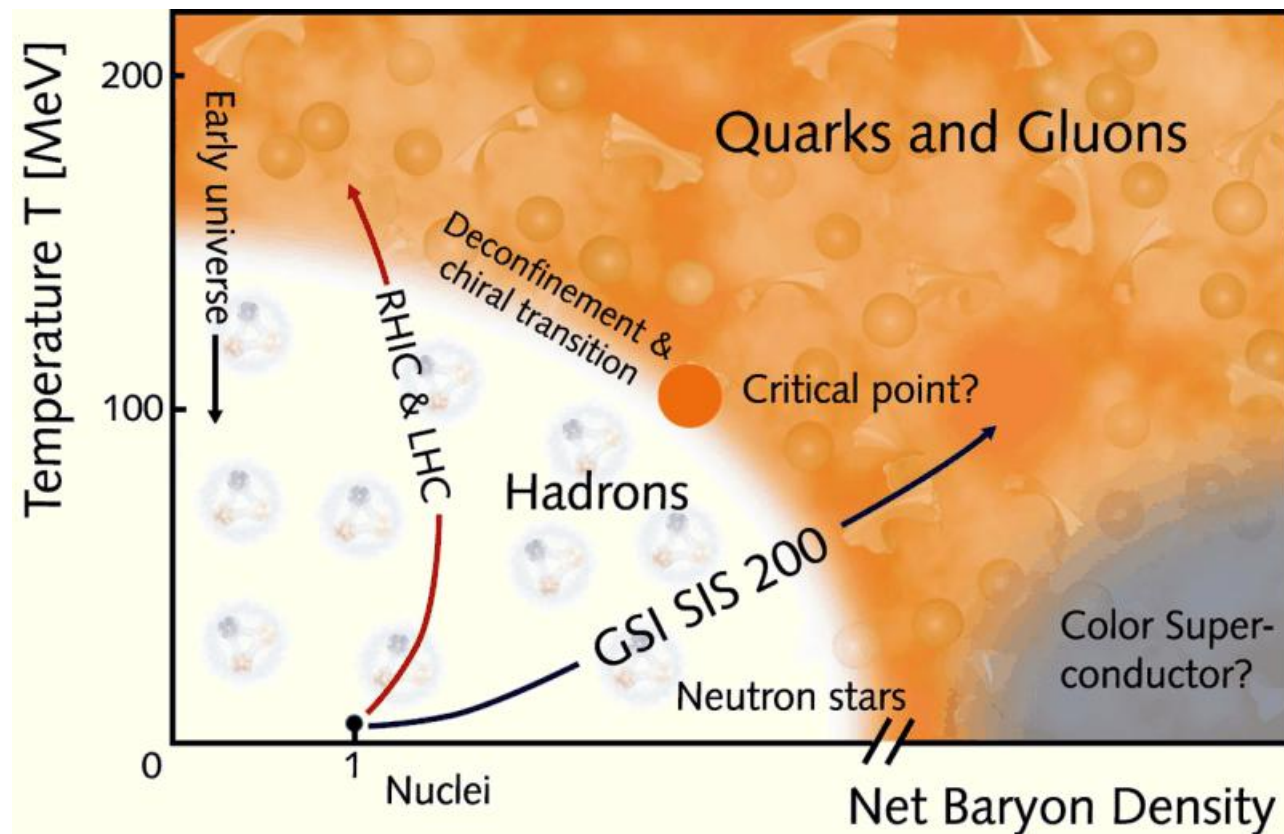
Gavai and Gupta, Phys Rev D65, 2002 and hep-lat/0510044.

- $\lambda_s$  — Measure of Production of strange quark-antiquark pairs; Expts agree with estimates from the new state Quark-Gluon Plasma.
  - Lattice QCD suggests that strangeness carried by quark-like objects
  - Robust correlations like BQ are better observables.

- Host of new results now on  $T$ - $\mu$  phase diagram and more complex observables such as  $J/\psi$ -dissolution/persistence, dileptons, speed of sound, transport coefficients... etc.



- Host of new results now on  $T$ - $\mu$  phase diagram and more complex observables such as  $J/\psi$ -dissolution/persistence, dileptons, speed of sound, transport coefficients... etc.



- New conceptual problems at nonzero  $\mu_B$  : Fermion determinant becomes complex, known analytical/numerical methods fail.
- Fermion Sign (Phase) Problem.

- New conceptual problems at nonzero  $\mu_B$  : Fermion determinant becomes complex, known analytical/numerical methods fail.
- Fermion Sign (Phase) Problem.
- Tremendous progress recently, discussed below. BUT, still unable to address the very high density and low temperature regions of colour superconductivity.
  - Two parameter Re-weighting (Z. Fodor & S. Katz, JHEP 0203 (2002) 014 ).

- New conceptual problems at nonzero  $\mu_B$  : Fermion determinant becomes complex, known analytical/numerical methods fail.
- Fermion Sign (Phase) Problem.
- Tremendous progress recently, discussed below. BUT, still unable to address the very high density and low temperature regions of colour superconductivity.
  - Two parameter Re-weighting (Z. Fodor & S. Katz, JHEP 0203 (2002) 014 ).
  - **Imaginary Chemical Potential** (Ph. de Frocrand & O. Philipsen, NP B642 (2002) 290; M.-P. Lombardo & M. D'Elia PR D67 (2003) 014505 ).

- New conceptual problems at nonzero  $\mu_B$  : Fermion determinant becomes complex, known analytical/numerical methods fail.
- Fermion Sign (Phase) Problem.
- Tremendous progress recently, discussed below. BUT, still unable to address the very high density and low temperature regions of colour superconductivity.
  - Two parameter Re-weighting (Z. Fodor & S. Katz, JHEP 0203 (2002) 014 ).
  - Imaginary Chemical Potential (Ph. de Frocrand & O. Philipsen, NP B642 (2002) 290; M.-P. Lombardo & M. D'Elia PR D67 (2003) 014505 ).
  - **Taylor Expansion** (C. Allton et al., PR D66 (2002) 074507 & D68 (2003) 014507; R.V. Gavai and S. Gupta, PR D68 (2003) 034506 ).

# Why Taylor series expansion?

- Ease of taking continuum and thermodynamic limit.

# Why Taylor series expansion?

- Ease of taking continuum and thermodynamic limit.
- E.g.,  $\exp[\Delta S]$  factor makes this exponentially tough for re-weighting and imaginary  $\mu$  needs analytic continuation.

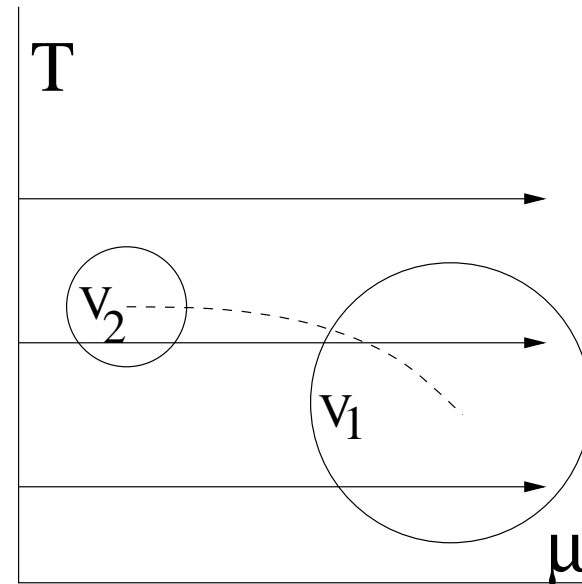
# Why Taylor series expansion?

- Ease of taking continuum and thermodynamic limit.
- E.g.,  $\exp[\Delta S]$  factor makes this exponentially tough for re-weighting and imaginary  $\mu$  needs analytic continuation.
- Better control of systematic errors.



# Why Taylor series expansion?

- Ease of taking continuum and thermodynamic limit.
- E.g.,  $\exp[\Delta S]$  factor makes this exponentially tough for re-weighting and imaginary  $\mu$  needs analytic continuation.
- Better control of systematic errors.



We study volume dependence at several  $T$  to i) bracket the critical region and then to ii) track its change as a function of volume.

# How Do We Do This Expansion?

Assuming  $N_f$  flavours of quarks, and denoting by  $\mu_f$  the corresponding chemical potentials, the QCD partition function is

$$\mathcal{Z} = \int DU \exp(-S_G) \prod_f \text{Det } M(m_f, \mu_f) \quad .$$

Canonical definitions then yield various number densities and susceptibilities :

$$n_i = \frac{T}{V} \frac{\partial \ln \mathcal{Z}}{\partial \mu_i} \quad \text{and} \quad \chi_{ij} = \frac{T}{V} \frac{\partial^2 \ln \mathcal{Z}}{\partial \mu_i \partial \mu_j} \quad .$$

Denoting higher order susceptibilities by  $\chi_{n_u, n_d}$ , the pressure  $P$  has the expansion in  $\mu$ :

$$\frac{\Delta P}{T^4} \equiv \frac{P(\mu, T)}{T^4} - \frac{P(0, T)}{T^4} = \sum_{n_u, n_d} \chi_{n_u, n_d} \frac{1}{n_u!} \left( \frac{\mu_u}{T} \right)^{n_u} \frac{1}{n_d!} \left( \frac{\mu_d}{T} \right)^{n_d} \quad (2)$$

# How Do We Do This Expansion?

Assuming  $N_f$  flavours of quarks, and denoting by  $\mu_f$  the corresponding chemical potentials, the QCD partition function is

$$\mathcal{Z} = \int DU \exp(-S_G) \prod_f \text{Det } M(m_f, \mu_f) \quad .$$

Canonical definitions then yield various number densities and susceptibilities :

$$n_i = \frac{T}{V} \frac{\partial \ln \mathcal{Z}}{\partial \mu_i} \quad \text{and} \quad \chi_{ij} = \frac{T}{V} \frac{\partial^2 \ln \mathcal{Z}}{\partial \mu_i \partial \mu_j} \quad .$$

Denoting higher order susceptibilities by  $\chi_{n_u, n_d}$ , the pressure  $P$  has the expansion in  $\mu$ :

$$\frac{\Delta P}{T^4} \equiv \frac{P(\mu, T)}{T^4} - \frac{P(0, T)}{T^4} = \sum_{n_u, n_d} \chi_{n_u, n_d} \frac{1}{n_u!} \left( \frac{\mu_u}{T} \right)^{n_u} \frac{1}{n_d!} \left( \frac{\mu_d}{T} \right)^{n_d} \quad (2)$$

# How Do We Do This Expansion?

Assuming  $N_f$  flavours of quarks, and denoting by  $\mu_f$  the corresponding chemical potentials, the QCD partition function is

$$\mathcal{Z} = \int DU \exp(-S_G) \prod_f \text{Det } M(m_f, \mu_f) \quad .$$

Canonical definitions then yield various number densities and susceptibilities :

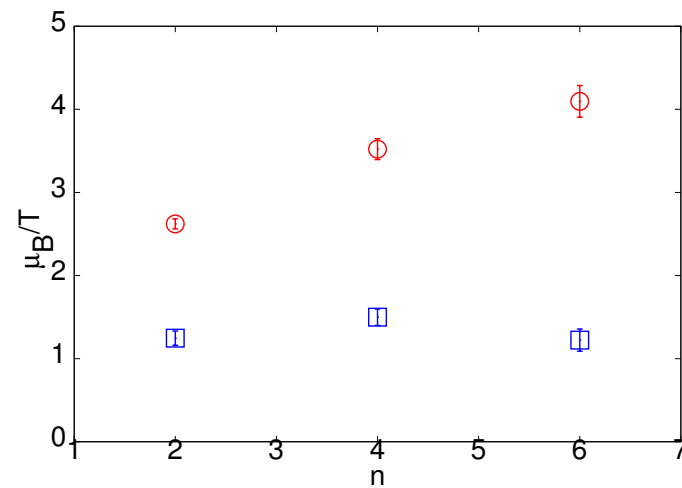
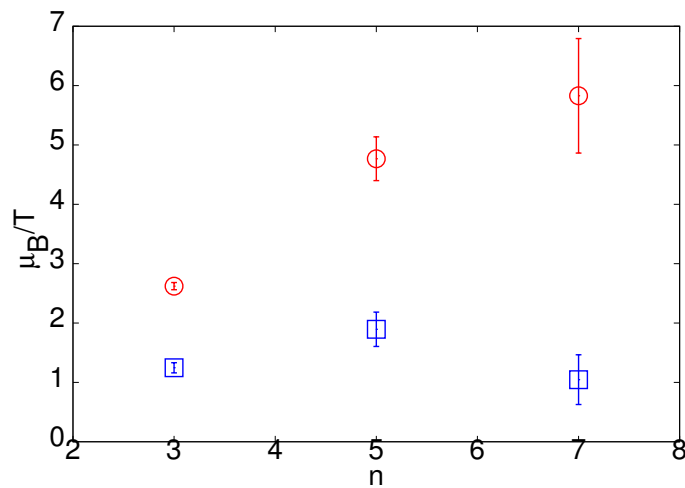
$$n_i = \frac{T}{V} \frac{\partial \ln \mathcal{Z}}{\partial \mu_i} \quad \text{and} \quad \chi_{ij} = \frac{T}{V} \frac{\partial^2 \ln \mathcal{Z}}{\partial \mu_i \partial \mu_j} \quad .$$

Denoting higher order susceptibilities by  $\chi_{n_u, n_d}$ , the pressure  $P$  has the expansion in  $\mu$ :

$$\frac{\Delta P}{T^4} \equiv \frac{P(\mu, T)}{T^4} - \frac{P(0, T)}{T^4} = \sum_{n_u, n_d} \chi_{n_u, n_d} \frac{1}{n_u!} \left( \frac{\mu_u}{T} \right)^{n_u} \frac{1}{n_d!} \left( \frac{\mu_d}{T} \right)^{n_d} \quad (2)$$

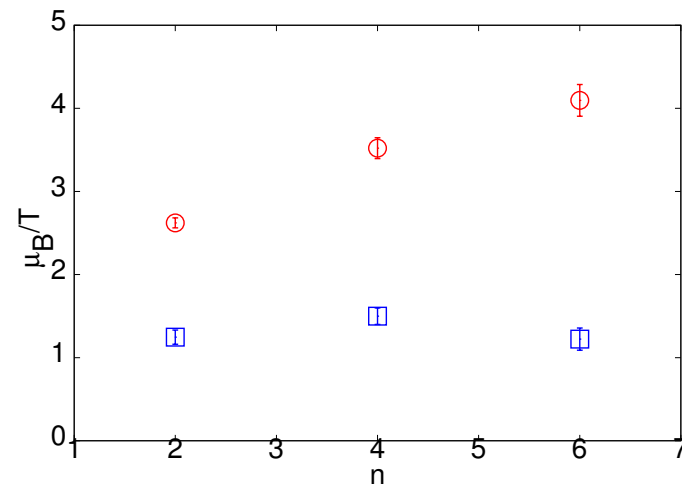
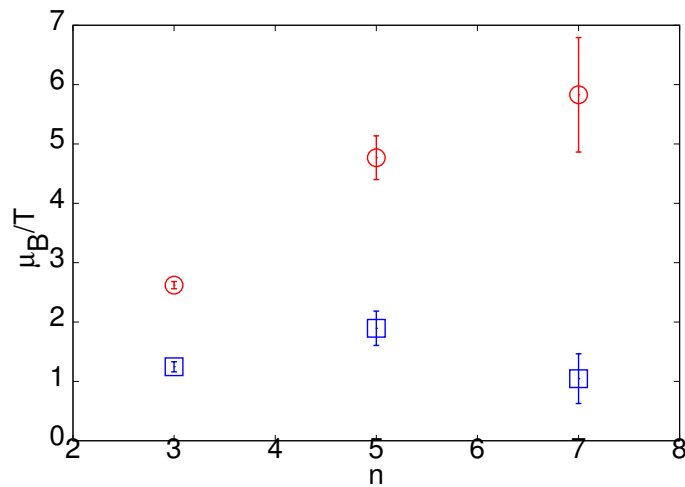
- From this expansion, a series for baryonic susceptibility can be constructed. Its radius of convergence gives the nearest critical point.
- Successive estimates for the radius of convergence can be obtained from these using  $\sqrt{\frac{\chi_B^n}{\chi_B^{n+2}}}$  or  $\sqrt{\frac{\chi_B^0}{\chi_B^n}}$ . We use terms up to 8th order in  $\mu$ , i.e., estimates from 2/4, 4/6 and 6/8 terms.

R. V. Gavai and Sourendu Gupta, Phys Rev. D 71, 114014 (2005).



- From this expansion, a series for baryonic susceptibility can be constructed. Its radius of convergence gives the nearest critical point.
- Successive estimates for the radius of convergence can be obtained from these using  $\sqrt{\frac{\chi_B^n}{\chi_B^{n+2}}}$  or  $\sqrt{\frac{\chi_B^0}{\chi_B^n}}$ . We use terms up to 8th order in  $\mu$ , i.e., estimates from 2/4, 4/6 and 6/8 terms.

R. V. Gavai and Sourendu Gupta, Phys Rev. D 71, 114014 (2005).



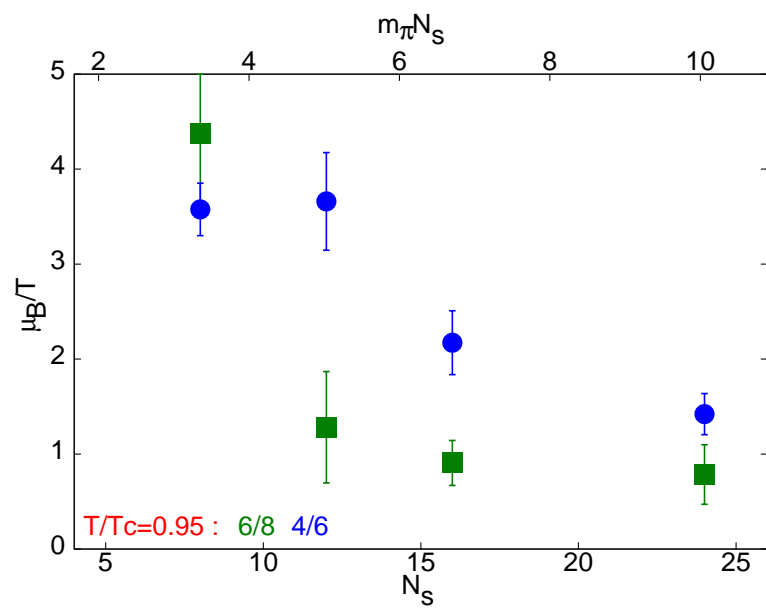
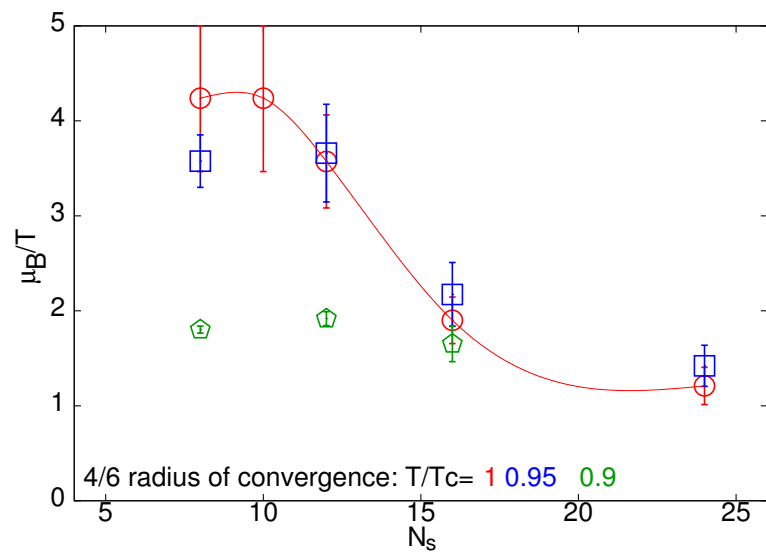
# How Do We Do This Expansion?

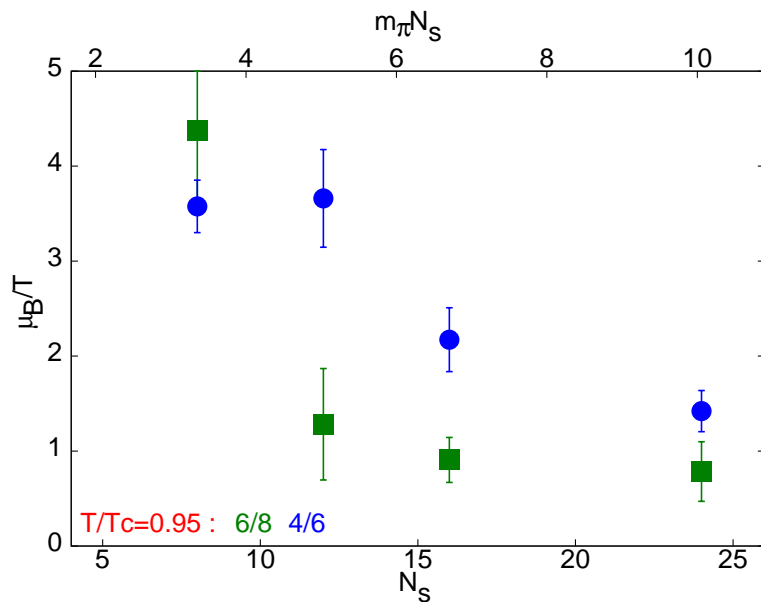
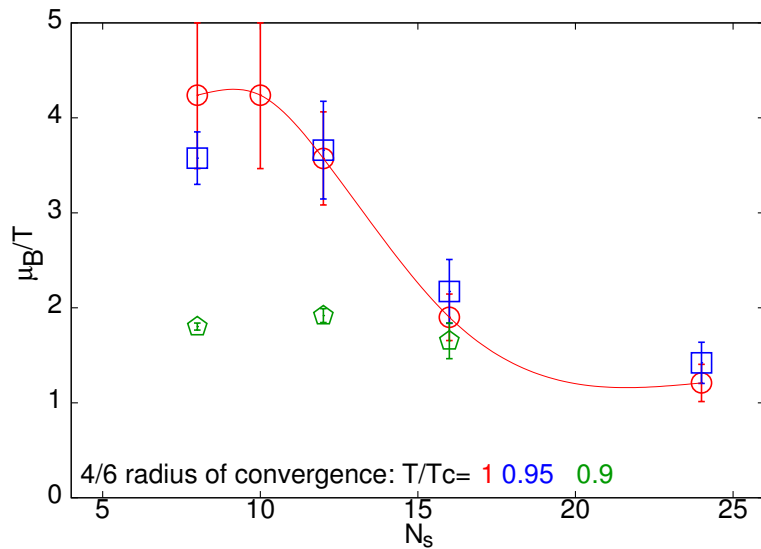


CRAY X1 of I L G T I , T I F R, Mumbai

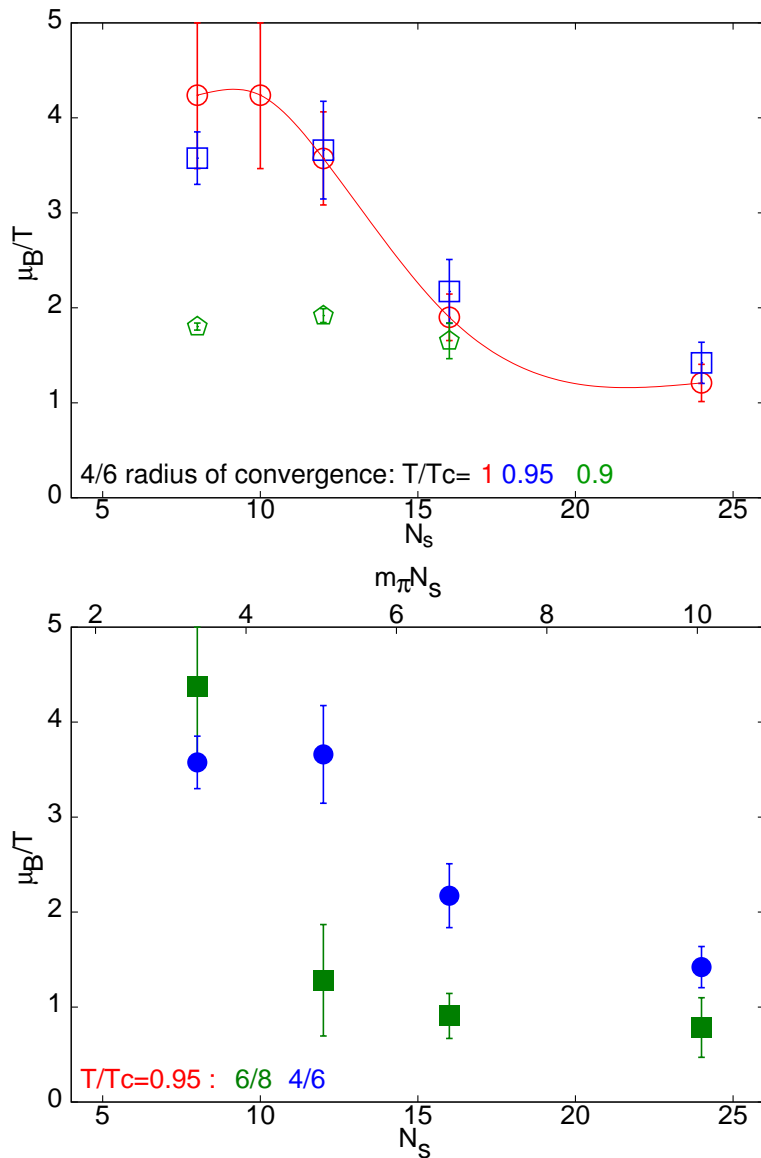
# More on our Results



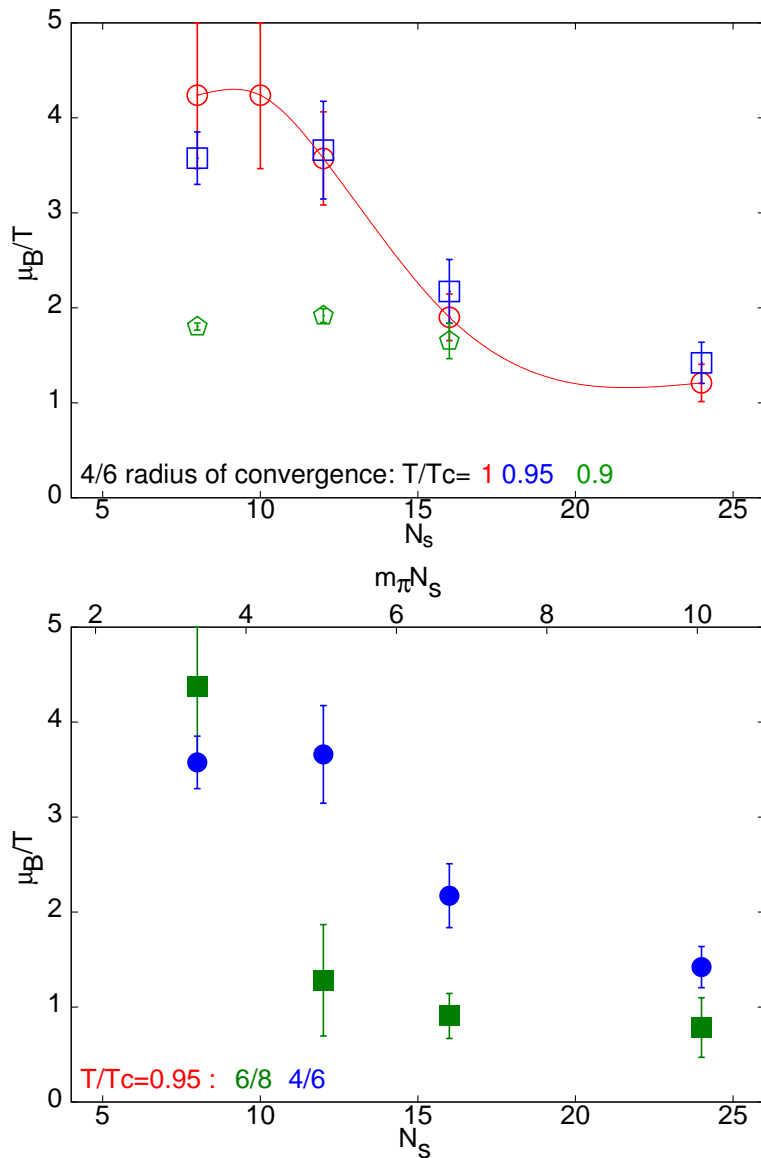




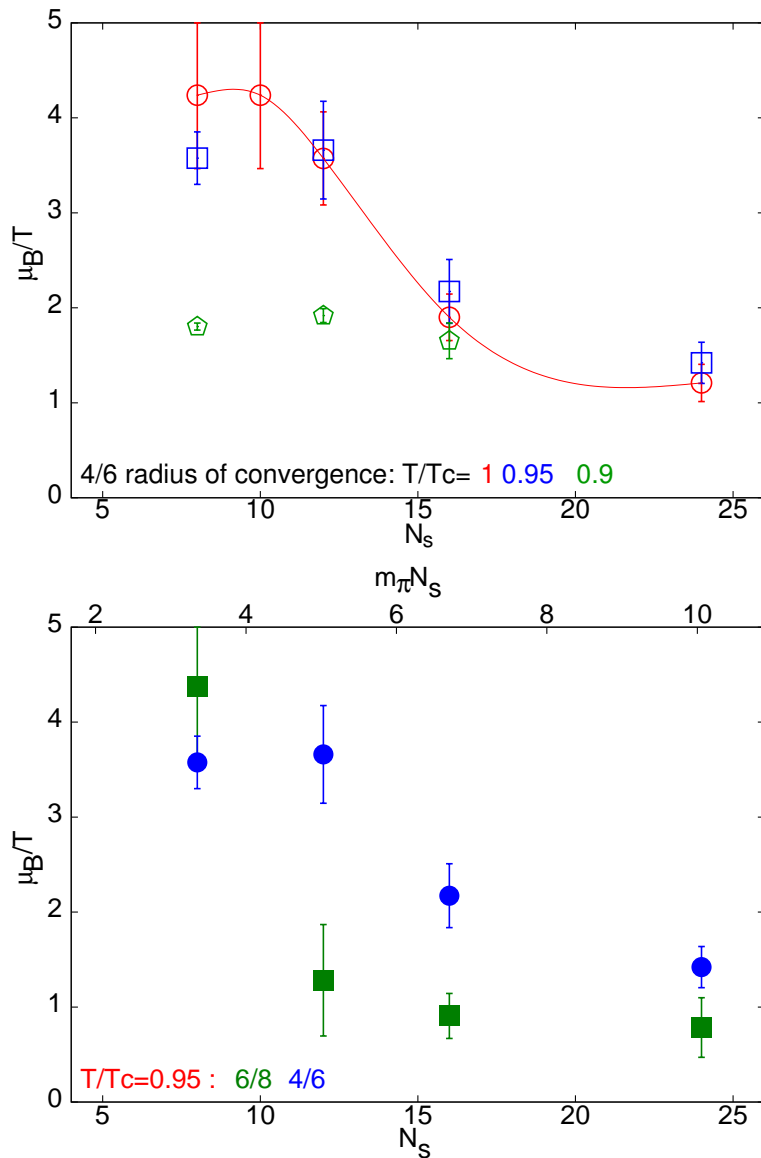
- We (RVG & S. Gupta, hep-lat/0412035) use terms up to 8th order in  $\mu$ .
- Our estimate consistent with Fodor & Katz (2002) [ $m_\pi/m_\rho = 0.31$  and  $N_s m_\pi \sim 3-4$ ].



- We (RVG & S. Gupta, hep-lat/0412035) use terms up to 8th order in  $\mu$ .
- Our estimate consistent with Fodor & Katz (2002) [ $m_\pi/m_\rho = 0.31$  and  $N_s m_\pi \sim 3-4$ ].
- Strong finite size effects for small  $N_s$ . A strong change around  $N_s m_\pi \sim 6$ .



- We (RVG & S. Gupta, hep-lat/0412035) use terms up to 8th order in  $\mu$ .
- Our estimate consistent with Fodor & Katz (2002) [ $m_\pi/m_\rho = 0.31$  and  $N_s m_\pi \sim 3-4$ ].
- Strong finite size effects for small  $N_s$ . A strong change around  $N_s m_\pi \sim 6$ .
- Critical point shifted to smaller  $\mu_B/T \sim 1 - 2$ .



- We (RVG & S. Gupta, hep-lat/0412035) use terms up to 8th order in  $\mu$ .
- Our estimate consistent with Fodor & Katz (2002) [ $m_\pi/m_\rho = 0.31$  and  $N_s m_\pi \sim 3-4$ ].
- Strong finite size effects for small  $N_s$ . A strong change around  $N_s m_\pi \sim 6$ .
- Critical point shifted to smaller  $\mu_B/T \sim 1 - 2$ .
- Bielefeld-Swansea results (hep-lat/0501030) up to 6th order. They use  $N_s m_\pi \sim 15$  but have a large  $m_\pi/m_\rho \sim 0.7$ .

# Heavy Ion Collisions

- Where does one find these new phases ? Can they be produced in laboratory ?

# Heavy Ion Collisions

- Where does one find these new phases ? Can they be produced in laboratory ?
- Early Universe — About  $10 - 20\mu s$  after the Big Bang and in Cores of Dense Neutron Stars

# Heavy Ion Collisions

- Where does one find these new phases ? Can they be produced in laboratory ?
- Early Universe — About  $10 - 20\mu s$  after the Big Bang and in Cores of Dense Neutron Stars
- Quark-Gluon Plasma can be, and may **indeed** have been, produced in Heavy Ion Collisions in CERN, Geneva and BNL, New York.

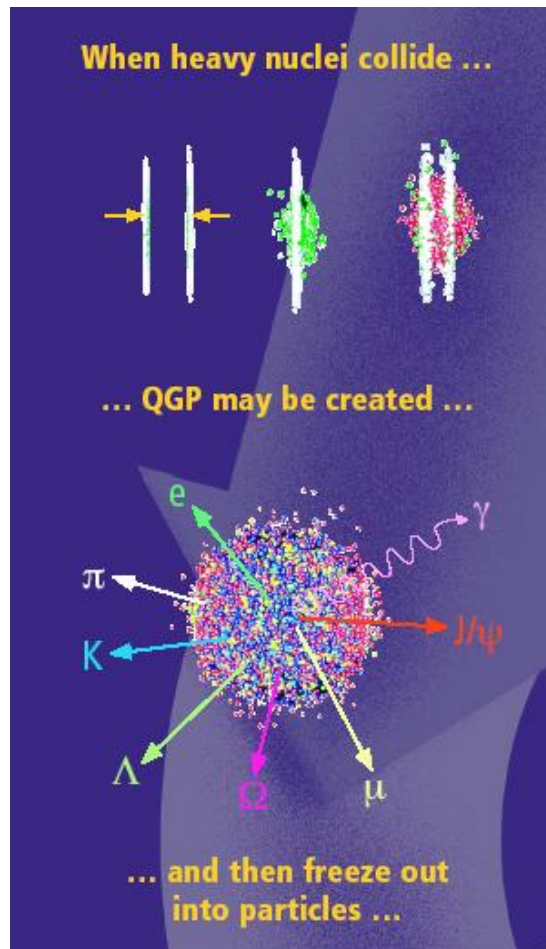


# Heavy Ion Collisions

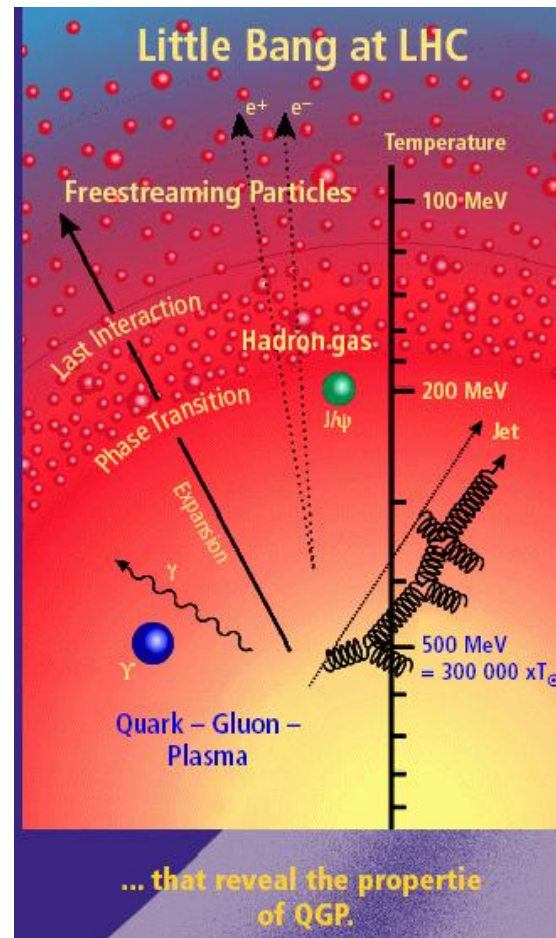
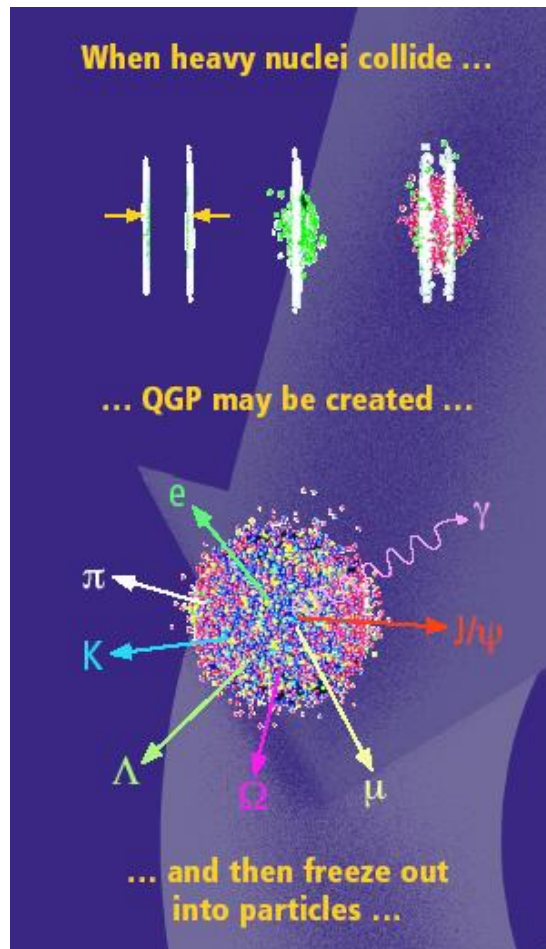
- Where does one find these new phases ? Can they be produced in laboratory ?
- Early Universe — About  $10 - 20\mu\text{s}$  after the Big Bang and in Cores of Dense Neutron Stars
- Quark-Gluon Plasma can be, and may **indeed** have been, produced in Heavy Ion Collisions in CERN, Geneva and BNL, New York.
- Necessary Conditions for QGP production :
  - High Energy Density,  $\approx 1\text{-}3 \text{ GeV}/\text{fm}^3$ .
  - Large System Size,  $L \gg \Lambda_{QCD}^{-1}$ .
  - Many particles

⇒ Heavy Ion Collisions at 99.5-99.995 % Velocity of Light.

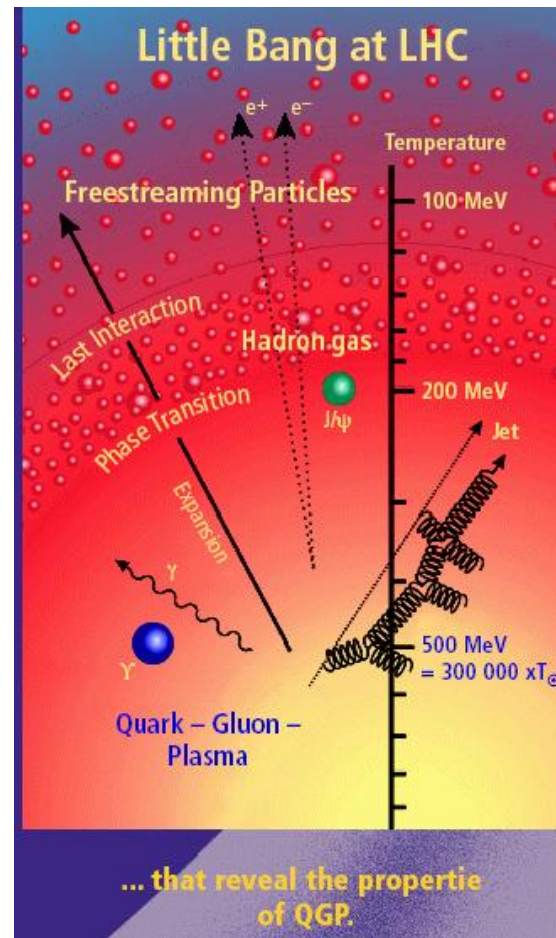
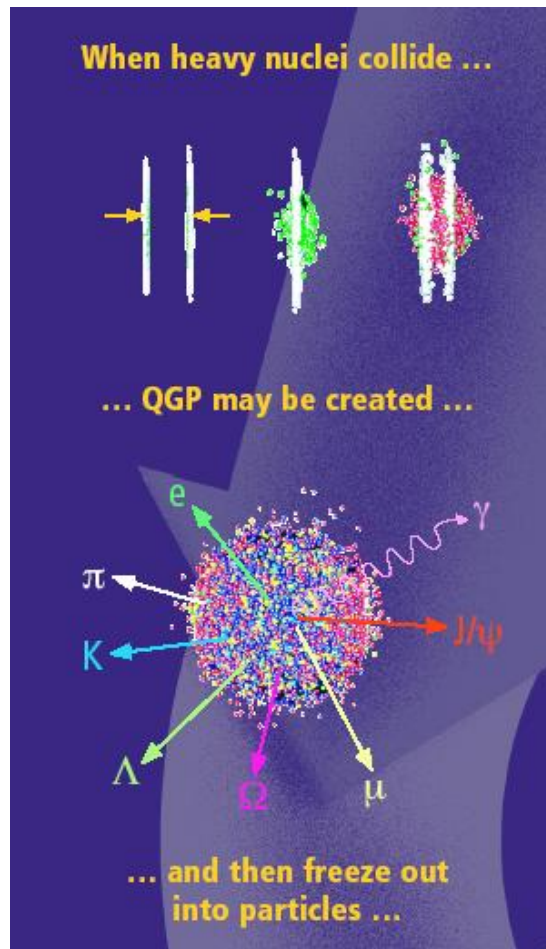
⇒ Heavy Ion Collisions at 99.5-99.995 % Velocity of Light.



⇒ Heavy Ion Collisions at 99.5-99.995 % Velocity of Light.

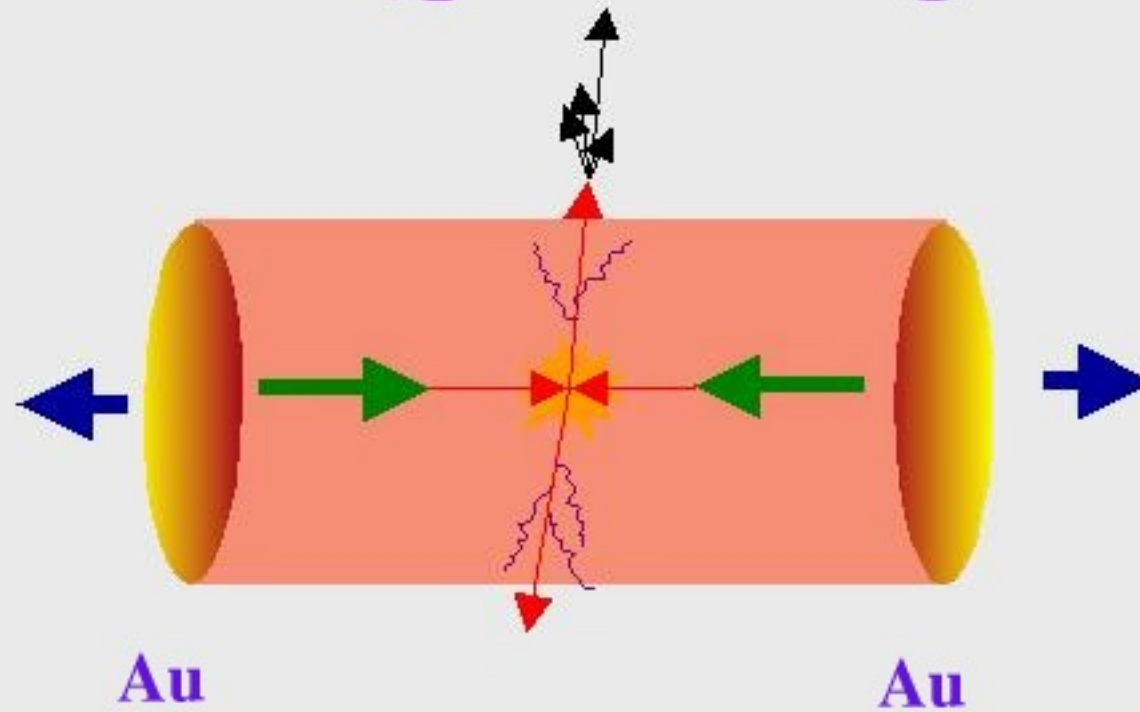


⇒ Heavy Ion Collisions at 99.5-99.995 % Velocity of Light.

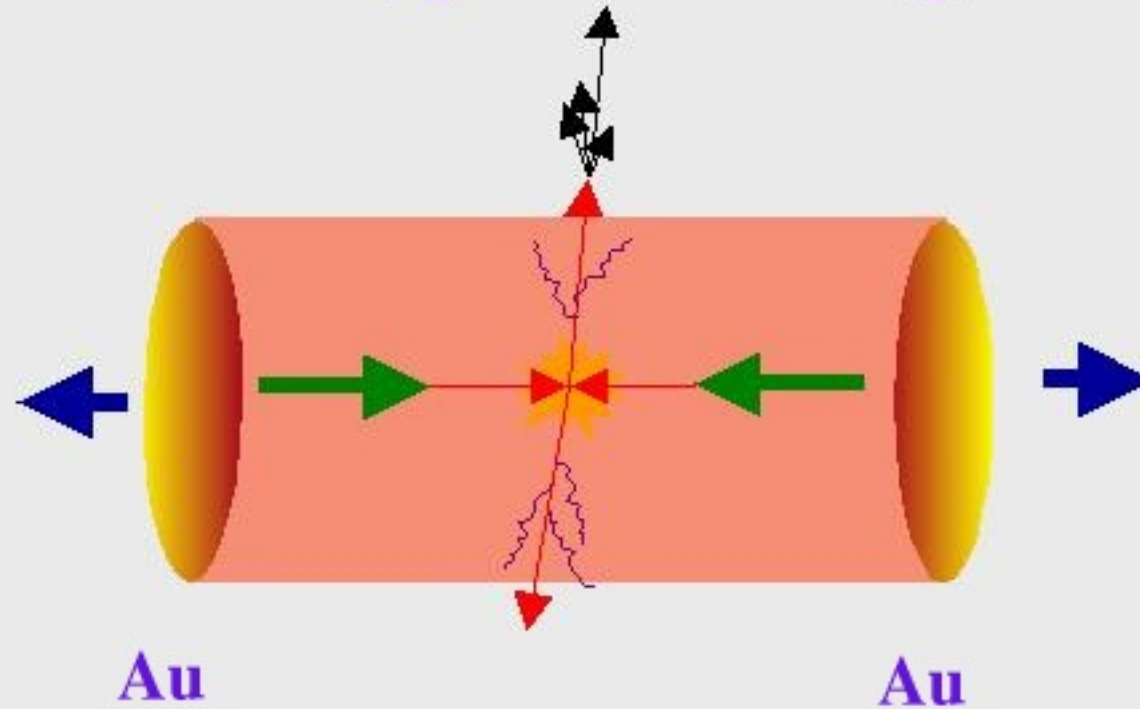


Fireball of QGP condenses into hadrons in  $\approx 10^{-23}$  seconds.

# *Jet Quenching*



# Jet Quenching



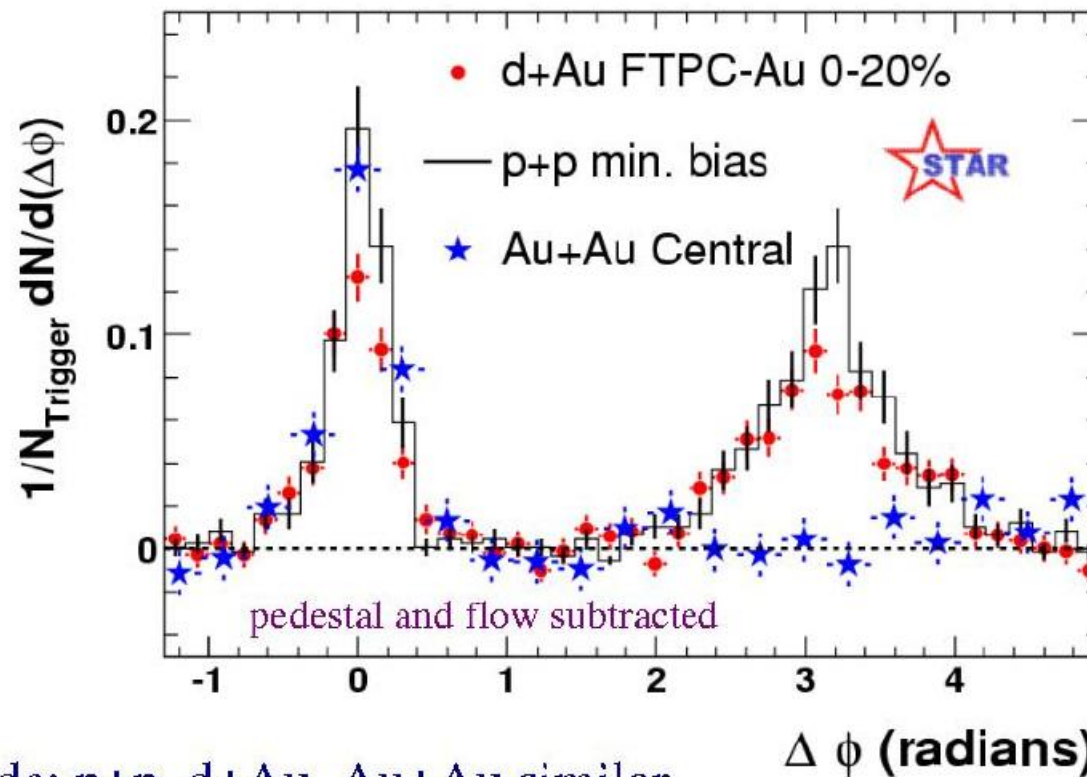
- Rare, Highly Energetic Scatterings produce jets of particles :  $g + g \rightarrow g + g$ .
- Quark-Gluon Plasma, any medium in general, interacts with a jet, causing it to lose energy – Jet Quenching.

- On-Off test possible – Compare Collisions of Heavy-Heavy nuclei with Light-Heavy or Light-Light.



- On-Off test possible – Compare Collisions of Heavy-Heavy nuclei with Light-Heavy or Light-Light.

## Azimuthal distributions



Near- side: p+p, d+Au, Au+Au similar

Back- to- back: Au+Au strongly suppressed relative to p+p and d+Au

# Anomalous $J/\psi$ Suppression : CERN NA50 results

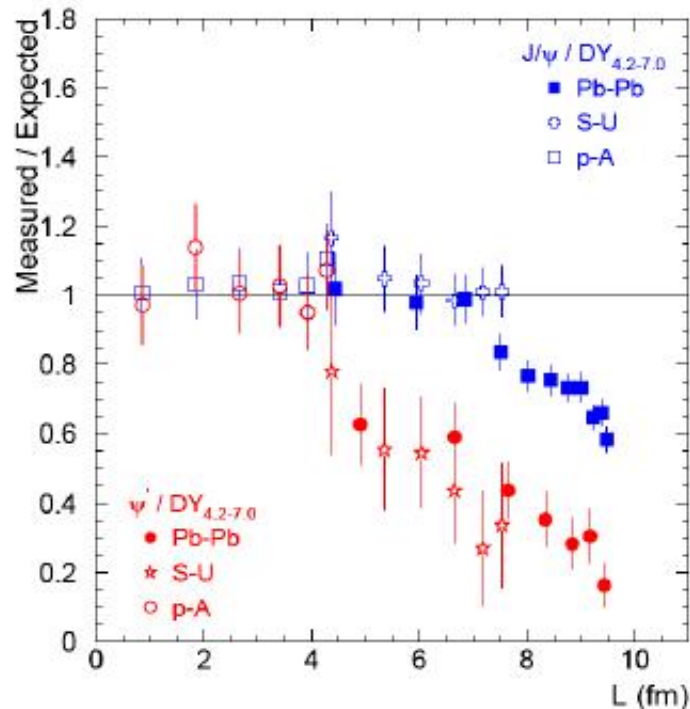
- ♠ Matsui-Satz idea —  $J/\psi$  suppression as a signal of QGP.
- ♠ Deconfinement  $\rightsquigarrow$  Screening of coloured quarks, which cannot bind.

# Anomalous $J/\psi$ Suppression : CERN NA50 results

Expected = Glauber absorption model

$$\sigma_{\text{abs}}(J/\psi) = 4.18 \pm 0.35 \text{ mb}$$

$$\sigma_{\text{abs}}(\psi') = 7.60 \pm 1.12 \text{ mb}$$



- S-U and **peripheral Pb-Pb**  $(J/\psi)/DY$  results follow the absorption curve extrapolated from p-A measurements.
- **Pb-Pb central** collisions show an **anomalous  $(J/\psi)/DY$  suppression** with respect to p-A behaviour.
- $\psi'/DY$  behaviour is the same in **S-U** and **Pb-Pb** interactions and not compatible with the one observed in p-A collisions.
- $\psi'$  **anomalous suppression** sets in earlier than the  $J/\psi$  one.

# $J/\psi$ Suppression

# $J/\psi$ Suppression or Not ?

- Original Matsui-Satz idea — Based on Quarkonium potential model calculations and an Ansatz for temperature dependence  $\rightsquigarrow$  dissolution of  $J/\psi$  and  $\chi_c$  by  $1.1T_c$ .

# $J/\psi$ Suppression or Not ?

- Original Matsui-Satz idea — Based on Quarkonium potential model calculations and an Ansatz for temperature dependence  $\rightsquigarrow$  dissolution of  $J/\psi$  and  $\chi_c$  by  $1.1T_c$ .
- Impressive NA50 results from CERN.

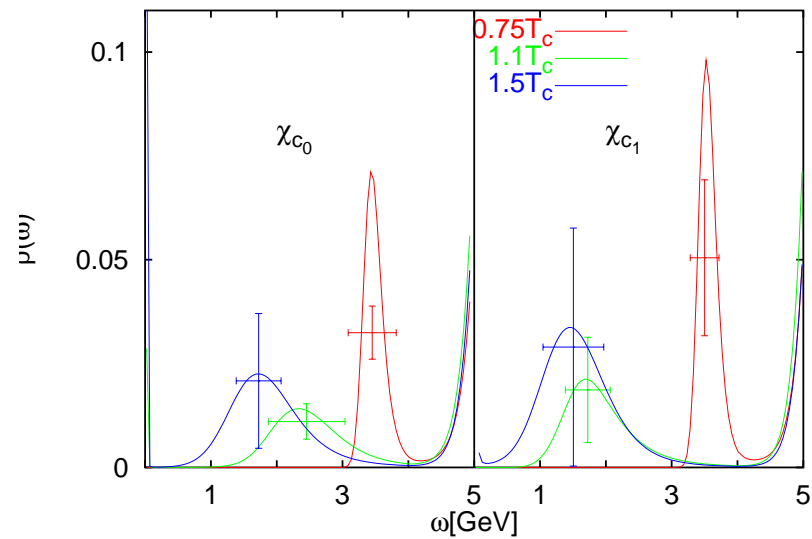
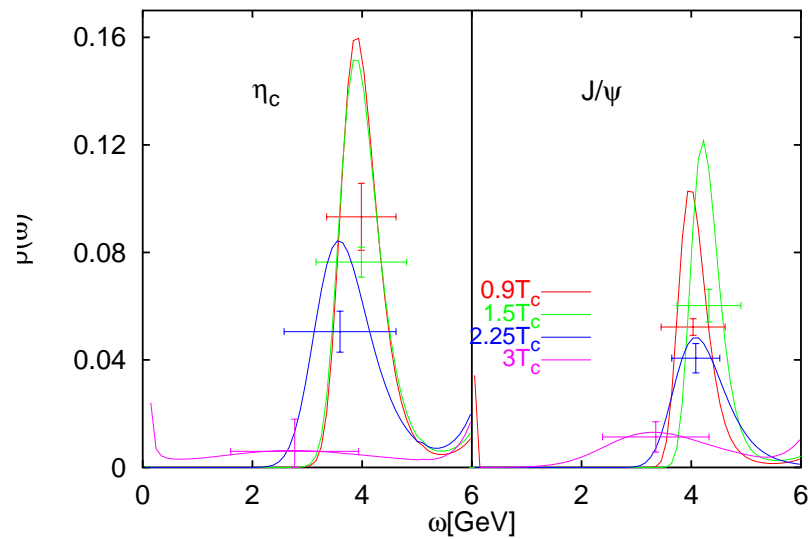
# $J/\psi$ Suppression or Not ?

- Original Matsui-Satz idea — Based on Quarkonium potential model calculations and an Ansatz for temperature dependence  $\rightsquigarrow$  dissolution of  $J/\psi$  and  $\chi_c$  by  $1.1T_c$ .
- Impressive NA50 results from CERN.
- A critical assessment of the original theoretical argument: Made feasible by the recognition of MEM technique as a tool to extract spectral functions from the temporal correlators computed on the Euclidean lattice.

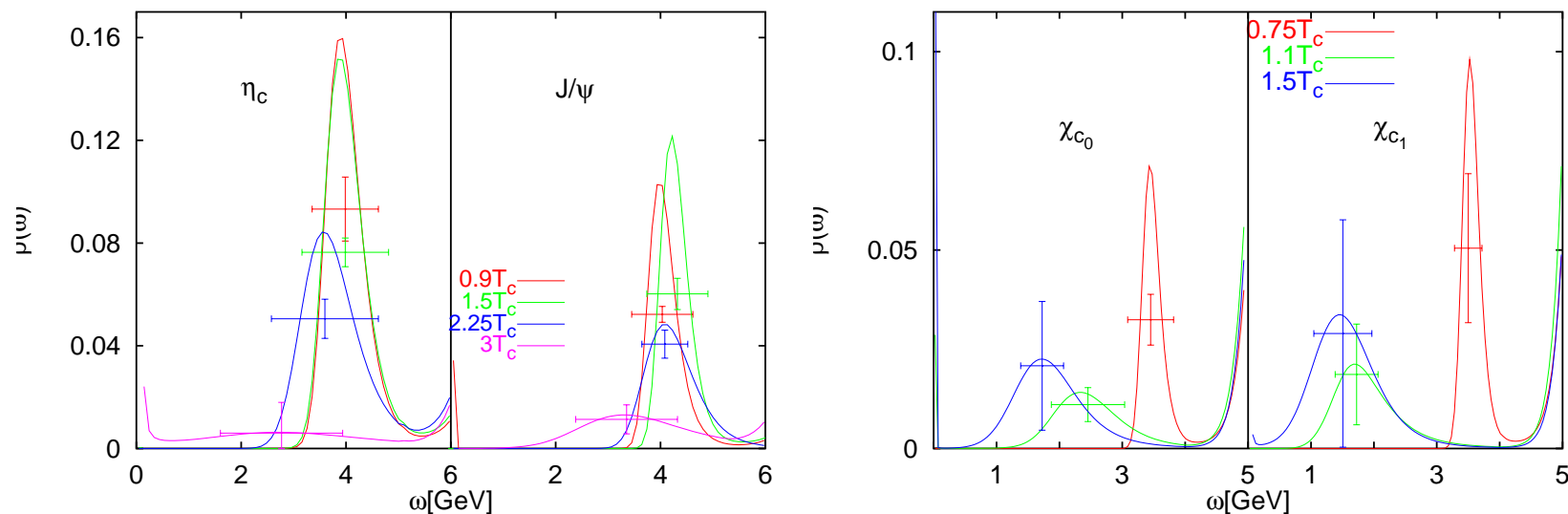
# $J/\psi$ Suppression or Not ?

- Original Matsui-Satz idea — Based on Quarkonium potential model calculations and an Ansatz for temperature dependence  $\rightsquigarrow$  dissolution of  $J/\psi$  and  $\chi_c$  by  $1.1T_c$ .
- Impressive NA50 results from CERN.
- A critical assessment of the original theoretical argument: Made feasible by the recognition of MEM technique as a tool to extract spectral functions from the temporal correlators computed on the Euclidean lattice.
- Caution : nonzero temperature obtained by making temporal lattices shorter.



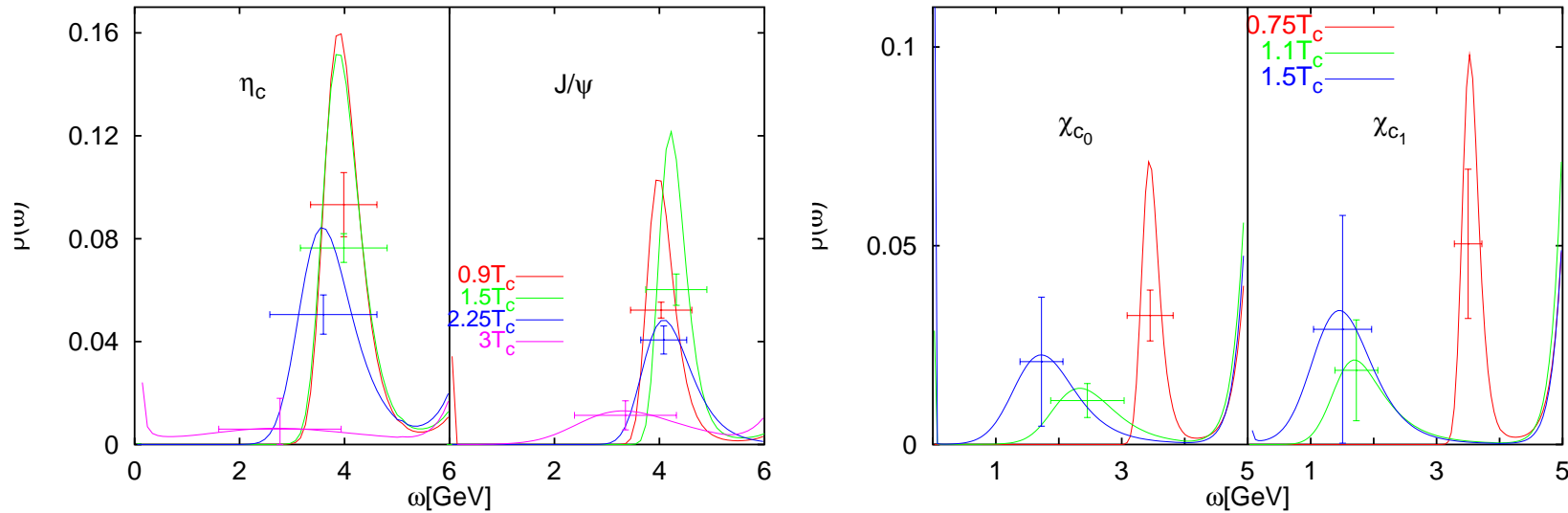


$48^3 \times 12$  to  $64^3 \times 24$  Lattices used : (S. Datta et al., Phys. Rev. D 69, 094507 (2004).)



$48^3 \times 12$  to  $64^3 \times 24$  Lattices used : (S. Datta et al., Phys. Rev. D 69, 094507 (2004).)

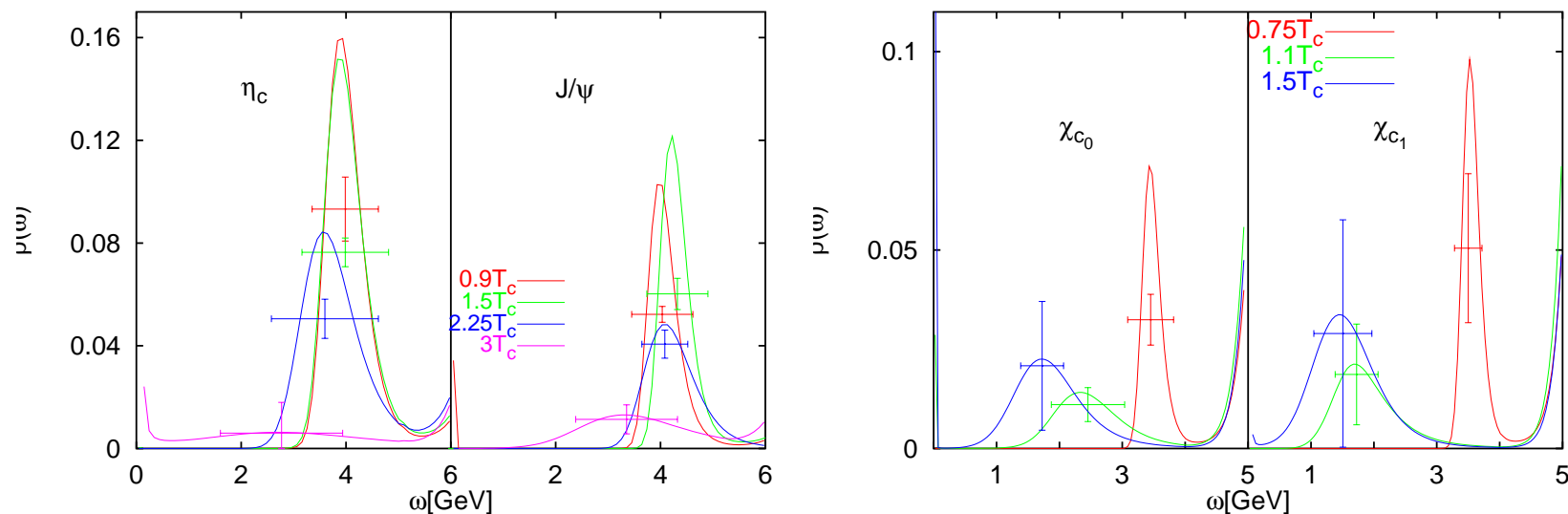
♠  $\chi_c$  seems to indeed dissolve by  $1.1T_c$ , however,  $J/\psi$  and  $\eta_c$  persist up to  $2.25T_c$  and are gone at  $3T_c$ ; Similar results by Asakawa-Hatsuda and Matsufuru.



$48^3 \times 12$  to  $64^3 \times 24$  Lattices used : (S. Datta et al., Phys. Rev. D 69, 094507 (2004).)

♠  $\chi_c$  seems to indeed dissolve by  $1.1T_c$ , however,  $J/\psi$  and  $\eta_c$  persist up to  $2.25T_c$  and are gone at  $3T_c$ ; Similar results by Asakawa-Hatsuda and Matsufuru.

♠ Since about 30 % observed  $J/\psi$  come through  $\chi$  decays, expect changes of suppression patterns as a function of  $T$  or  $\sqrt{s}$ .



$48^3 \times 12$  to  $64^3 \times 24$  Lattices used : (S. Datta et al., Phys. Rev. D 69, 094507 (2004).)

♠  $\chi_c$  seems to indeed dissolve by  $1.1T_c$ , however,  $J/\psi$  and  $\eta_c$  persist up to  $2.25T_c$  and are gone at  $3T_c$ ; Similar results by Asakawa-Hatsuda and Matsufuru.

♠ Since about 30 % observed  $J/\psi$  come through  $\chi$  decays, expect changes of suppression patterns as a function of  $T$  or  $\sqrt{s}$ .

♠ Effect of inclusion of dynamical fermions ?

# Speed of Sound

- $C_s$  – Crucial for elliptic flow, hydrodynamical studies ...
- $C_v$  – Event-by-event temperature/ $p_T$  fluctuations.

# Speed of Sound

- $C_s$  – Crucial for elliptic flow, hydrodynamical studies ...
- $C_v$  – Event-by-event temperature/ $p_T$  fluctuations.
- Can be obtained from  $\ln Z$  by taking appropriate derivatives which relate it to the temperature derivative of anomaly measure  $\Delta/\epsilon$ .  
(RVG, S. Gupta and S. Mukherjee, hep-lat/0412036 )
- New method to obtain these differentially without getting negative pressure. Introducing a parameter 't', t=1 used in earlier Bielefeld studies, we use  $t = 0$ .  
(RVG, S. Gupta and S. Mukherjee, hep-lat/0506015 )

- Using lattices with 8, 10, and 12 temporal sites ( $38^3 \times 12$  and  $38^4$  lattices) and with statistics of 0.5-1 million iterations,  $\epsilon$ ,  $P$ ,  $s$ ,  $C_s^2$  and  $C_v$  obtained in continuum.

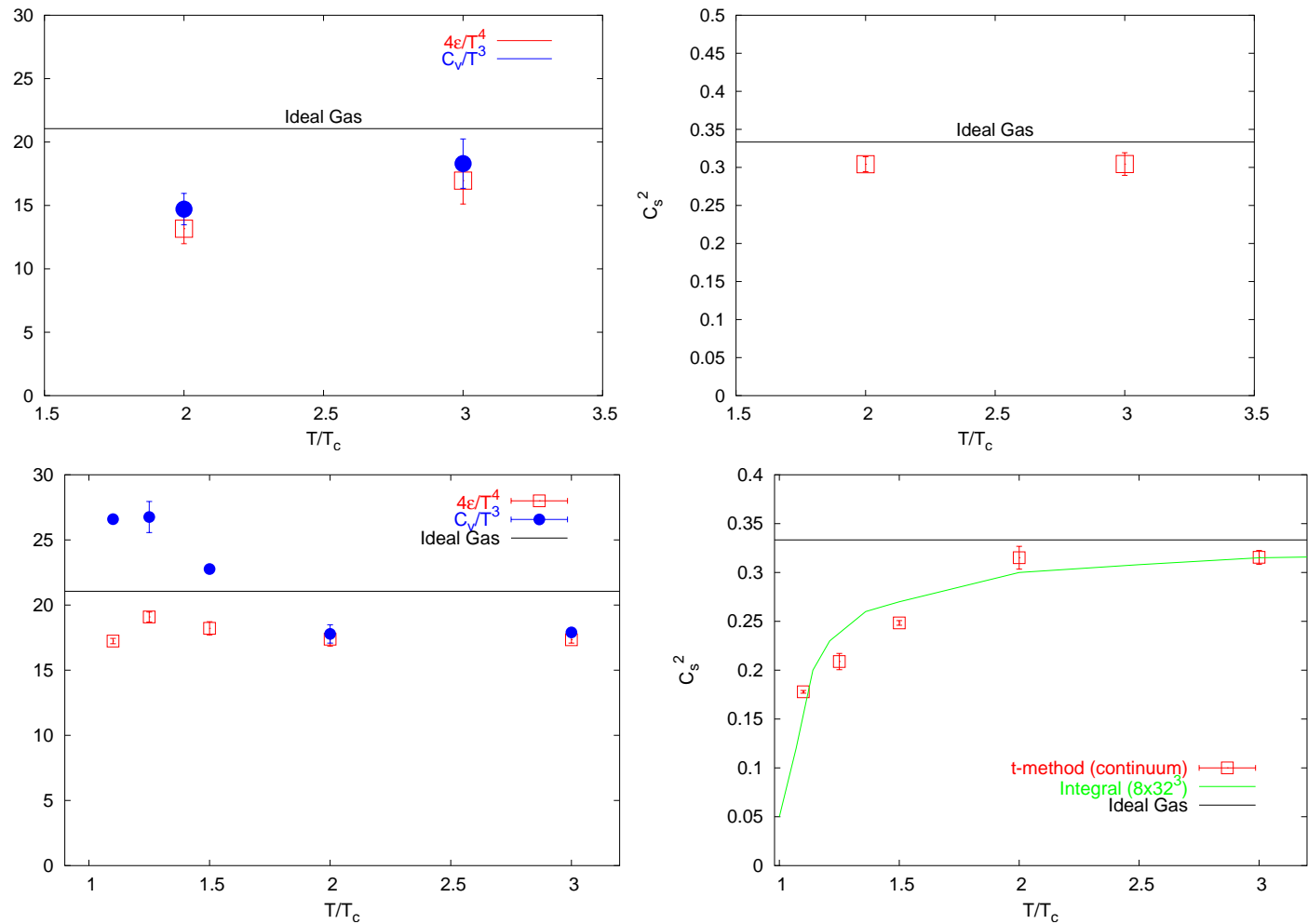
- Using lattices with 8, 10, and 12 temporal sites ( $38^3 \times 12$  and  $38^4$  lattices) and with statistics of 0.5-1 million iterations,  $\epsilon$ ,  $P$ ,  $s$ ,  $C_s^2$  and  $C_v$  obtained in continuum.
- Entropy agrees with strong coupling SYM prediction  
(Gubser, Klebanov & Tseytlin, NPB '98, 202)

$$\begin{aligned}
 \frac{s}{s_0} &= f(g^2 N_c), \quad \text{where} \\
 f(x) &= \frac{3}{4} + \frac{45}{32} \zeta(3) (2x^{-3/2}) + \dots \quad \text{and} \\
 s_0 &= \frac{2}{3} \pi^2 N_c^2 T^3,
 \end{aligned} \tag{3}$$

for  $T = 3T_c$  but fails at  $2T_c$ , as do various weak coupling schemes.



## Results for $t = 1$ and $0$ respectively:



# Summary

- Lattice QCD **predicts** new states of strongly interacting matter and is able to shed light on the properties of the Quark-Gluon plasma phase.

# Summary

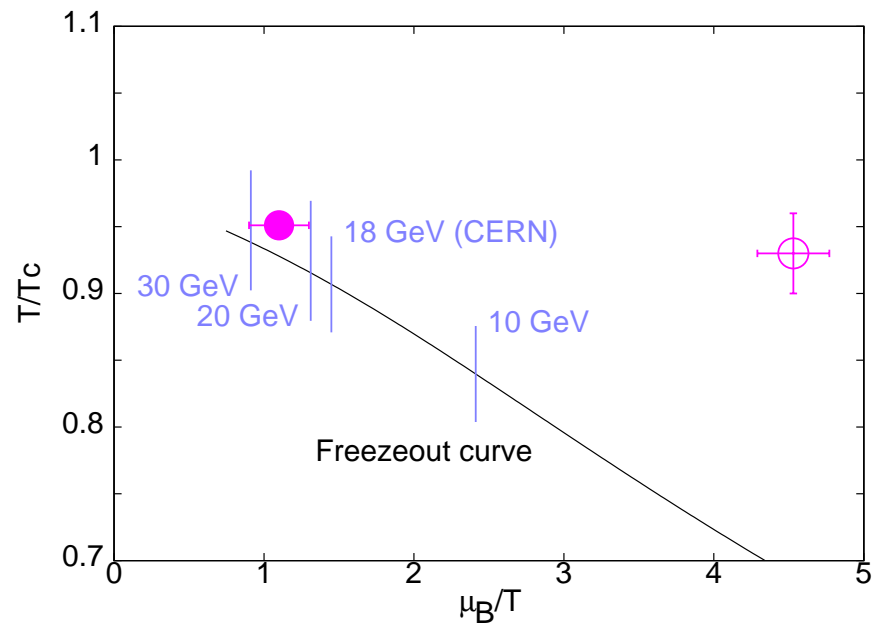
- Lattice QCD **predicts** new states of strongly interacting matter and is able to shed light on the properties of the Quark-Gluon plasma phase.
- Our results on correlations of quantum numbers suggest QGP to have quarklike excitations.

# Summary

- Lattice QCD **predicts** new states of strongly interacting matter and is able to shed light on the properties of the Quark-Gluon plasma phase.
- Our results on correlations of quantum numbers suggest QGP to have quarklike excitations.
- Phase diagram in  $T - \mu_B$  plane has begun to emerge: Our estimate for the critical point is  $\mu_B/T \sim 1 - 2$ .

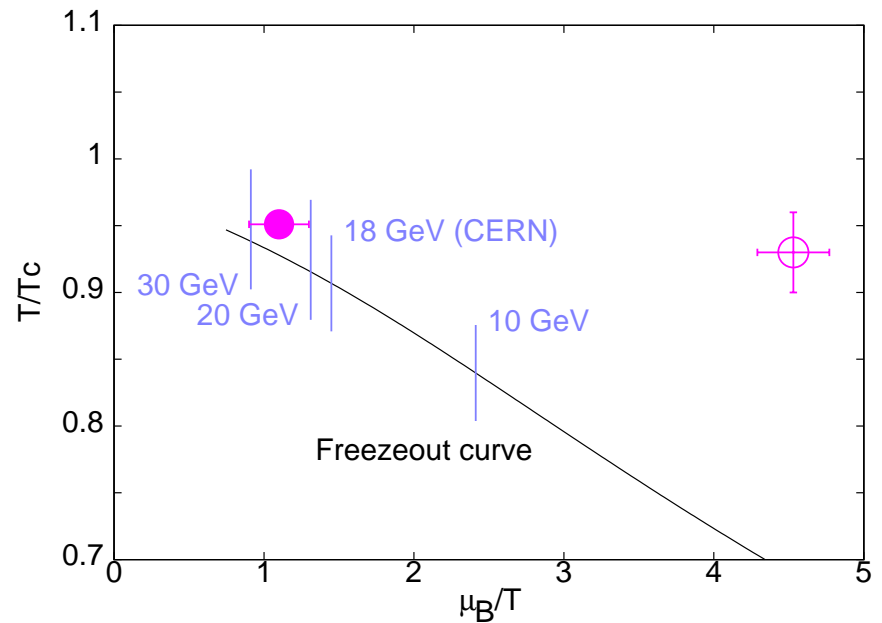
# Summary

- Lattice QCD **predicts** new states of strongly interacting matter and is able to shed light on the properties of the Quark-Gluon plasma phase.
- Our results on correlations of quantum numbers suggest QGP to have quarklike excitations.
- Phase diagram in  $T - \mu_B$  plane has begun to emerge: Our estimate for the critical point is  $\mu_B/T \sim 1 - 2$ .



# Summary

- Lattice QCD **predicts** new states of strongly interacting matter and is able to shed light on the properties of the Quark-Gluon plasma phase.
- Our results on correlations of quantum numbers suggest QGP to have quarklike excitations.
- Phase diagram in  $T - \mu_B$  plane has begun to emerge: Our estimate for the critical point is  $\mu_B/T \sim 1 - 2$ .



Heavy Ion Collisions in CERN Geneva, and BNL, New York, have seen tell-tale signs of QGP : Many surprises already and more excitement likely to come.