

Extreme QCD

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TIFR

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Extreme reductionism

Building things up

- Particles

- Nuclei and stars

- Hot matter

- Dense Matter

Future

Outline

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The reductionist method

Always pack a microscope when you go exploring

The reductionist method

Always pack a microscope when you go exploring

In order to understand something first find what it is made of.

- ▶ To understand chemistry, start with the chemical elements
- ▶ For life: understand the working of cells
- ▶ Matter: examine elementary particles

The well-known story of matter

- ▶ Existence of atoms deduced from the laws of stoichiometry.
- ▶ Connection with the Gas Laws: kinetic theory of gases, Avogadro's number. The length scale of atoms: 0.1 nm.
- ▶ The atom split in 1897: electrons (negatively charged) seen. Rutherford's experiments in 1911 reveal positively charged atomic nucleus: length scale of 1–10 fm.
- ▶ In 1913 X-ray spectroscopy established that the periodic table is ordered by the nuclear charge Z (Moseley).
- ▶ Great developments in nuclear physics: β -decay, fission, fusion: energy generation, understanding of the mechanism of stars, transmutation of elements, artificial elements.

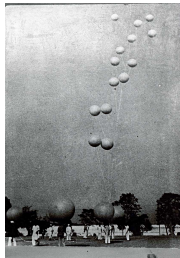
The puzzling behaviour of strong interactions

Protons are positively charged, but nucleus is usually stable. In fact, β -decays increase Z !

Neutrons discovered in 1933 (Chadwick).

In 1935 Yukawa proposed a new interaction to stabilize nuclei; called strong interactions: mediated by a new particle—a meson. In 1947 π observed in cosmic rays: Yukawa's **meson**.

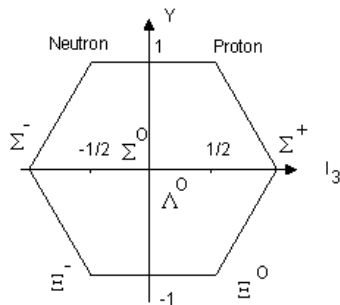
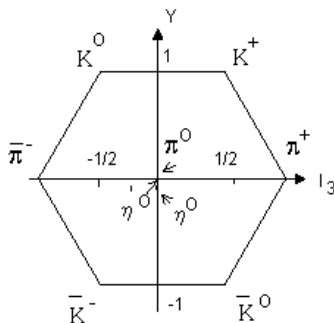
In 1947 entirely different mesons also found in cosmic rays. Through the '50s lots of new particles found. Baryons (like proton and neutron): fermions, mesons: bosons.



The hadron periodic table

Gell-Mann, Okubo and Zweig built hadrons from true elementary particles: quarks. Mesons = quark and anti-quark, baryons = three quarks.

Three varieties of quarks: up, down and strange.



A quantum particularity

Statistics

Truly elementary particles of the same kind indistinguishable.

- ▶ Exactly one particle per state: **Fermions**
- ▶ Any number particles in the same state: **Bosons**

Spin

Quantum mechanics allows only discrete angular momenta: $\hbar/2$ (Planck's constant).

- ▶ Fermions have angular momenta $\hbar/2, 3\hbar/2, 5\hbar/2$ *etc.*
- ▶ Bosons have angular momenta $0, \hbar, 2\hbar, \text{etc.}$

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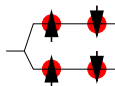
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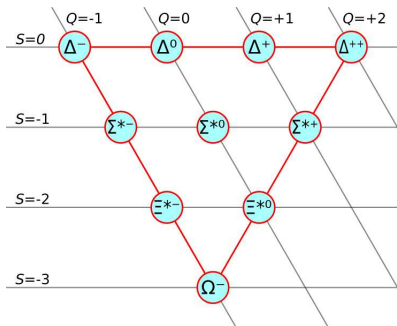
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A small puzzle: the gateway to the standard model



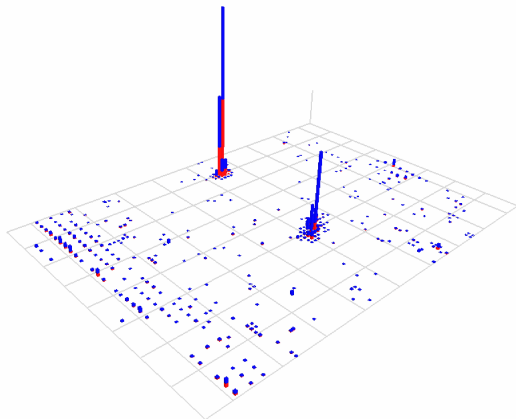
Baryon Δ^{++} contains three up quarks in the same state.

Quarks are fermions. Cannot be in the same state.

There must be three types of quarks. What distinguishes them?

New charge. Called **colour**. Turns out to be the charge of the strong interactions.

Seeing is believing



Single quarks are never seen in experiment: the only strongly interacting particles ever seen are hadrons.

Quantum ChromoDynamics

Quarks carry colour charge. Interact by exchanging gluons. Gluons also have colour charge. No other elementary particle has colour charge. The quantum theory of “coloured particles” is called QCD.

Binding of quarks into hadrons the true strong interaction; the binding of the nucleus a much weaker “van der Waals” remnant force.

From energy scales of a few MeV to TeV no substructure to quarks found!

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1908–2008: 30 Nobel prizes to almost 50 people!

Parameters of QCD

Fundamental theory: very few parameters.

1. Λ : an intrinsic mass scale. $\Lambda \simeq 200$ MeV; corresponding length scale: 1 fm. Strength of interaction distance dependent: $\simeq 1$ at 1 fm, decreases with distance: **asymptotic freedom**
2. Up and down quark masses: $m_u, m_d \simeq 5\text{--}10$ MeV. Is that natural— $m_{u,d} \ll \Lambda$? No. Approximate symmetry forces light quark masses almost to zero: **chiral symmetry**
3. A medium heavy quark: $m_s \simeq \Lambda$. Natural; no special symmetry.
4. Several very heavy quarks: $m_c, m_b, m_t \gg \Lambda$. Important at very short distances; unimportant at length scale ≥ 1 fm. Origin of heavy masses related to **Higgs boson**

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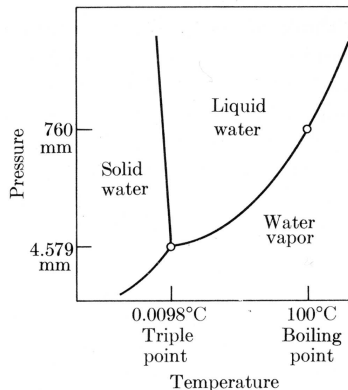
Future

Emergent behaviour

At macroscopic distances and times thermodynamics emerges from all theories of matter: universal laws.

Microscopic theories explain characteristics such as the specific heat or bulk compressibility.

Various kinds of matter also undergo **phase transitions**: location of phase transitions come from microscopic theory.

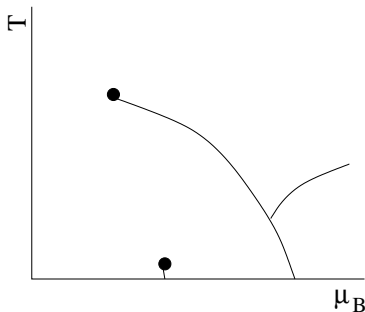


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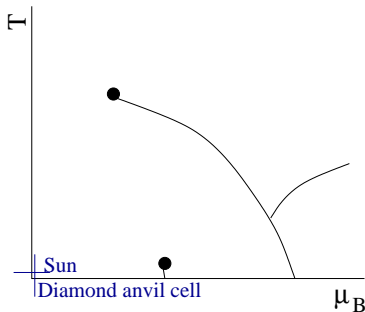


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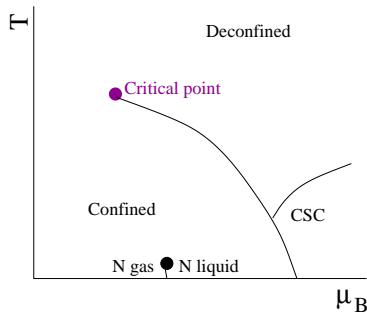


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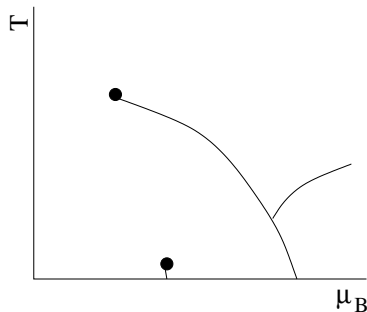


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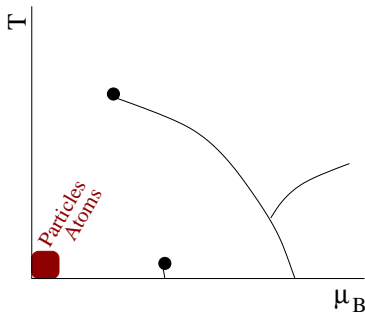


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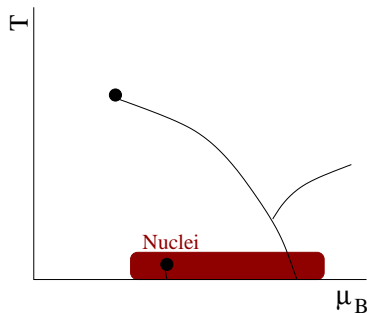


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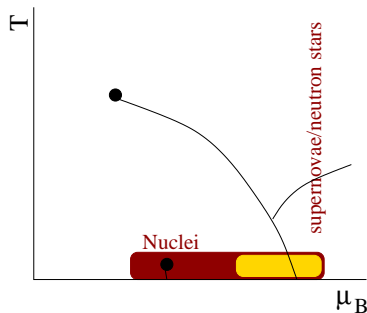


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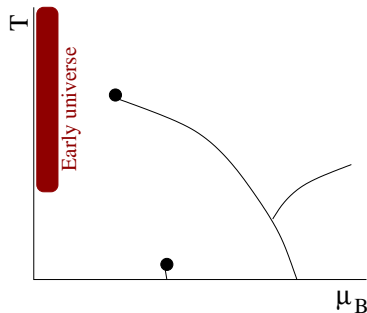


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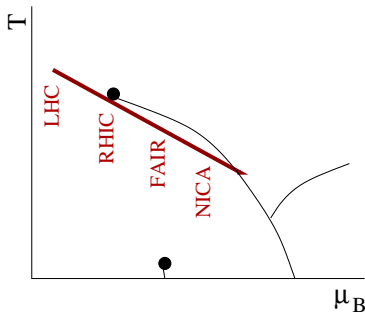


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Extreme computing

QCD mathematically intractable:
prize for proving that colour charge
cannot be produced in a lab: \$
1,000,000

Alternative: put it on computers.
Tremendous computing challenge:
multi Eflops year. All future
developments require base of
supercomputing.

- ▶ Humans: $\simeq 0.1$ flops
- ▶ Desktops: $\simeq 1$ Gflops
- ▶ QCD today: $\simeq 1\text{--}10$ Tflops
- ▶ QCD in 5 years: $\simeq 1$ Pflops
- ▶ US long-range plan: $\simeq 1$ Eflops



IBM Blue Gene: designed
in collaboration with QCD
practitioners.

1 flops: adding two 8-digit
numbers in 1 sec

The mass of matter



Can the mass of this system be computed from the standard model of particle physics?

1. Protein folding and other entropic terms ≈ 1 eV
2. Binding energy of electrons ≈ 1 KeV
3. Electron rest mass ≈ 1 MeV
4. Proton mass ≈ 1 GeV

QCD answers the question with accuracy of about 1 part in 10^3 . This involves computing the mass of the proton from first principles.

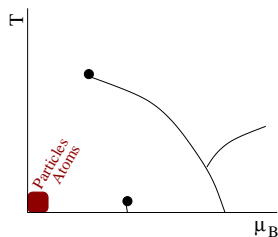
Exotics

Lesson from the '60s: meson = 1 quark + 1 anti-quark; baryon = 3 quarks. Nothing else known.

Excitement of the '00s: pentaquark baryons = 4 quarks + 1 antiquark. Weak evidence at present.

Mathur et al., 2004

Future: glueballs = multiple gluons; hybrid mesons = 2 quarks + 2 anti-quarks; others?



Nuclear accidents

The next-to-simplest nucleus: ${}^2\text{H}$ very lightly bound. Why?

	$a({}^1S_0)$ fm	
	pp	np
Expt*	-7.8098 (23)	-23.748 (10)
Bonn	-7.82	-23.75
Paris	-7.85	-23.72

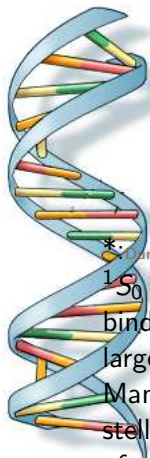
*: [Dumbras et al., 1983](#)

1S_0 scattering lengths in fm. The natural scale for nuclear binding is 1 fm, so the scattering lengths are unnaturally large. Why?

Many similar coincidences known. Some very important for stellar nucleosynthesis. Understanding from QCD? Beginning of a new subject.

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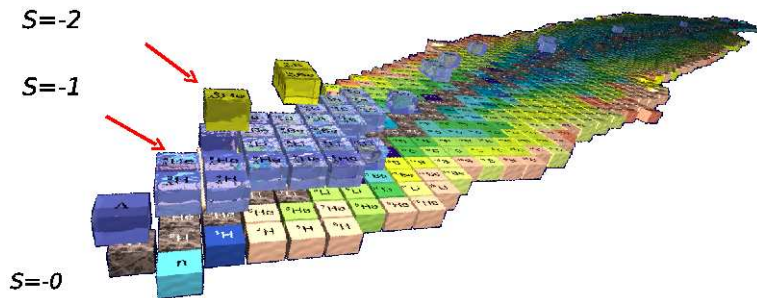
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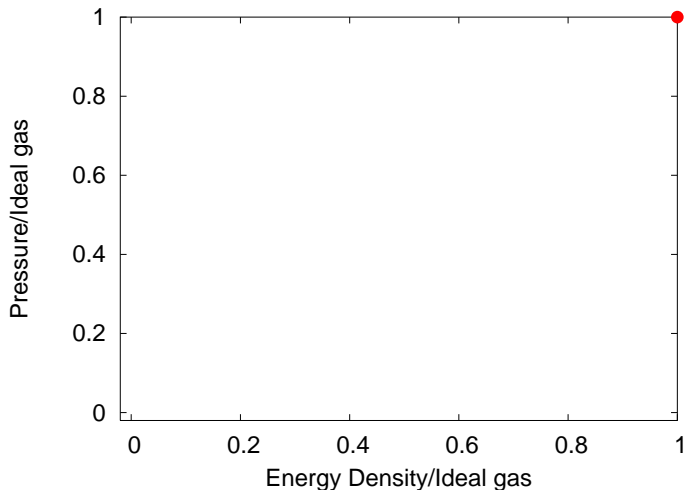
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Nuclear physics: new dimensions



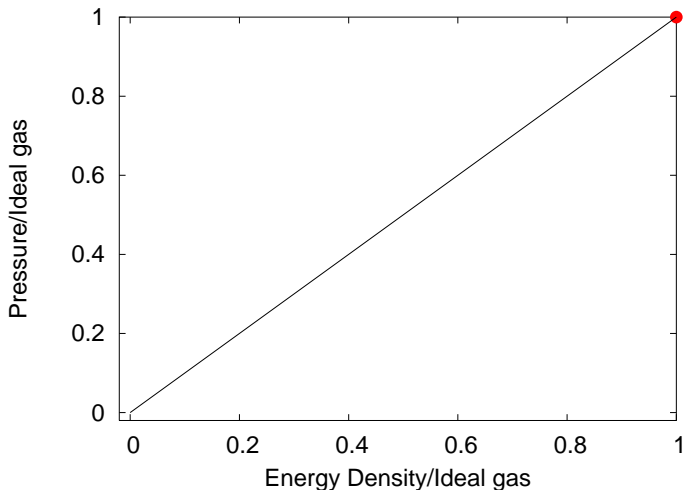
STAR Collaboration, 2009

Equation of state of hot QCD

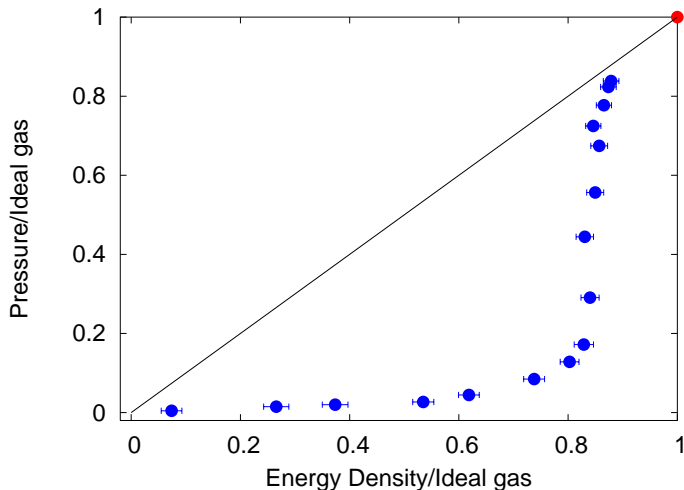


Datta and SG, 2010

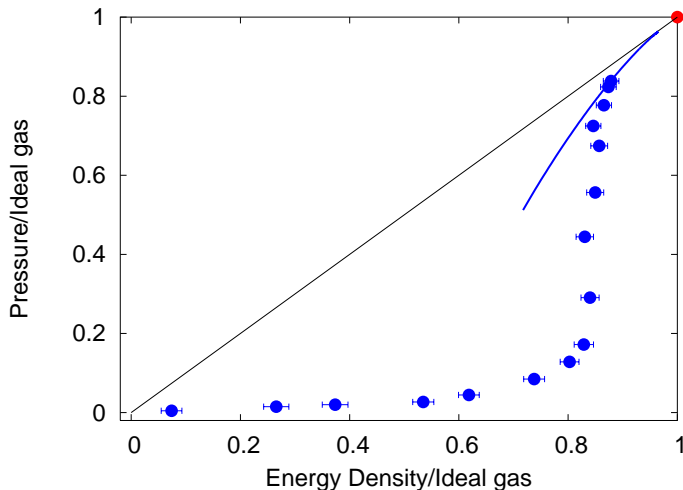
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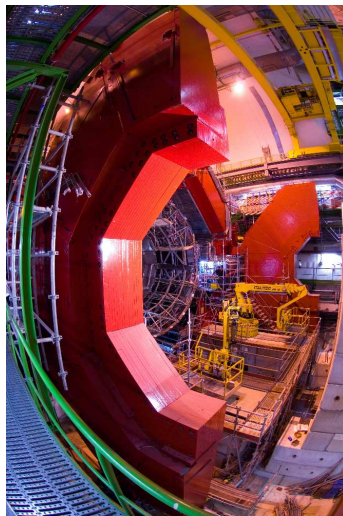
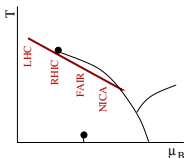
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Hydrodynamics

Matter at long distances and long times almost always obeys hydrodynamics: almost universal theory. More generally: coupled advection-diffusion equations.

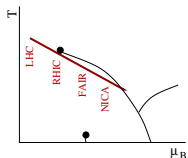
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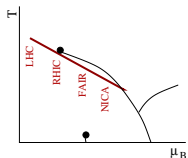
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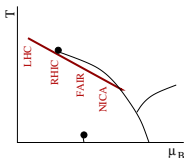
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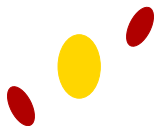
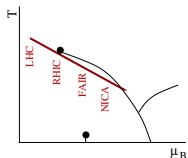
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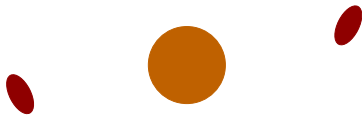
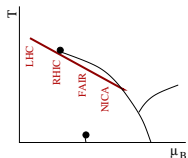
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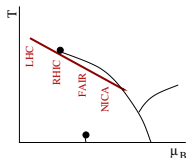
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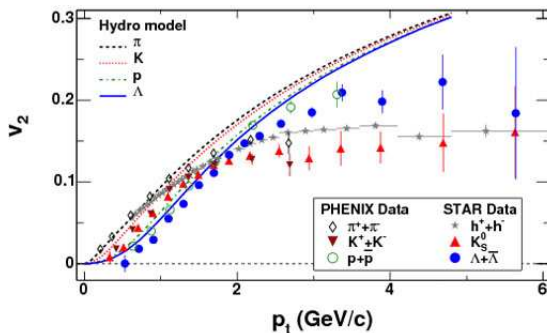
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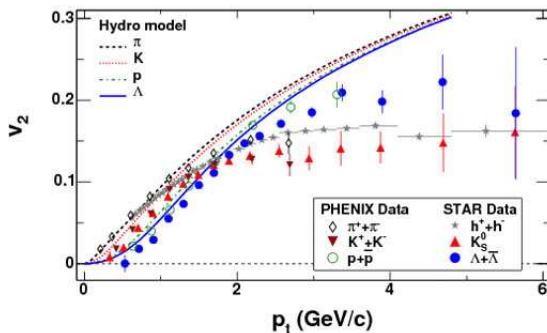


Elliptic flow: hot QCD and cold atoms

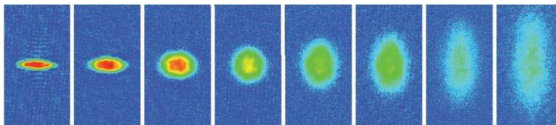


Heinz, 2005.

Elliptic flow: hot QCD and cold atoms



Heinz, 2005.



Extreme viscosity

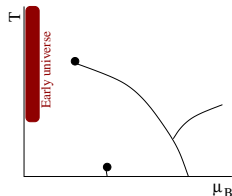
Shear viscosity of different materials cannot be directly compared. Instead compare “kinematic viscosity”: η/n ; relativistically η/S .

This has the same dimension as \hbar/k_B . So $\eta k_B/(S\hbar)$ is dimensionless. How small can it be?

$$\frac{\eta}{S} \times \frac{k_B}{\hbar} \begin{cases} \simeq 0.8 & \text{(liquid He)} \\ \leq 0.5 & \text{(BEC)} \\ \leq 0.5 & \text{(hot QCD)} \end{cases}$$

Danielewics & Gyulassy 1985

Son *et al.*, 2001; Schaeffer, 2010



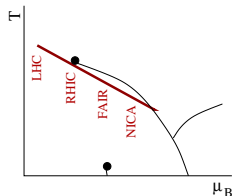
Femtophysics is nanofluidics

Knudsen number is $K = \lambda/L$. When $K \ll 1$ coarse-graining possible. As $K \rightarrow 0$ kinetic theory \rightarrow fluid dynamics.

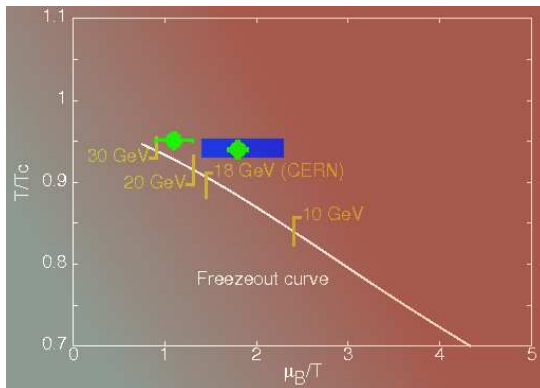
In colliders $\lambda \simeq 0.1\text{--}1$ fm expected. L measured less than 10 fm. Hence $K \simeq 0.1\text{--}1$. Microscopic dynamics may be important: causal viscous fluid dynamics.

Nanofluidics, gas dynamics, neutrino flow in supernovae all have $K \simeq 0.1\text{--}1$.

Bhalerao *et al.* 2005, SG 2005



The critical point



Gavai and SG, 2008

New computational techniques to deal with the long-standing and ubiquitous **sign problem**: QCD, superconductivity, *etc.*
 New experimental program at RHIC to test this prediction of QCD.

Bypassing the sign problem

Taylor expansion of the pressure in μ_B

$$P(T, \mu_B) = \sum_n \frac{1}{n!} \chi^{(n)}(T) \mu_B^n$$

has coefficients that need to be evaluated only at $\mu_B = 0$ where there is no sign problem. The baryon number susceptibility (second derivative of P) has a related Taylor expansion

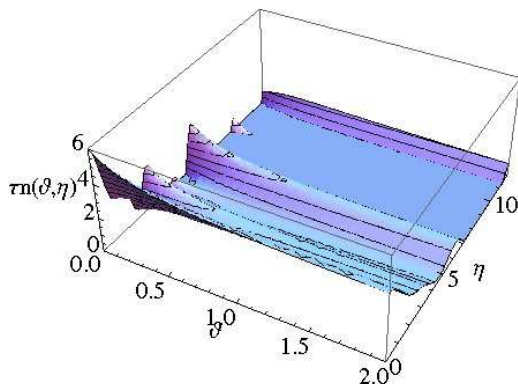
$$\chi_B(T, \mu_B) = \sum_n \frac{1}{n!} \chi^{(n+2)}(T) \mu_B^n.$$

χ_B diverges at the critical point. Series expansion can show signs of divergence. Series resummations can give $P(T, \mu_B)$.

Gavai & SG, 2003, 2005, 2008

The method is perfectly general and can be applied to any theory.

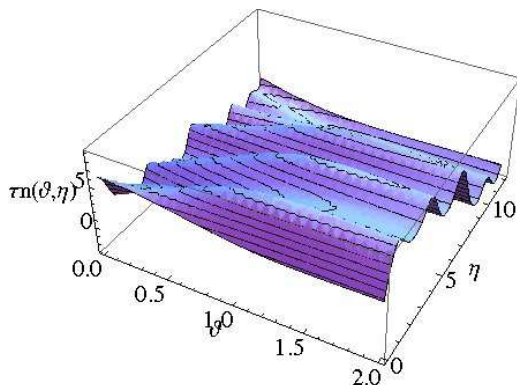
QCD fireball evolution: multiphase nanofluidics



Bhalerao and SG, 2009

Diffusion-advection equations in the limit when $K \simeq 0.1-1$

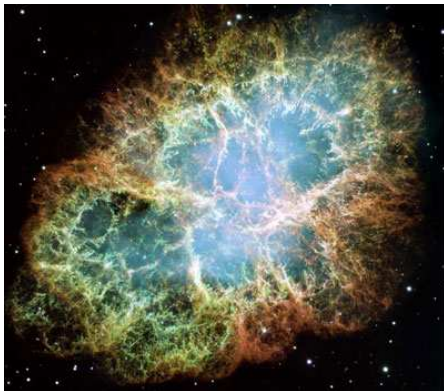
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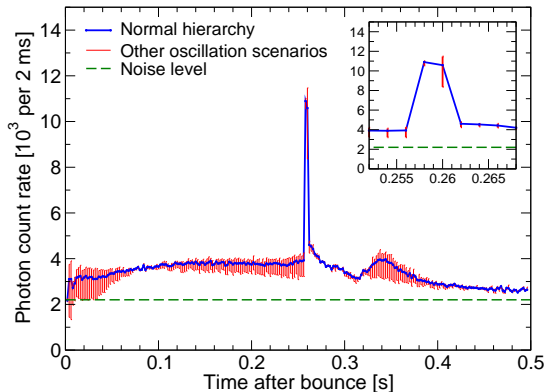
A possible supernova signal



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Dasgupta *et al.*, 2009

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The next $10\sqrt[3]{\frac{1}{3}}$ years

1. The RHIC (Brookhaven), LHC (Geneva), FAIR (Darmstadt), NICA (Dubna) will run for the next 10 years & more. Need international collaborations; long-term detector R&D: collaboration with materials sciences.
2. Install 10s of Teraflops computing capacity in three years, scale to petaflops by end of the XII plan period. Algorithmic challenges. Petabyte data transfer challenge: grid?
3. Hot and dense matter: core theory expertise. Augment with new experimental group; share problems with condensed matter physics. New challenge: transport coefficients.
4. QCD nuclear-astrophysics: expected to develop in 5–7 years.
5. Fluid dynamics: the $K = 1/10$ challenge. Kinetic theory too cumbersome, fluid dynamics too inaccurate. Extend hydrodynamics: many fields, heavy-ions, astro and nano physics. Other fluid dynamics problems.

Beyond



QCD today

