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The Phase Diagram of

**Strongly Interacting Matter** 

Helmut Satz Universität Bielefeld, Germany

based on joint work with Paolo Castorina, Rajiv Gavai and Krzysztof Redlich At sufficiently high temperature or large baryon number density: <u>Limits of Hadronic Matter</u>



- different limit forms in different T,  $\mu$  regions
- does this arise from different hadronic interactions?
- does this lead to different deconfined states of matter?

### **Constituent Structure of Hadronic Matter**



- low  $\mu$ : with increasing T, mesonic medium of increasing density mesons experience attraction  $\rightarrow$  resonance formation mesons are permeable (overlap)  $\rightarrow$  resonances  $\sim$  same size
- low T: with increasing  $\mu$ , baryonic medium of increasing density nucleons experience attraction  $\rightarrow$  formation of nuclei nucleons repel (hard core)  $\rightarrow$  nuclei grow linearly with A

#### In both cases, $\exists$ clustering

∃ relation between clustering and critical behavior? Frenkel 1939 Essam & Fisher1963

consider spin systems, e.g., Ising model

- for H = 0, spontaneous  $Z_2$  symmetry breaking  $\rightarrow$  magnetization transition
- but this can be translated into cluster formation and fusion critical behavior via cluster fusion: percolation ≡ critical behavior via spontaneous symmetry breaking

Fisher 1967, Fortuin & Kasteleyn 1972, Coniglio & Klein 1980

• for  $H \neq 0$ , partition function is analytic, no thermal critical behavior but clustering & percolation persists  $\exists$  geometic critical behavior In spin systems,

 $\exists$  geometric critical behavior for all values of H;

for H = 0, this becomes identical to thermal critical behavior, with non-analytic partition function &  $Z_2$  exponents

for  $H \neq 0$ ,  $\exists$  Kertész line geometric transition with singular cluster behavior & percolation exponents

For spin systems,



### thermal critical behavior $\subset$ geometric critical behavior

Also in QCD? Hadrons have intrinsic size, with increasing density they form clusters & eventually percolate

### Hadron Percolation $\sim$ Color Deconfinement

Pomeranchuk 1951

Baym 1979, Çelik, Karsch & S. 1980

**Recall percolation** 

• 2-d, with overlap: lilies on a pond



• 3-d: N spheres of volume  $V_h$  in box of volume V, with overlap increase density n = N/V until largest cluster spans volume: percolation

critical percolation density  $n_p \simeq 0.34/V_h$ 

at  $n = n_P$ , 30 % of space filled by overlapping spheres, 70 % still empty how dense is the percolating cluster? Digal, Fortunato & S. 2004 critical cluster density  $n_m \simeq 1.2/V_h$ 

$$R_h \simeq 0.8 \text{ fm} \Rightarrow n_m \simeq \frac{0.6}{\text{fm}^3}$$
 as deconfinement density

so far, cluster constituents were allowed arbitrary overlap

what if they have a hard core? percolation for spheres of radius  $R_0$ with a hard core of radius  $R_{hc} = R_0/2$  Kratky 1988 hard cores tend to prevent dense clusters; higher density needed to achieve percolating clusters

$$n_b \simeq rac{2.0}{V_0} = rac{0.25}{V_{hc}} \simeq rac{1.0}{\mathrm{fm}^3} \simeq 6 \, \, \mathrm{n}_0$$

for the deconfinement density of baryonic matter

- $\exists$  two percolation thresholds in strongly interacting matter:
- mesonic matter, full overlap:  $n_m \simeq 0.6/{
  m fm}^3$
- baryonic matter, hard core:  $n_b \simeq 1.0/{\rm fm}^3$ now apply to determine critical behavior

If interactions are resonance dominated, interacting medium  $\equiv$  ideal resonance gas Beth & Uhlenbeck 1937; Dashen, Ma & Bernstein 1969

include all PDG states for  $M \leq 2.5$  GeV, partition function

 $\ln Z(T,\mu,\mu_S,V) = \sum_{\text{mesons i}} \ln Z^i_M(T,V,\mu_S) + \sum_{\text{baryons i}} \ln Z^i_B(T,\mu,\mu_S,V)$ 

for mesonic and baryonic contributions; enforce S = 0

• low baryon-density limit: percolation of overlapping hadrons



baryons included, but hard core effects ignored slow decrease of transition temperature with  $\mu$ , due to associated production • high baryon-density limit: percolation of hard-core baryons density of pointlike baryons

$$n_b^0 = rac{1}{V} iggl( rac{\partial \ T \ln Z_B(T,\mu,V)}{\partial \mu} iggr)$$



combine the two mechanisms: phase diagram of hadronic matter

• low baryon density:

percolation of overlapping hadrons clustering  $\sim$  attraction

• high baryon density: percolation of hard-core baryons



#### NB:

nuclear attraction plus hard-core repulsion  $\rightarrow 1^{st}$  order transition

clustering and percolation can provide a conceptual basis for the limits of hadronic matter in the QCD phase diagram

## What happens beyond the limits?

There are two roads to deconfinement:

- Increase quark density so that several quarks/antiquarks within confinement radius  $\rightarrow$  pairing ambiguous or meaningless.
- Increase temperature so much that gluon screening forbids communication between quarks/antiquarks distance r apart.

Illustration of the second case: heavy Q correlations, <u>quenched</u> QCD Quarks separated by about 1 fm no longer "see" each other for  $T \geq T_c$ 

mesonic matter: when quark density is high enough, gluon screening radius is short enough, so both coincide



baryonic matter?

in hadrons & in hadronic matter  $\exists$  chiral symmetry breaking

 $\Rightarrow$  confined quarks acquire effective mass  $M_q \simeq 300$  MeV effective size  $R_q \simeq R_h/3 \simeq 0.3$  fm through surrounding gluon cloud

what happens at deconfinement? Possible scenarios:

- $\bullet$  plasma of massless quarks and gluons, ground state shift re physical vacuum  $\to$  bag pressure B
- plasma of massive "constituent" quarks, all gluon effects in  $M_q$

"effective" quark?  $\sim$  depends on how you look:

- hadronic distances, soft probes: massive constituent quark (additive quark model)
- sub-hadronic distances, hard probes: bare current quark (deep inelastic scattering)

Origin of constituent quark mass? quark polarizes gluon medium  $\rightarrow$  gluon cloud around quark

 $M_q \sim m_q + \epsilon_g r^3$ 

where  $\epsilon_g$  is the change in energy density of the gluon field due to the presence of the quark

QCD: non-abelian gluon screening limits "visibility" range to  $r_g$ 



 $\rightarrow$  energy density of gluon cloud and screening radius determine "asymptotic" constituent quark mass  $\sim$  gluon cloud

relation to chiral symmetry breaking? estimates from perturbative QCD

Politzer 1976

effective quark mass  $M_q^{ ext{eff}}(r)$  at distance r

$$M_q^{
m eff}(r) = 4 \; g^2(r) \; r^2 \left[ rac{g^2(r)}{g^2(r_0)} 
ight]^{-d} raket{ar{\psi}\psi(r_0)}$$

with reference point  $r_0$  for determination of  $\langle \bar{\psi}\psi(r_0) \rangle$ ; coupling is

$$g^2(r) = rac{16\pi^2}{9} rac{1}{\ln[1/(r^2\Lambda_{
m QCD}^2)]}$$
 for  $N_f=3, \; N_c=3 \; o \; d=4/9$ 

constituent quark mass is defined as solution of

$$M_q = M_q^{
m eff}(r=1/2M_q)$$

giving  $M_q$  in terms of  $r_0$  and  $\langle ar{\psi} \psi(r_0) 
angle$ 

With  $r_0 = 1/2M_q$  (meeting of perturbative and non-perturbative)

$$M_q^3 = egin{cases} rac{16\pi^2}{9} \; rac{1}{\ln(4M_q^2/\Lambda_{QCD}^2)} iggl\} ig\langlear\psi\psi(r_0)
angle$$

and with  $\Lambda_{QCD}=0.2~{
m GeV},~\langlear\psi\psi(r_0)
angle^{1/3}=0.2~{
m GeV}$ 

 $M_q = 375 \,\,{
m MeV}; \quad R_q = 0.26 \,\,{
m fm}$ 

constituent quark mass determined by chiral condensate

how does  $\langle \bar{\psi}\psi(T)\rangle^{1/3}$  change with temperature? gluon cloud evaporates, constituent quark mass vanishes as  $T \to T_c$ 



So there are two ways to make the effective quark mass vanish

- decrease interquark distance
- increase temperature



now consider different  $T - \mu$  regions:

- $\mu \simeq 0, \ T \simeq T_c$ : interquark distance ~ 1 fm but hot medium makes gluon cloud evaporate  $\Rightarrow M_q^{\text{eff}} \simeq 0$
- $T \simeq 0, \ \mu \simeq \mu_c$ : interquark distance ~ 1 fm and cold medium, gluon cloud does not evaporate  $\Rightarrow M_q^{\text{eff}} \simeq M_q$

in cold dense matter,  $M_q^{\rm eff} \rightarrow 0$  requires short interquark distance  $\sim$  constituent quark percolation

intermediate massive quark plasma for 0.3 < r < 1 fm and  $T \lesssim T_c$ 



color deconfinement, but chiral symmetry remains broken; constituents: massive colored quarks, gluons only as quark dressing

baryon density limit through quark percolation  $n_b^c \simeq 3.5 \text{ fm}^{-3}$ 

- nuclear matter  $n_b \leq 0.9 \ {\rm fm}^{-3}$
- quark plasma 0.9  ${\rm fm}^{-3} \le n_b \le 3.5 ~{\rm fm}^{-3}$
- quark-gluon plasma  $n_b \geq 3.5 ~{
  m fm}^{-3}$



Nature of massive quark plasma

- massive quarks and (at higher T) some massive antiquarks - no gluons, "chiral pions"?

no color confinement, but colored bound states possible

anti-triplet qq bound states = diquarks

(genuine two-body states, not Cooper pairs)

attractive interaction for  $qq \rightarrow \text{color anti-triplet},$   $q\bar{q} \rightarrow \text{color singlet},$ with same functional form of potential in r, T



Bielefeld Lattice Group 2002

constituent quark plasma can be structurally similar to hadron gas:

- massive quarks
- (antitriplet) diquark and (singlet)  $q\bar{q}$  states
- higher excitations (colored resonance gas)
- also possible: glueballs, chiral pions
- $\bullet$  all states have intrinsic finite size, hence  $\exists$  percolation limit



- $\Rightarrow$  Three State Phase Diagram (modulo color superconductor)
  - Hadronic matter at low  $T, \mu$ : quarks and gluons confined to hadrons, broken chiral symmetry
  - Quark plasma at low T, large(r)  $\mu$ : massive deconfined quarks, broken chiral symmetry
  - Quark-gluon plasma at large  $T, \mu$ : deconfined massless quarks and gluons, restored chiral symmetry

# Back-Up

quark plasma has effective color degrees of freedom

- hadron gas:  $d_{
  m eff} = 1$
- ullet massive quark plasma:  $d_{
  m eff}=N_c$
- ullet quark-gluon plasma:  $d_{
  m eff}=N_c^2$

relation to quarkyonic matter? McLerran & Pisarski 2007 phase structure of QCD for  $N_c \to \infty$ :

• confined hadronic matter is purely mesonic,

since  $n_b \sim \exp\{(\mu - M)\}$ , and  $\mu$ ,  $M \sim N_c$ .

• quark-gluon plasma becomes gluon plasma,

since gluon sector  $\sim N_c^2$ , quark sector  $\sim N_c$ .

• quarkyonic matter proposed to have

color degrees of freedom  $\sim N_c$ , hence no "free" gluons.

• quark plasma, with  $n_q \sim N_c (\mu_q^2 - M_q^2)$ , contracted to  $\mu_q = M_q$ .



