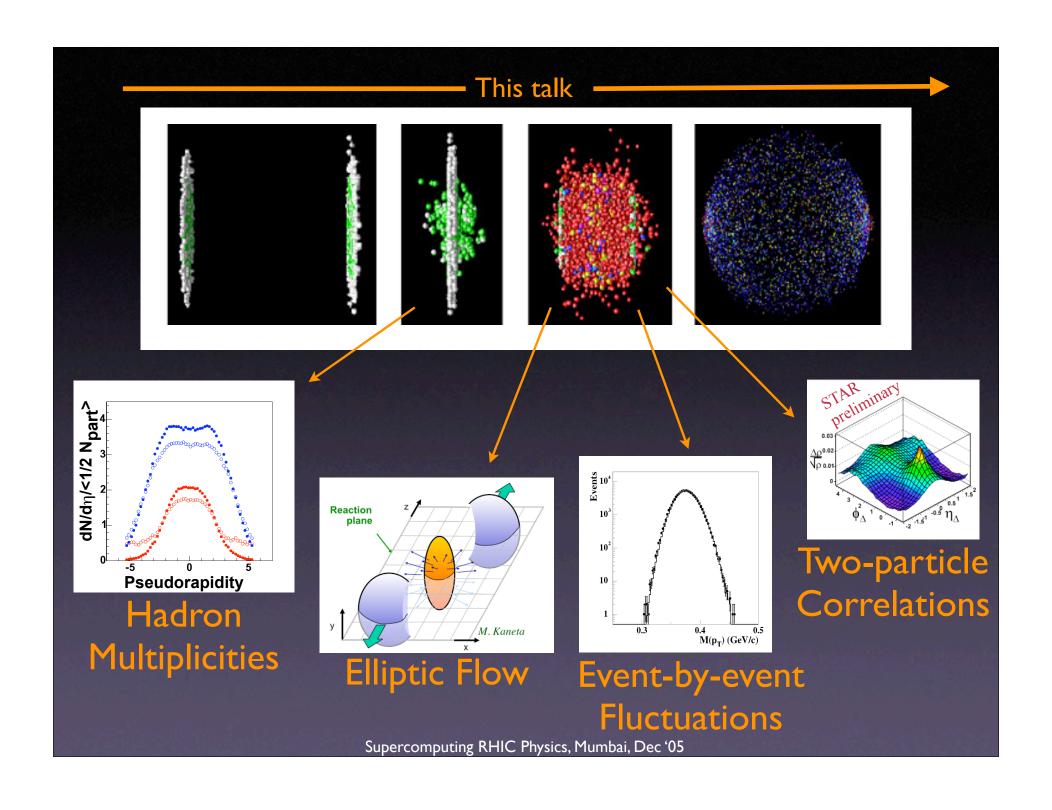
# Correlations and Fluctuations in Nuclear Collisions

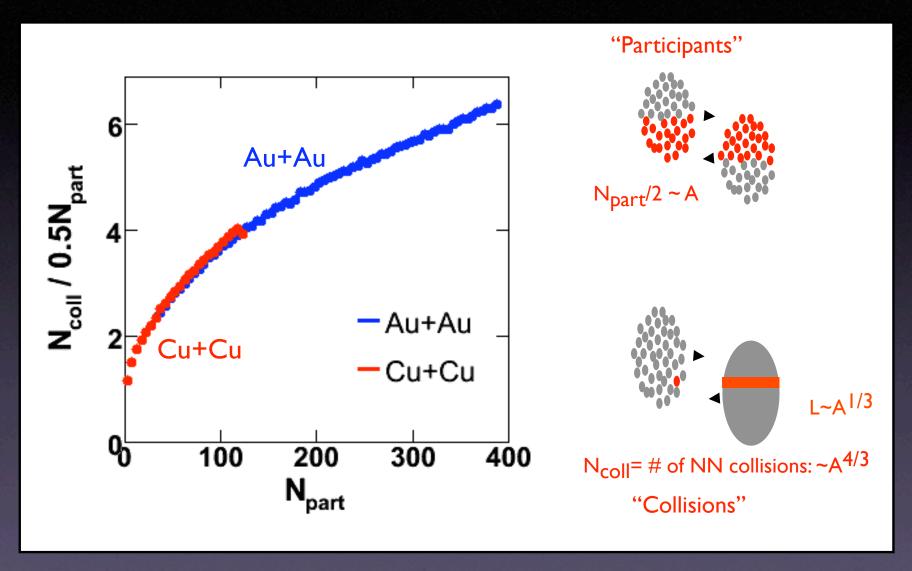
Experimental Overview

Gunther Roland - MIT

Supercomputing RHIC Physics
TIFR, Mumbai
Dec 5-9 2005

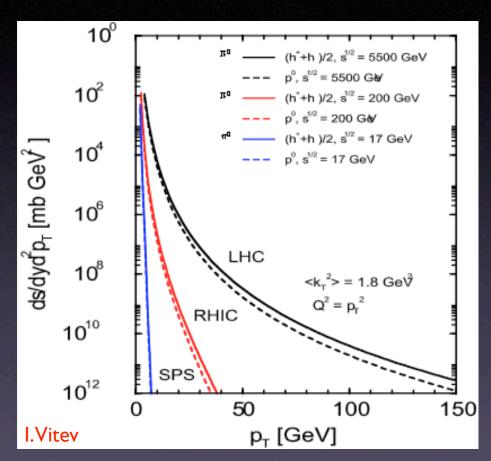


#### Pre-requisites: Centrality Characterization

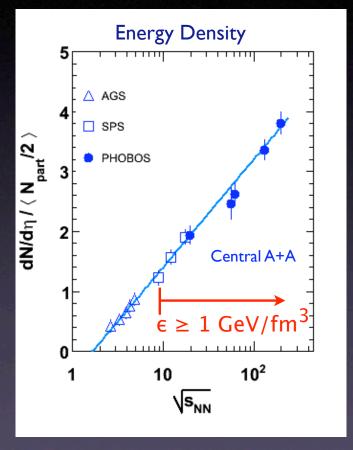


Number of participating nucleons from Glauber MC

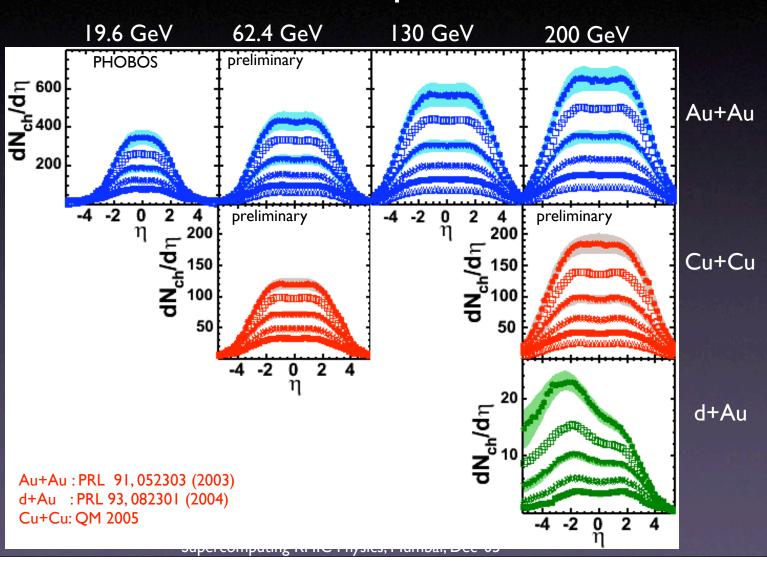
#### Pre-requisites: Hard vs Soft Hadron Production

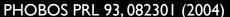


Fast rise of high p<sub>T</sub> yields from hard collisions

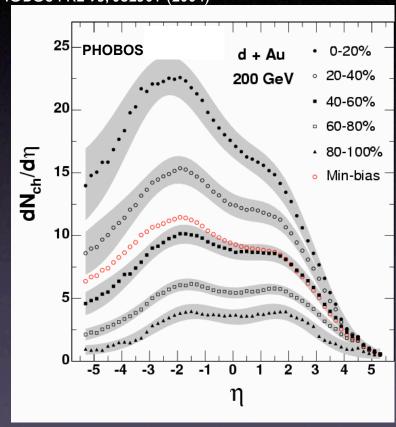


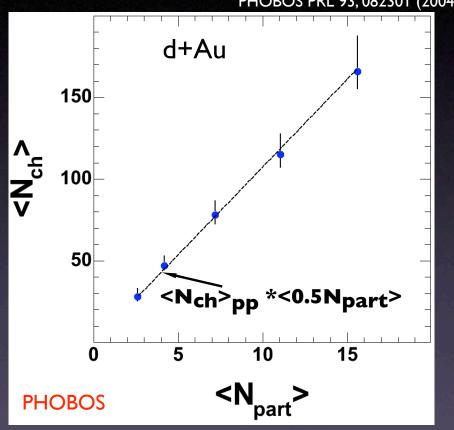
Logarithmic rise of particle (≈energy) density









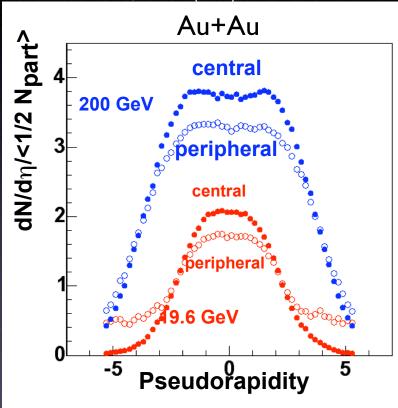


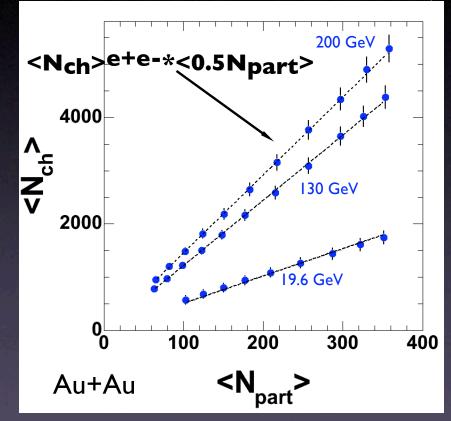
Shape changes dramatically versus centrality

Multiplicity per participant is constant

PHOBOS PRL 91, 052303 (2003)

PHOBOS PRL 91, 052303 (2003)

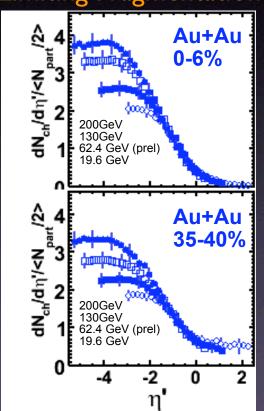




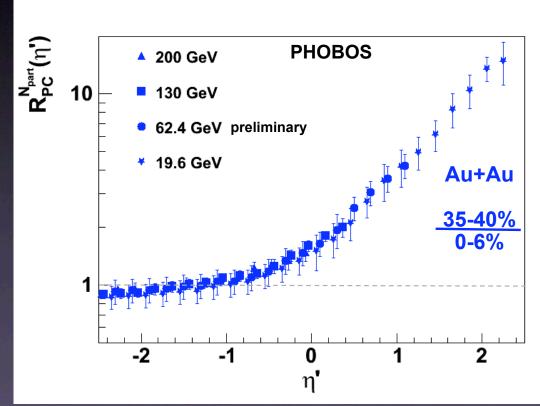
Shape changes dramatically versus centrality

Multiplicity per participant is constant

Limiting Fragmentation

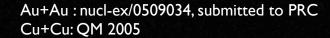


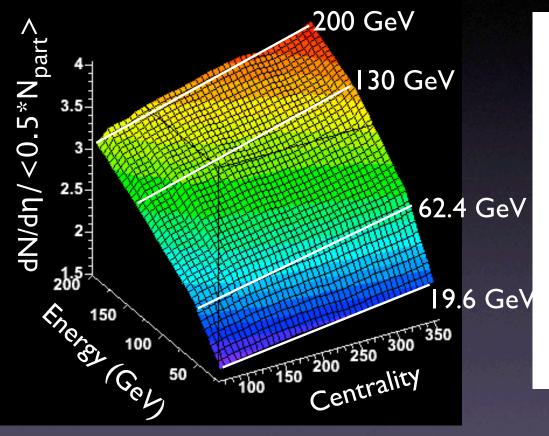
Ratio of 0-6% and 35-40% centrality bins, each normalized by N<sub>part</sub>

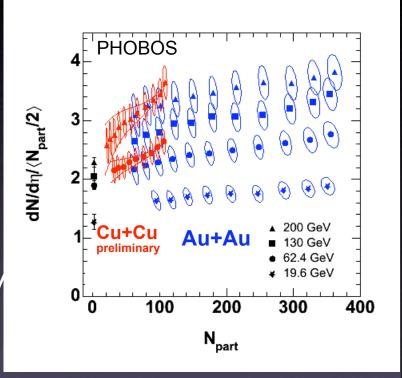


Shape change of longitudinal distributions is energy independent

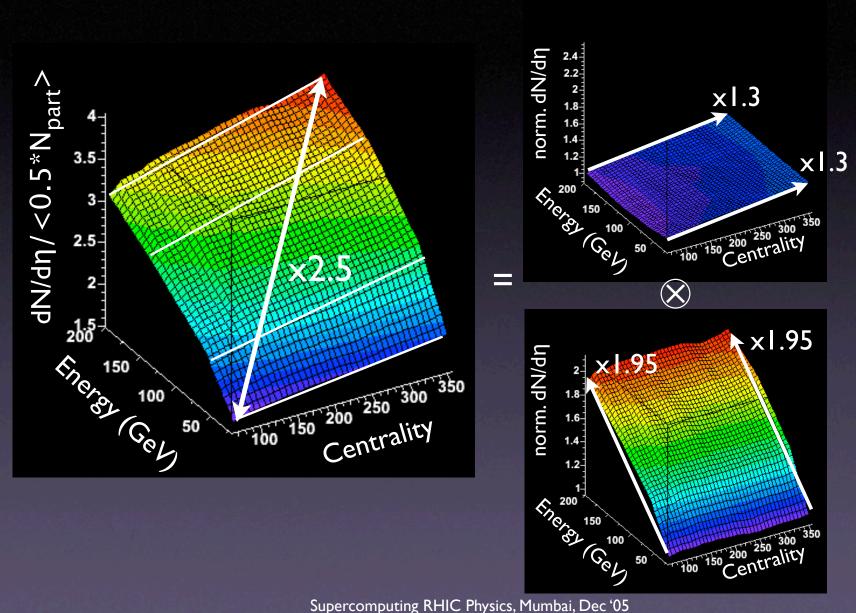
## Mid-rapidity dN/dη vs √s and N<sub>part</sub>

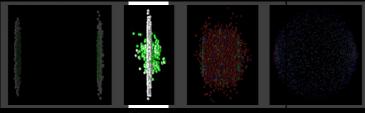




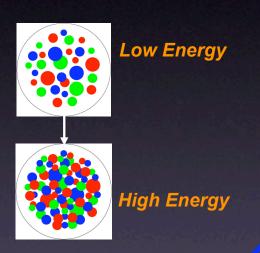








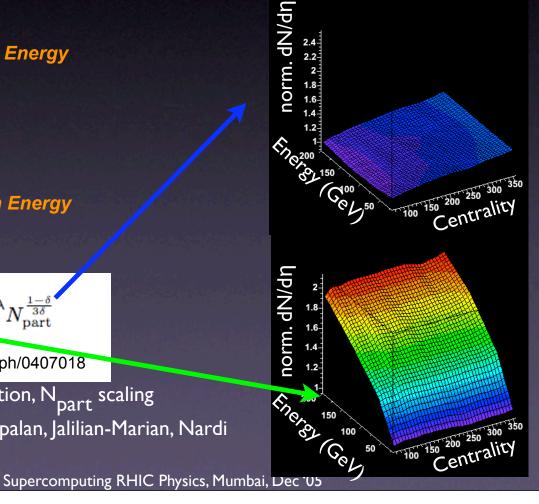
Initial State
Parton Saturation

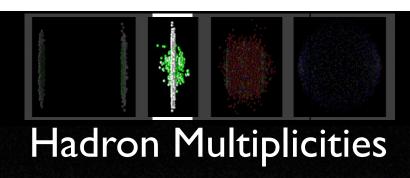


$$\left. rac{1}{N_{
m part}} rac{dN^{AA}}{d\eta} 
ight|_{\eta \sim 0} = N_0 \sqrt{s}^{\lambda} N_{
m part}^{rac{1-\delta}{3\delta}}$$

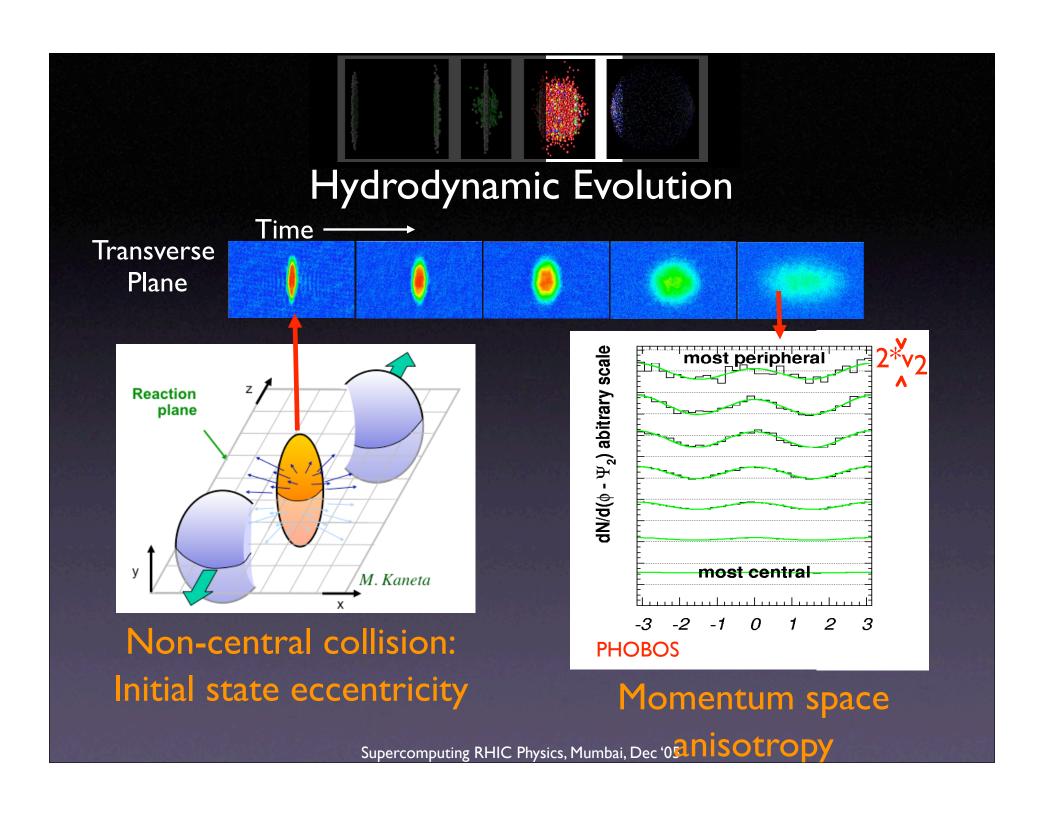
Armesto, Salgado, Wiedemann hep-ph/0407018

Also limiting fragmentation, N<sub>part</sub> scaling (c.f. Kharzeev, McLerran, Venugopalan, Jalilian-Marian, Nardiet al)

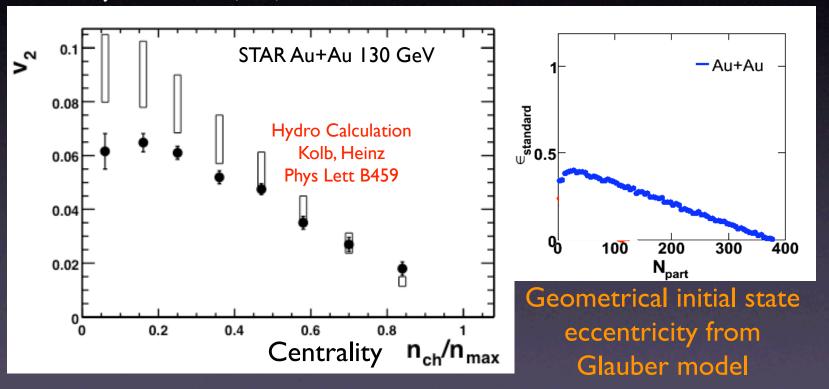




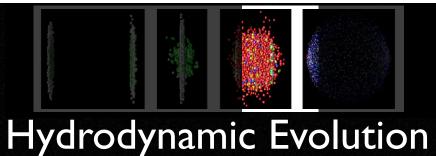
- Participant scaling of total multiplicities
  - Global constraints over full η range
- Slow growth of multiplicity with energy
  - Saturation + LPHD?
- Factorization of energy/centrality dependence
  - Saturation +LPHD?
- No modification during expansion/hadronization/recscattering?



Phys. Rev. Lett. 86 (2001) 402



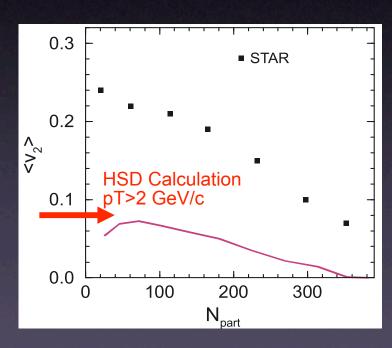
Elliptic Flow signal exhausts "hydro limit" for mid-central to central collisions



#### Parton Cascade

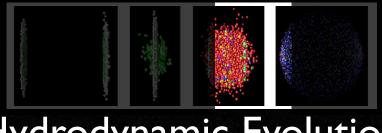
# 0.2 What STAR prelim. (Filimonov, Nov '01) $dN_g/d\eta_{cent} = 1000$ $\sigma_{el} \approx 45 \text{ mb}$ $\sigma_{el} \approx 8 \text{ mb}$ 0.05 $\sigma_{el} \approx 8 \text{ mb}$ MPC Au+Au @ 130A GeV duality $\sigma_{el} \approx 8 \text{ mb}$ $\sigma_{el} \approx 8 \text{ mb}$ Oncompare the state of the parton-hadron duality duality

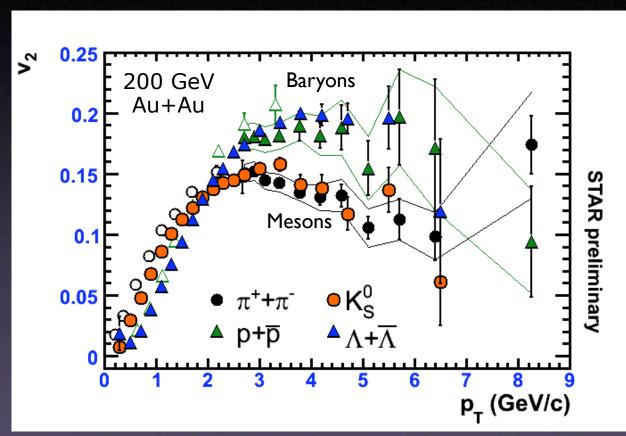
#### Hadron Cascade



Cassing et al

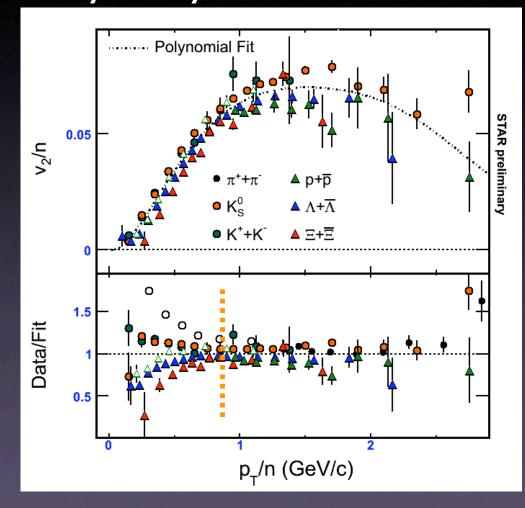
Neither partonic nor hadronic cascades reproduce flow





PHENIX (open symbols): Phys. Rev. Lett. **91**, 182301 (2003)

Rich structure vs mass (?) and pT

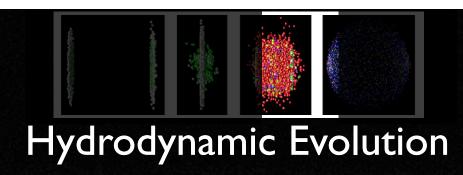


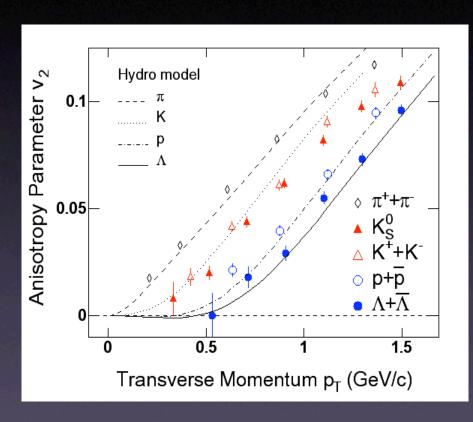
PHENIX (open symbols): Phys. Rev. Lett. **91**, 182301 (2003)

Quark-number scaling

Mass scaling

M. Oldenburg, STAR, QM2005

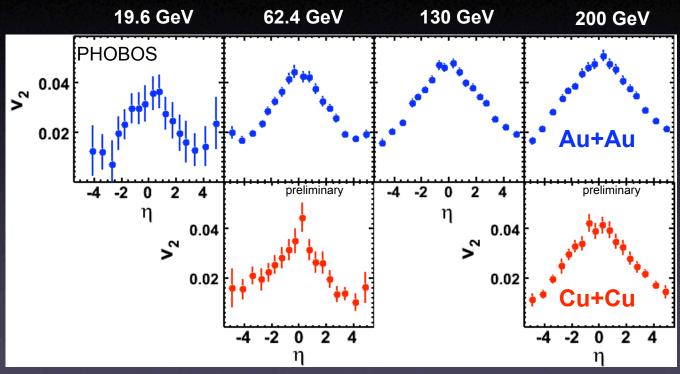




200 GeV Au+Au Data: STAR, PHENIX

Hydro: P. Huovinen et al., Phys. Lett. B503, 58 (2001)

Mass splitting at low p<sub>T</sub> understood in hydro calculations



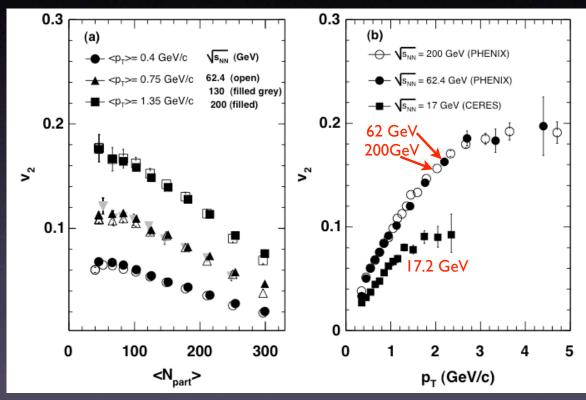
Strong rapidity dependence of elliptic flow Challenge to hydrodynamic calculations Connection between flow and  $dN/d\eta$ 

Au+Au: PHOBOS PRL 94 122303 (2005)

Cu+Cu: PHOBOS QM 2005

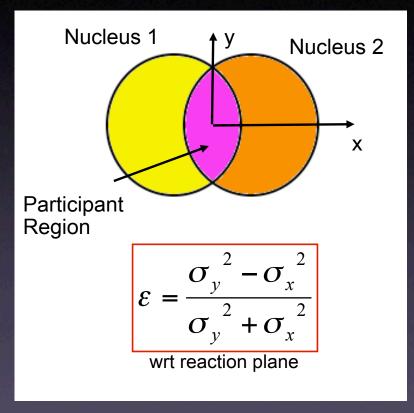


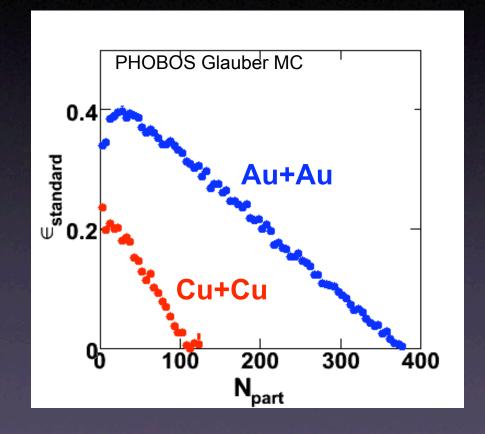
PHENIX nucl-ex/0411040



Saturation of  $v_2(p_T)$  above  $\sqrt{s} \approx 62$  GeV



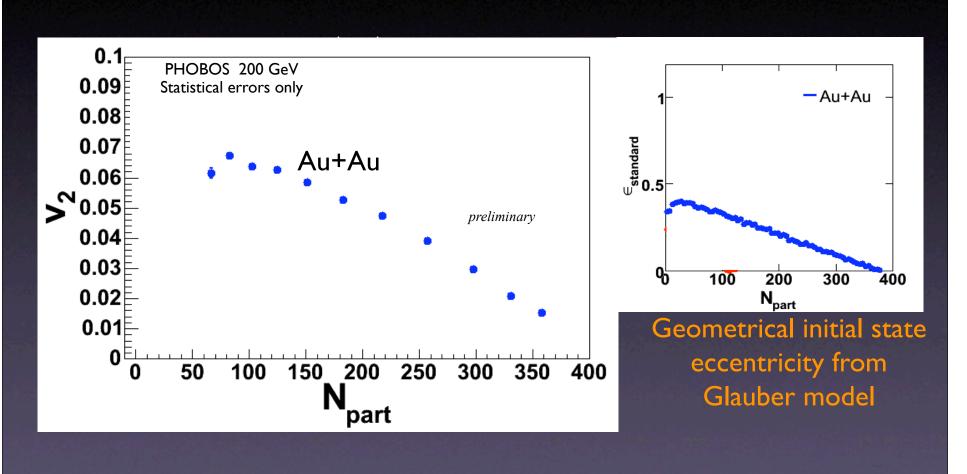




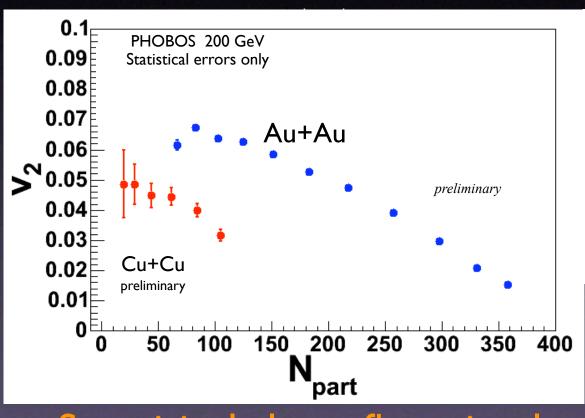
#### Au+Au vs Cu+Cu

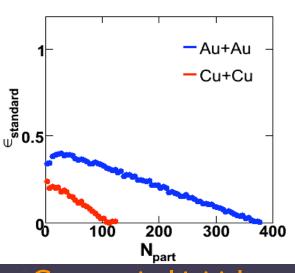
Interplay of initial geometry and initial density Test ideas of early thermalization and collectivity





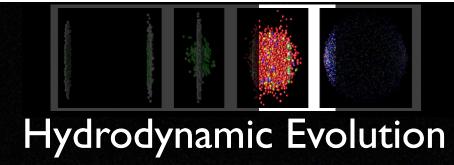






Geometrical initial state eccentricity from Glauber model

Surprisingly large flow signal in Cu+Cu!



Signature of AuAu collision

Nucleus B

Ox2

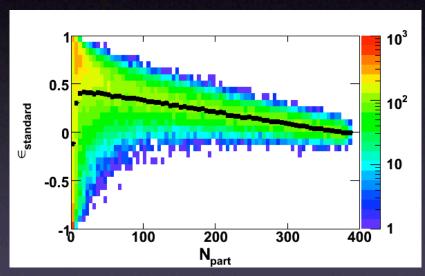
Description of AuAu collision

Participant Nucleons

Using the impact parameter as the x-axis, we define the standard eccentricity using the widths of the distribution in x and y

$$\varepsilon = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2}$$

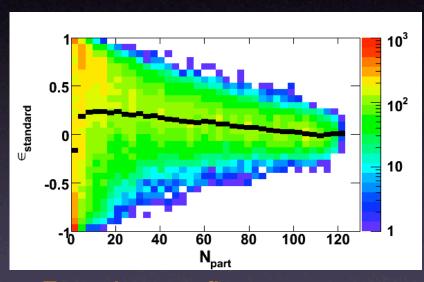
Au+Au



Large fluctuations in eccentricity

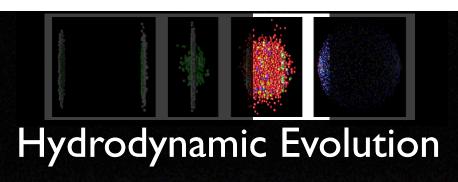
Many peripheral events with negative eccentricity

Cu+Cu

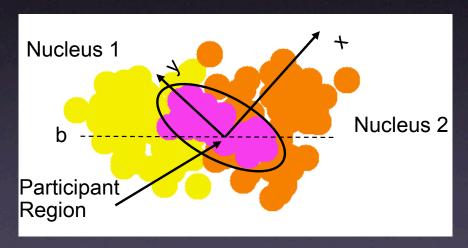


Even bigger fluctuations in Cu+Cu

Glauber MC Calculations

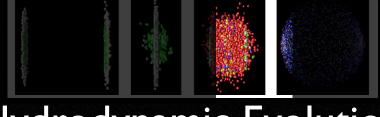


Possibly reasonable method is to realign the coordinate system to maximize the ellipsoidal shape (a principal axis transformation)

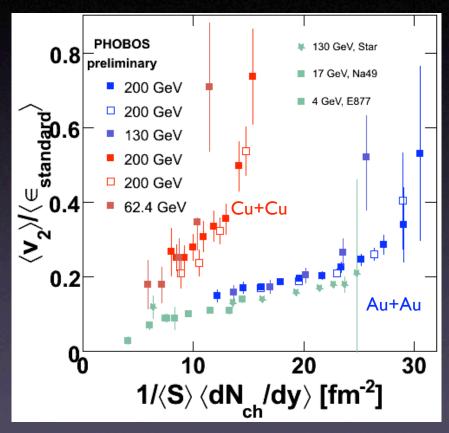


"Participant" eccentricity

(versus "standard" eccentricity)





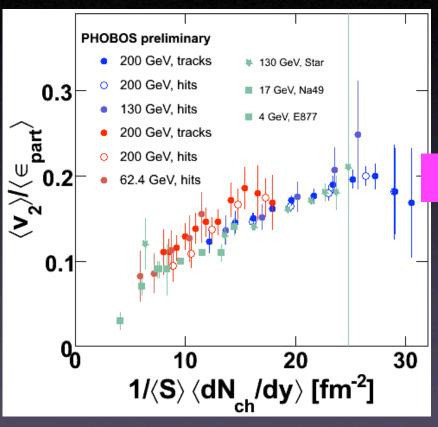


Low Density Limit: STAR, PRC 66 034904 (2002) Voloshin, Poskanzer, PLB 474 27 (2000) Heiselberg, Levy, PRC 59 2716, (1999)

Surprisingly strong elliptic flow in Cu+Cu Challenge to hydrodynamic picture??

Cu+Cu: PHOBOS QM 2005

using
"Participant"
Eccentricity

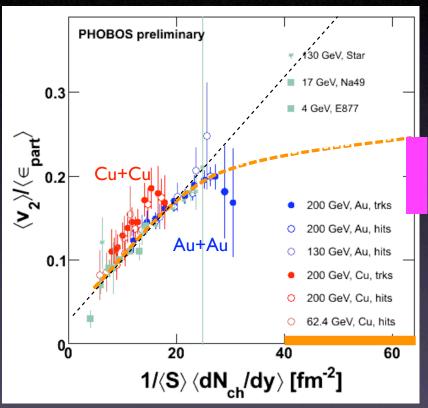


Low Density Limit: STAR, PRC 66 034904 (2002) Voloshin, Poskanzer, PLB 474 27 (2000) Heiselberg, Levy, PRC 59 2716, (1999)

"Hydro-Limit"

"Participant Eccentricity" provides universal scaling Approach to equilibrium?

Cu+Cu: PHOBOS QM 2005

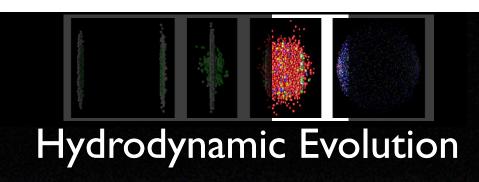


Low Density Limit: STAR, PRC 66 034904 (2002) Voloshin, Poskanzer, PLB 474 27 (2000) Heiselberg, Levy, PRC 59 2716, (1999)

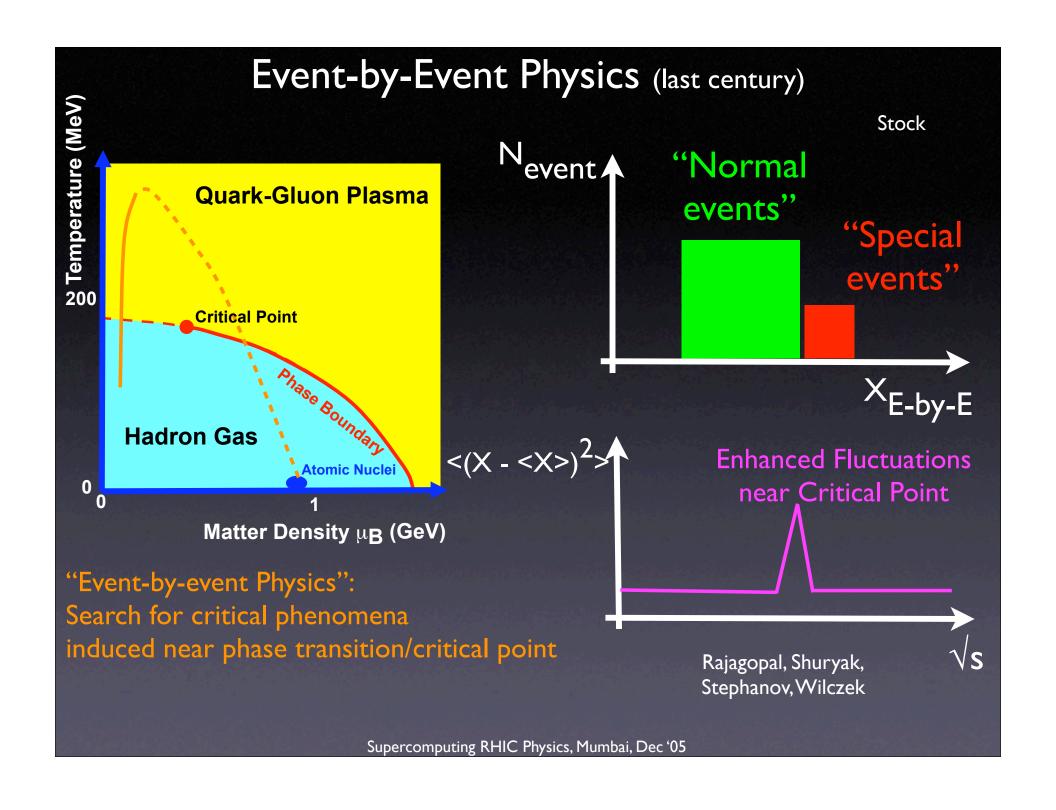
LHC

Will flow saturate at LHC as thermalization is achieved?

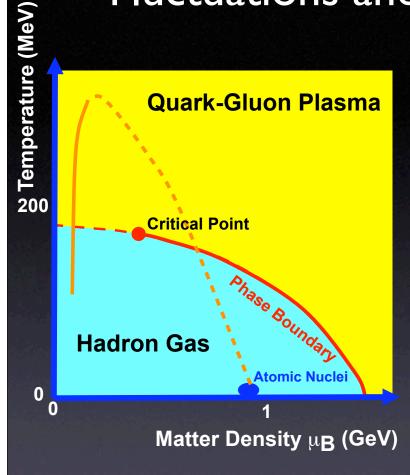
Cu+Cu: PHOBOS QM 2005



- Large collective flow signal observed in Au+Au
- Overall magnitude + mass splitting ≈ hydro
- Additional (geometrical?) azimuthal correlations in Cu+Cu
- How is thermalization/pressure build-up achieved?
- What are the (early) degrees of freedom?



#### Fluctuations and the QCD Phase Diagram



- Phase transition/Latent heat
  - Supercooling

Mishustin

- Droplet Formation
- <pT>, Multiplicity Fluctuations
- Location of critical point
  - <pT> Fluctuations

Rajagopal, Shuryak, Stephanov, Wilczek

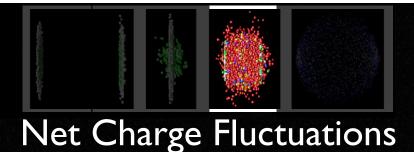
- Deconfinement
  - Charge/DoF

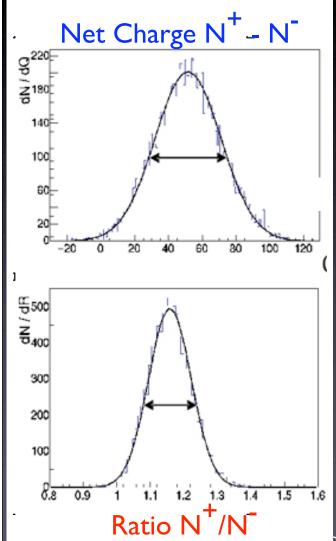
Jeon, Koch Asakawa, Heinz, Mueller

- Charge Fluctuations
- Chiral Symmetry Restoration
  - DCC formation

Rajagopal, Wilczek Bjorken

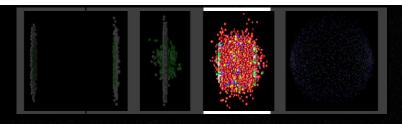
Charge/neutral fluctuations





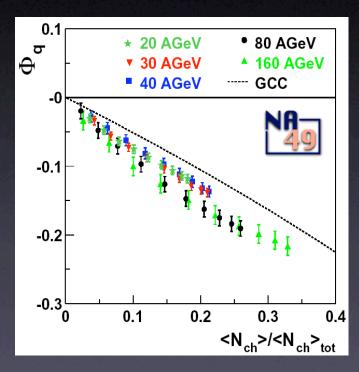
- Net Charge/∆y Fluctuations <-> Charge/DoF
- Jeon, Koch hep-ph/0003168
- Asakawa, Heinz, Mueller hep/ph/0003169
- Change from 1-2 (QGP) to 4 (Pion Gas)

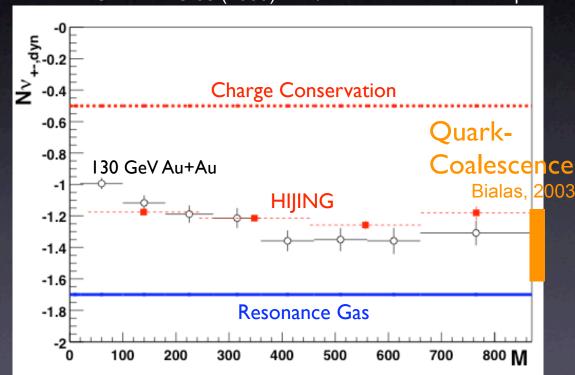
- Fluctuations frozen b/c charge conservation
- Diffusion vs Expansion timescale
- Fluctuations of N<sup>+</sup>/N<sup>-</sup> or N<sup>+</sup>- N<sup>-</sup> vs statistical reference

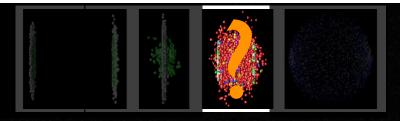


#### Net Charge Fluctuations

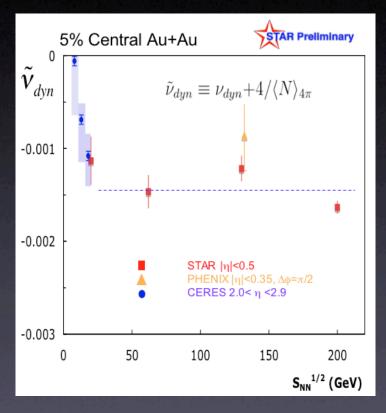




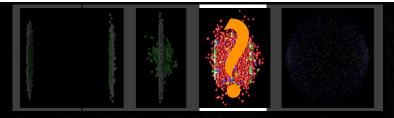




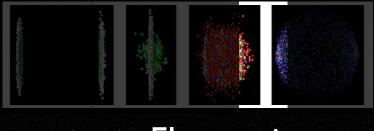
#### Net Charge Fluctuations vs $\sqrt{s}$







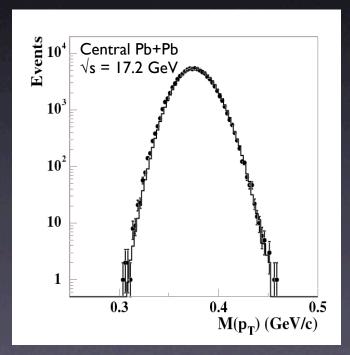
- Basic argument still appears valid
- Possible Explanations
  - Diffusion in long-lived hadronic phase?
  - Resonances?
  - A feature of hadronization?
  - Quark Coalescence?
  - Bound states?
- Need connection to other data and QCD



# T > Fluctuations

- p<sub>T</sub> simple observable (supposedly...)
- High statistical precision:
  - $\sigma_{pT}/<pT>_{inc}< 0.1%$
- Sensitive to many interesting scenarios
  - Critical Point
  - DCC production
  - Droplet formation
  - Any non-statistical, momentum-localized process

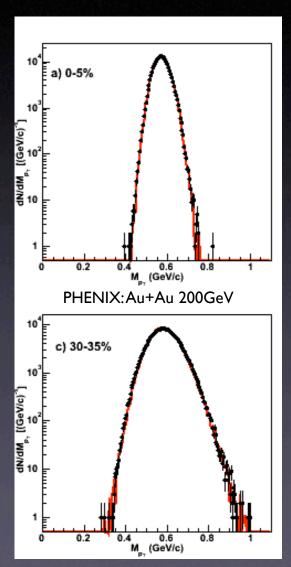
NA49, Phys Lett B459 (1999) 679

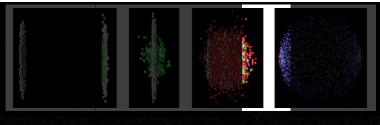


Event-by-event <p\_T > compared to stochastic reference (mixed events)

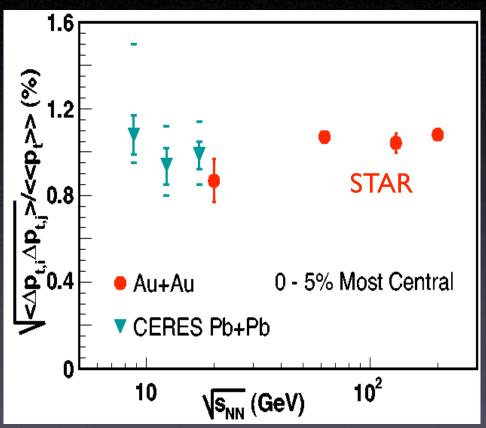
# T > Fluctuations

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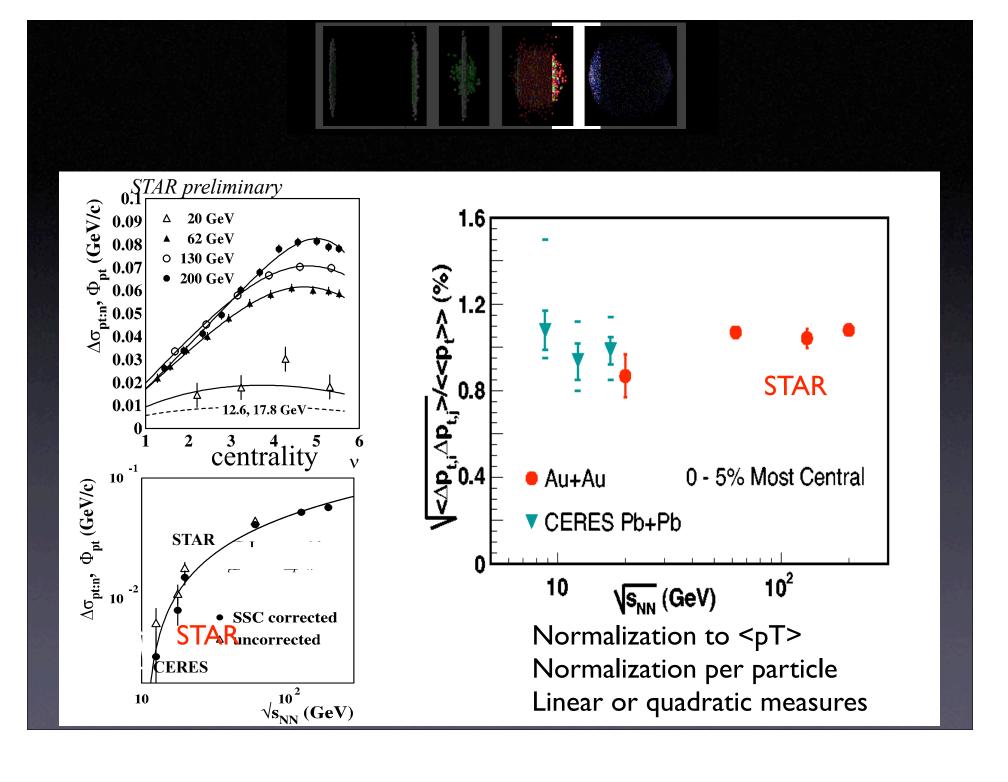




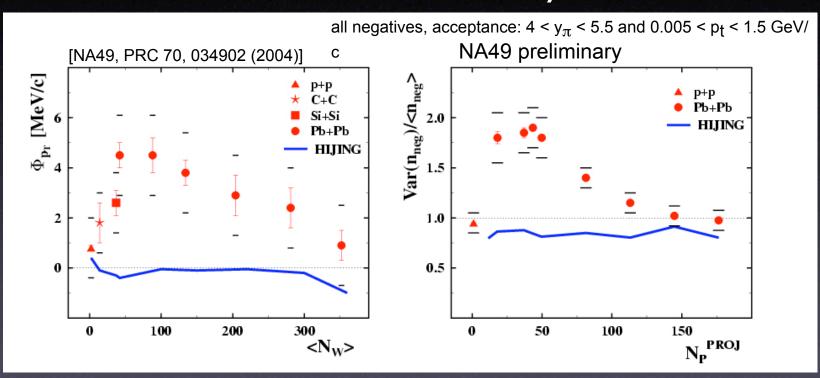
#### **Energy Dependence?**



No evidence for non-monotonic energy dependence
But: Interpretation ⇔ choice of variables
Non-monotonic system-size dependence
Supercomputing KHIC Physics, Mumbai, Dec '05

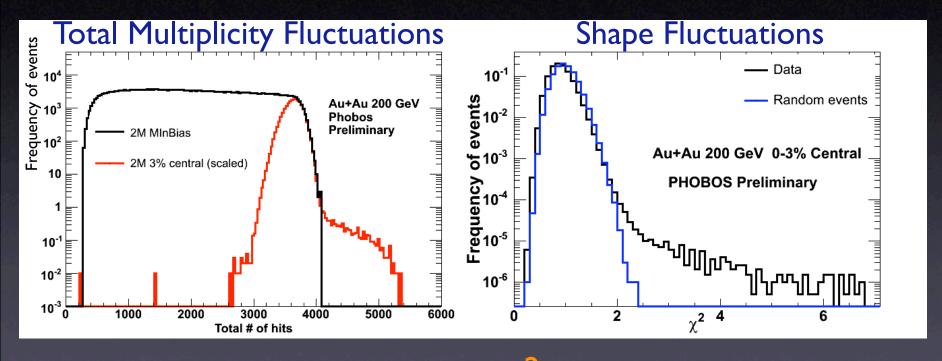


#### Fluctuations for small systems

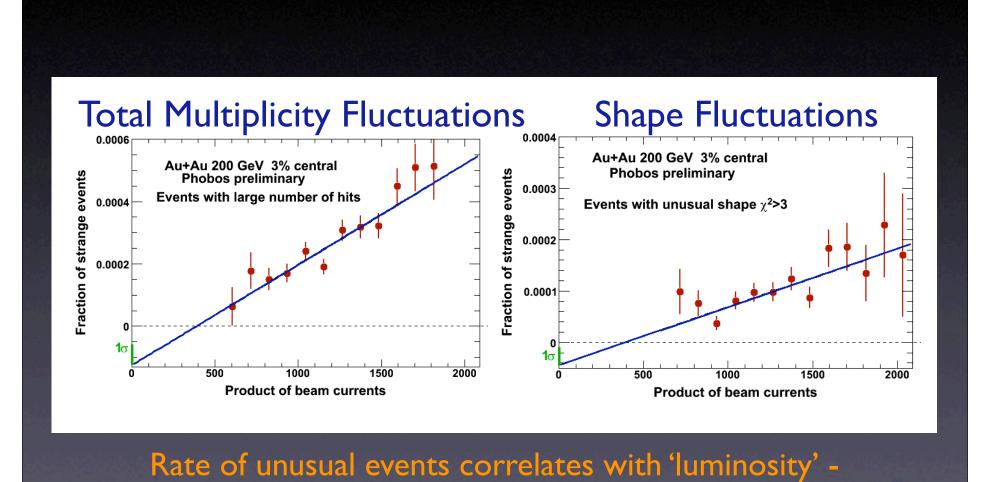


- Fluctuations and Percolation (Clustering) in small systems
- Connection to elliptic flow in Cu+Cu?
- Connection to strangeness enhancement vs N<sub>part</sub>?

#### Search for "unusual" events in Au+Au



Multiplicity distribution and  $\chi^2$  (shape) distribution shows distinct tails - O(10<sup>-4</sup>)

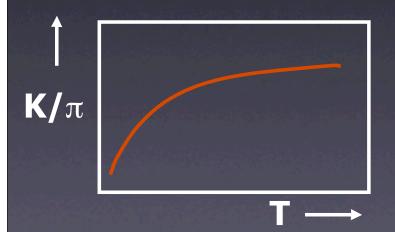


Consistent with collision-pileup as source of rare events

Supercomputing RHIC Physics, Mumbai, Dec '05

#### E-by-E fluctuations in the $K/\pi$ ratio

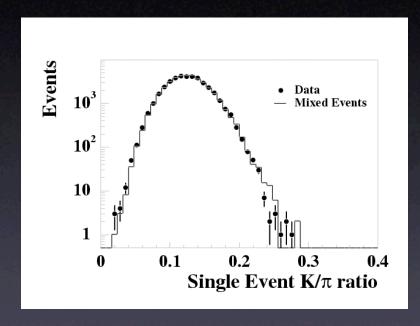
- Is strangeness enhanced in every event?
- Can we see signs of super-cooling below T<sub>crit</sub>?



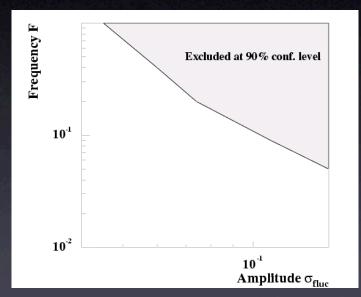
#### NA49 Measurement

- Use dE/dx to identify  $\pi$ , K,p event-by-event
- Do Max Likelihood fit to extract  $K/\pi$  ratio event-by-event
- Required 2 years of detector calibation to eliminate dE/dx multiplicity correlation

#### E-by-E fluctuations in the $K/\pi$ ratio



Pb+Pb, 17.2 GeV NA49, PRL 86 (2001) 1965



- Dynamical fluctuations are small ( < ~5%)</li>
- Compatible with resonance gas (Jeon, Koch; nuclth/9906074)
- Strangeness enhancement in every event
- · Chemical freeze-out at same T in every event

Supercomputing RHIC Physics, Mumbai, Dec '05

#### NA49 'Horn' Strangeness Fluctuations vs √s **♦** 0.06 NA49 (QM'04) Dynamical Fluctuations [%] 10 0.02 $(K^{+} + K^{-})/(\pi^{+} + \pi^{-})$ <**Κ**<sup>†</sup>/<π<sup>†</sup> 0 • Data mixed events To<sub>3</sub> • UrQMD v1.3 data 0.2 $\sigma_{data} = 17.78\%$ σ<sub>mixed</sub> = 17.23% 0.1 10<sup>2</sup> ∴ 0.2∴ 0.15∴ 0.15 preliminary 10 0.1 20 15 0.05 sqrt(s) 0.04 0.06 0.08 0 0 10<sup>2</sup> \s<sub>NN</sub> (GeV) 10 Fluctuations in K/pi ratio

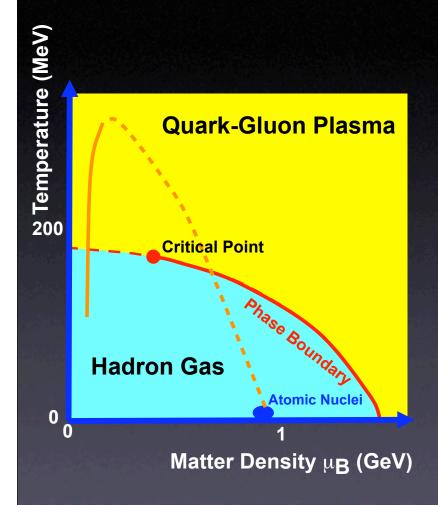
Rajagopal, Stephanov: Compatible with constant correlation strength

Supercomputing RHIC Physics, Mumbai, Dec '05

**Event-by-Event fluctuations** 

- p<sub>T</sub> fluctuations show 'smooth' √s dependence
  - no 20, 30 GeV data yet
- Fluctuations small in central events at top SPS energy + above
- Energy dependence of k/pi fluctuations?
- Multiplicity + p<sub>T</sub> fluctuations for peripheral events?

#### Fluctuations at RHIC



#### **RHIC**

Close to  $\mu_B \sim 0$  axis Cross-over? Far from critical point?

=>Fluctuations not induced by phase-change itself?

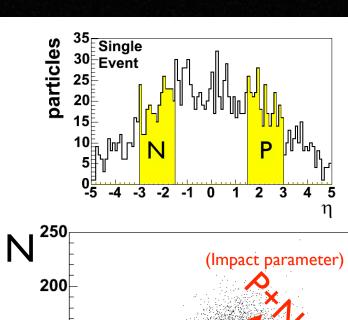
## An Evolving Paradigm

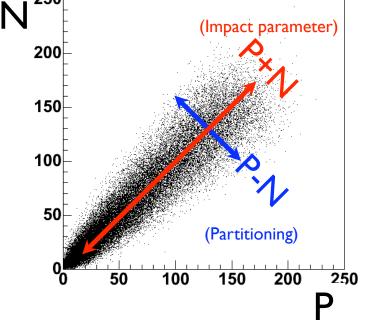
- Event-by-Event Physics
  - Critical phenomena (1990s)
  - Fluctuations of conserved quantities (2000)
- Fluctuations and Correlations
  - Connection between correlations and fluctuations (Koch, Bialas '98)
    - Study transport properties of the medium
    - Approach to thermalization
    - Properties of Hadronization



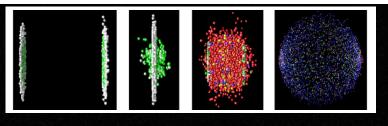
$$C = \frac{P - N}{\sqrt{P + N}}$$

Use variance  $\sigma^2$ 

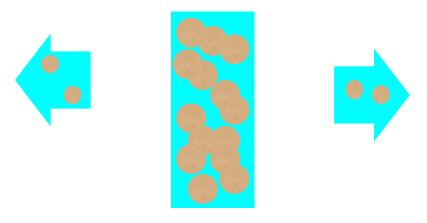




Supercomputing RHIC Physics, Mum



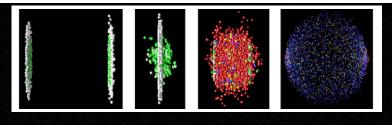
# Clusters and $\sigma^2$ C



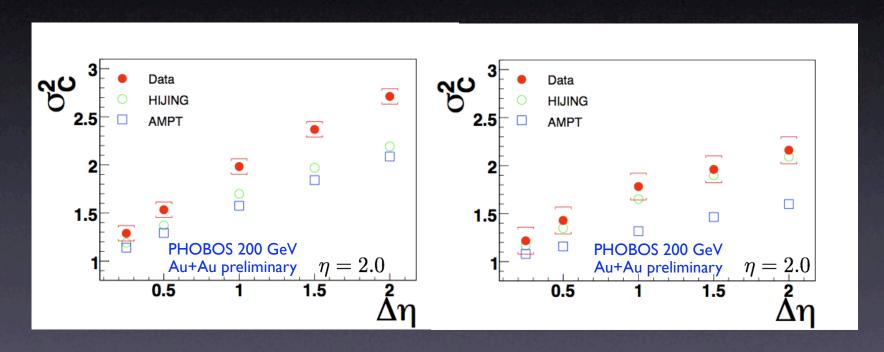
$$P o KP$$
 
$$C(\eta, \Delta \eta) = \frac{P - N}{\sqrt{P + N}} \quad C \to \sqrt{K}C$$
 
$$\sigma_C^2 \to K\sigma_C^2$$

Forward/backward correlations give access to <u>cluster structure</u> of particle production

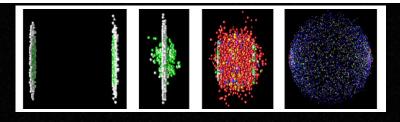
Supercomputing RHIC Physics, Mumbai, Dec '05



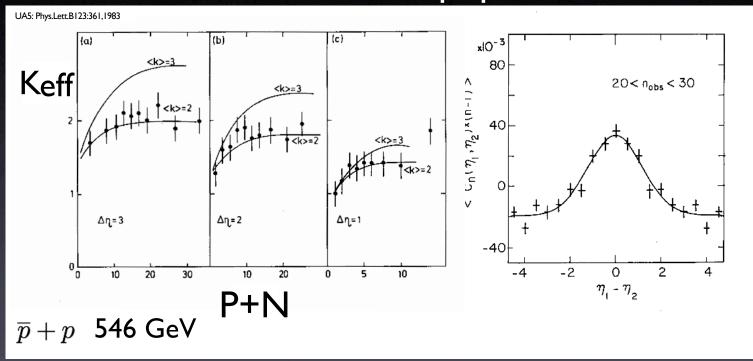
#### Cluster-size from F/B fluctuations



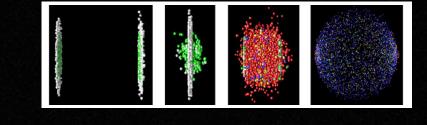
Forward/backward correlations suggest effective cluster size ≈ 2-2.5 for 200 GeV Au+Au



#### Clusters in p+p



# Clusters in Au+Au reminiscent of results from p+p

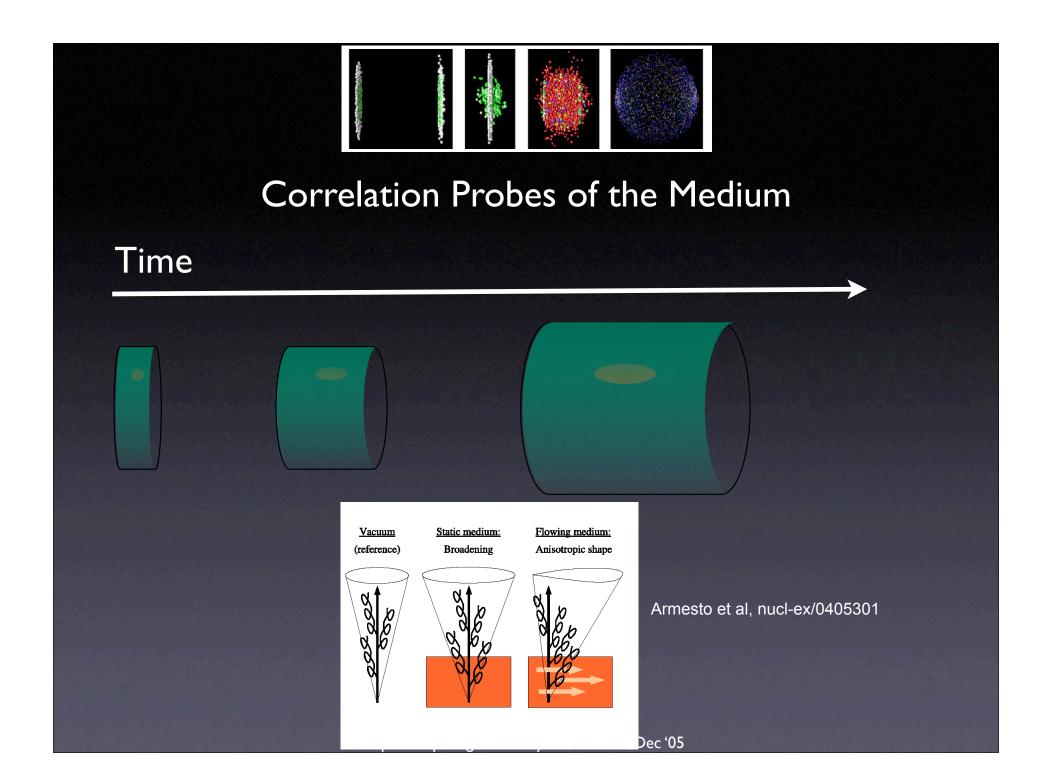


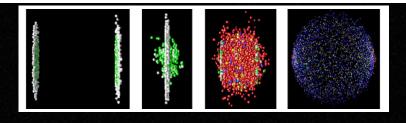
#### Correlation Probes of the Medium

Time

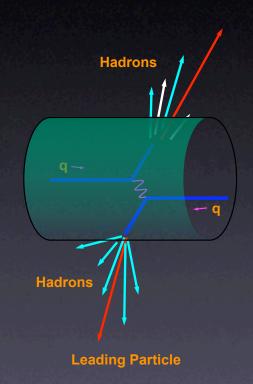


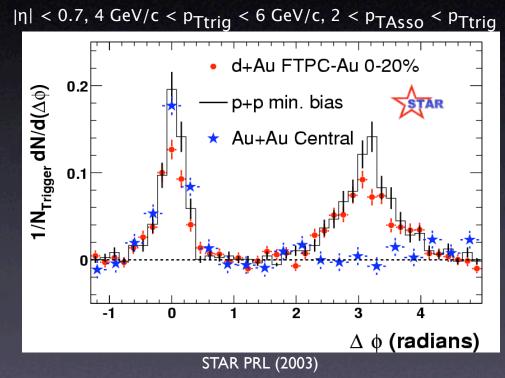
Probe





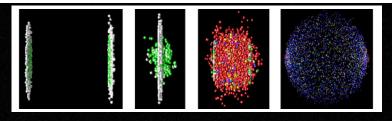
# Correlations at 'high' PT





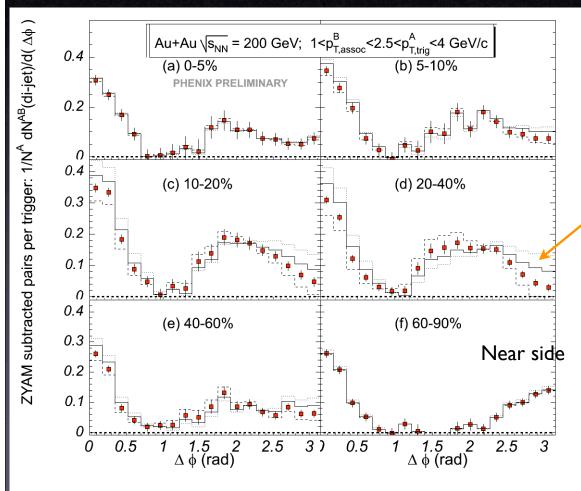
#### Relative to trigger particle:

- Jet-like near-side correlations visible in Au+Au
- Away-side correlations disappear for central Au+Au
  Supercomputing RHIC Physics, Mumbai, Dec '05



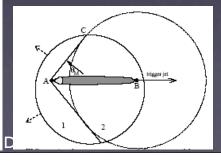
#### Correlations at not-so-high pT

PHENIX, ICPAQGP '05

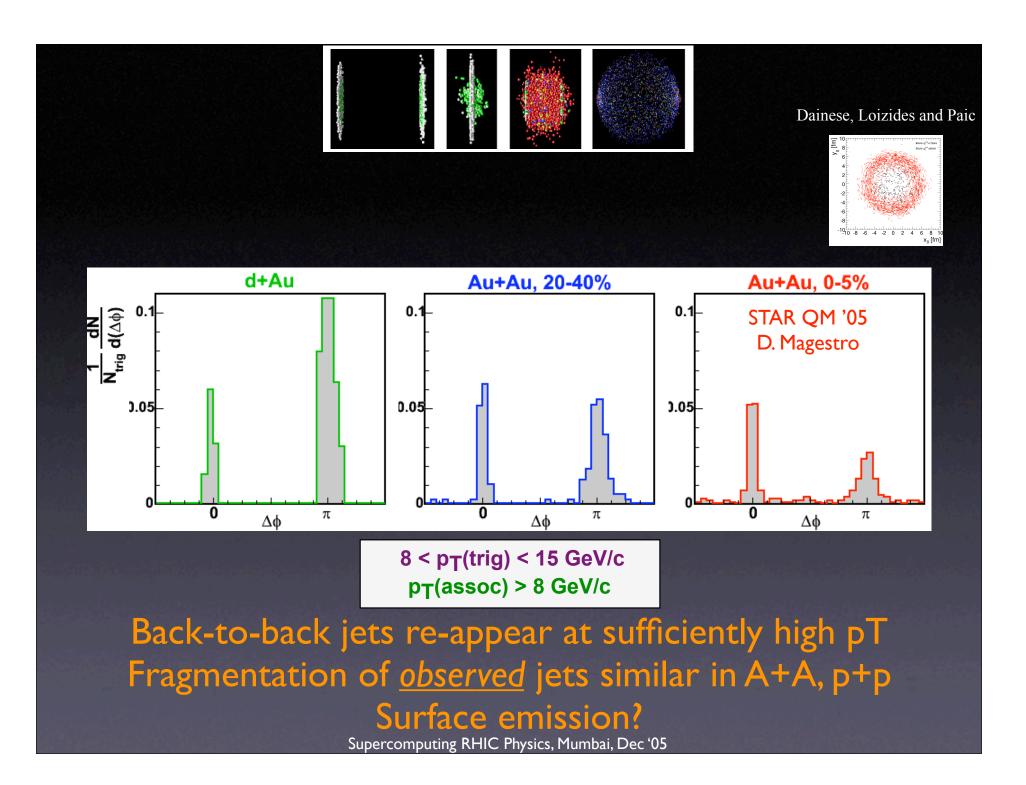


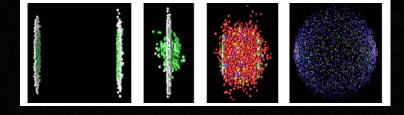
# Cone-Structure?

Sonic shock waves Stoecker, nucl-th0406018 Casalderrey, Shuryak, Teaney, hep-ph/0411315

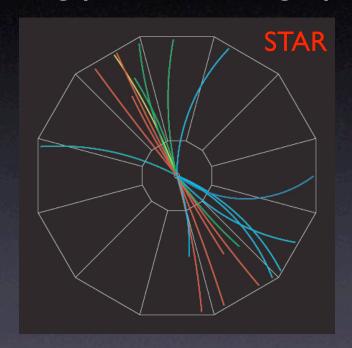


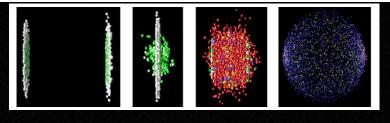
 $\cos(\theta) = c_S$ 



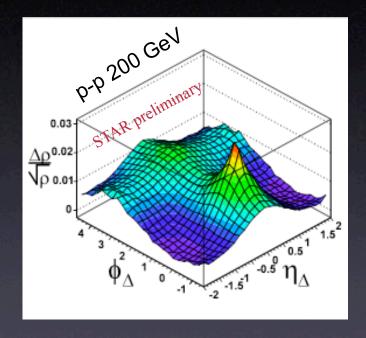


# Seeing partons at high pT





#### Soft Look at Partons

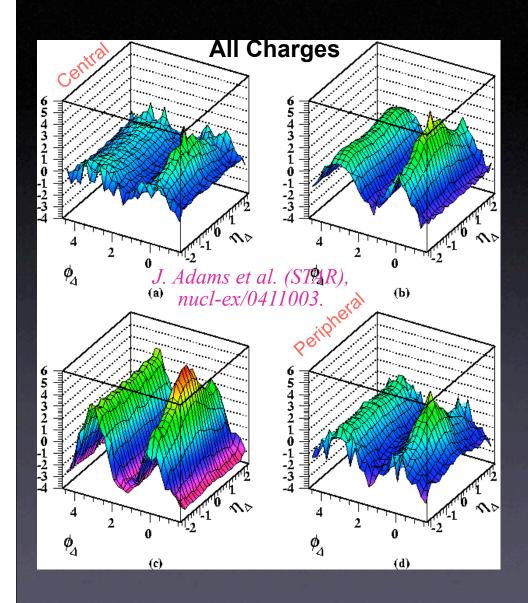


Tom Trainor, STAR

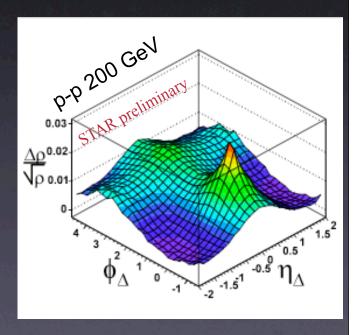
Two-particle angular correlations show rich structure at low to moderate  $p_T$  (~GeV/c)

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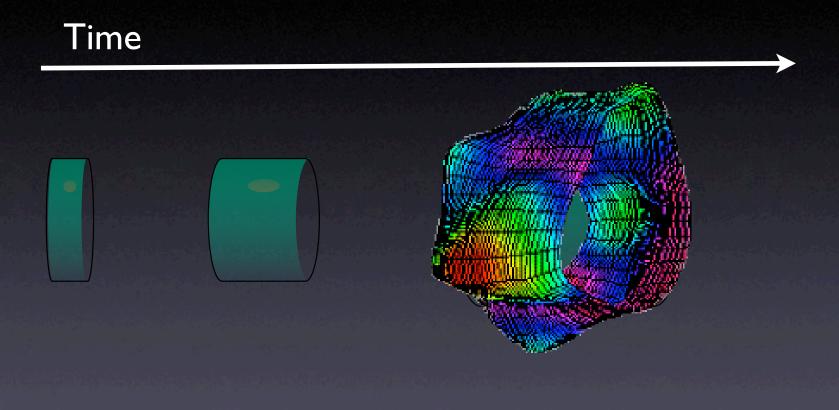
# From p+p to Au+Au



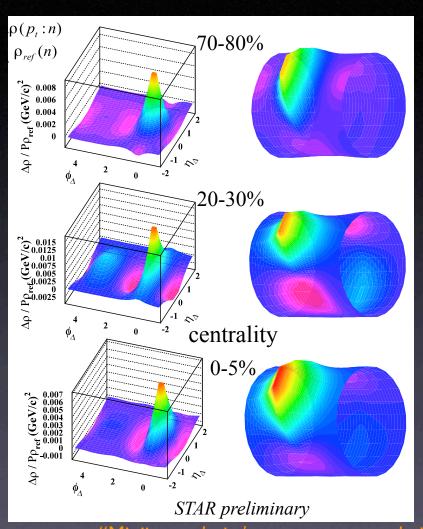
From p+p to central Au+Au



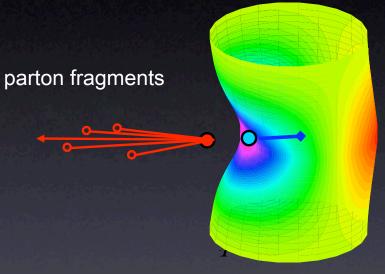
# Correlation Probes of the Medium



# Momentum Correlations at RHIC



Subtract fragmentation peak to look at medium

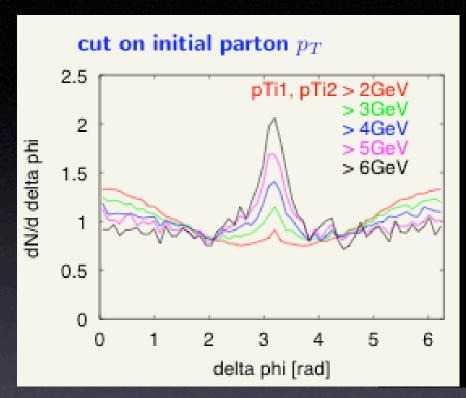


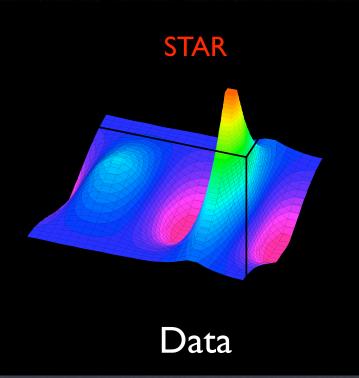
bulk medium

"Minijets: velocity/temperature correlation structures on  $(\eta,\phi)$ "

Tom Trainor, STAR, Bad Liebenzell, Oct '05 Supercomputing RHIC Physics, Mumbai, Dec '05

### Correlations in Transport Models



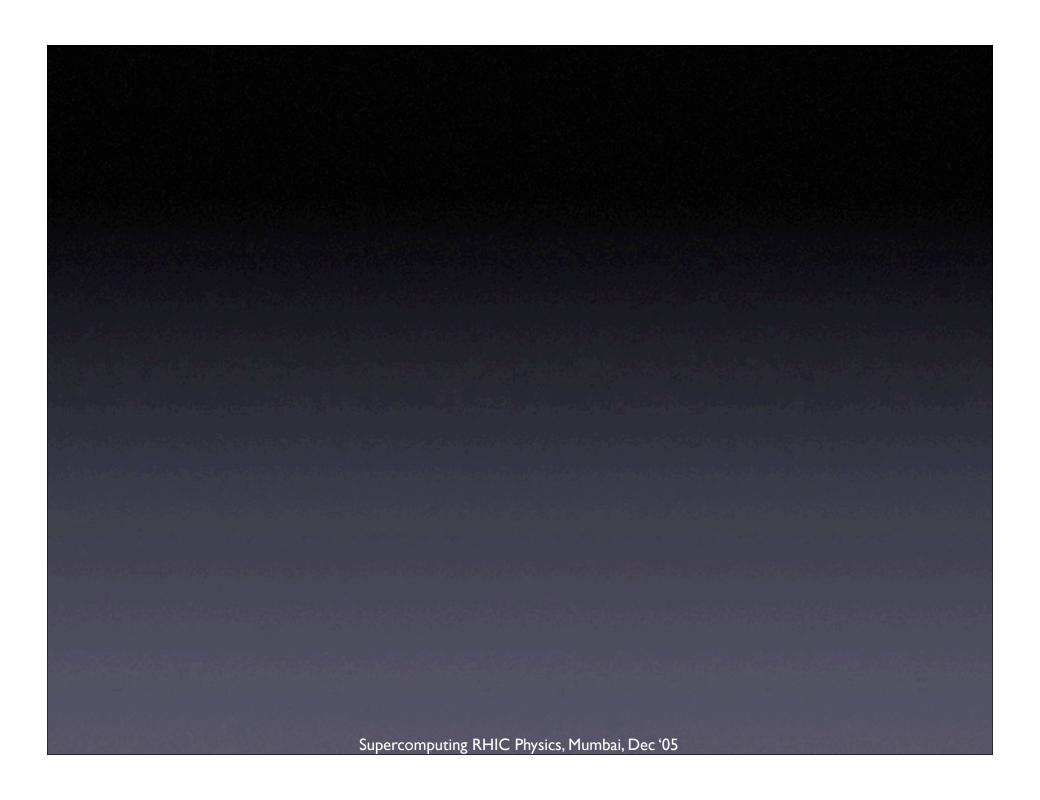


Denes Molnar, BNL workshop June '05

- This is the first study of jet correlations that treats the bulk sector and jets in the same framework. The results are encouraging but need several improvements:
  - add soft partons ("push" effect will contribute)
  - study centrality, particle type dependence (higher statistics)
  - include hadronization (coalescence, fragmentation)
  - extend to radiative processes, coherence
  - could also study other correlations, e.g., Mach cone ...

### Summary

- Evolving experimental + theoretical program
  - 'Global' scaling rules
  - Collective flow
  - Search for critical phenomena
  - Connection of correlations + fluctuations
  - Interaction of perturbations with medium
- Initial entropy production
- Fluctuations in small systems?
- Thermalization: How and what?
- What is the role of hadronization?



#### Net Charge, and $K/\pi$ Fluctuations

Instead of measuring the variance of a yield ratio,

$$r_{12} = \frac{n_1}{n_2} \qquad \Rightarrow \qquad \frac{\left\langle (\Delta r_{12})^2 \right\rangle}{\left\langle r_{12} \right\rangle^2} \approx \frac{\left\langle (\Delta n_1)^2 \right\rangle}{\left\langle n_1 \right\rangle^2} + \frac{\left\langle (\Delta n_2)^2 \right\rangle}{\left\langle n_2 \right\rangle^2} - 2\frac{\left\langle \Delta n_1 \Delta n_2 \right\rangle}{\left\langle n_1 \right\rangle \left\langle n_2 \right\rangle}$$

Study the "dynamical fluctuations":

$$v_{12,dyn} = \left\langle \left( \frac{n_1}{\langle n_1 \rangle} - \frac{n_2}{\langle n_2 \rangle} \right)^2 \right\rangle - \frac{1}{\langle n_1 \rangle} - \frac{1}{\langle n_2 \rangle} = \tilde{R}_{11} + \tilde{R}_{22} - 2\tilde{R}_{12}$$

Side Note:

$$D = \langle n_1 + n_2 \rangle \langle (\Delta r_{12})^2 \rangle$$

$$D = \langle n_1 + n_2 \rangle \langle (\Delta r_{12})^2 \rangle \qquad \frac{D}{4} \approx 1 + \frac{(\widetilde{R}_{++} + \widetilde{R}_{--} - 2\widetilde{R}_{+-})\langle n_+ + n_- \rangle}{4}$$

#### <p<sub>t</sub>> Fluctuations

$$\left\langle \Delta p_{t,1} \Delta p_{t,2} \right\rangle = \frac{1}{N_{event}} \sum_{k=1}^{N_{event}} \frac{C_k}{N_k (N_k - 1)}$$

where

$$C_{k} = \sum_{i=1}^{N_{k}} \sum_{j=1, i \neq j}^{N_{k}} \left( p_{t,i} - \left\langle \left\langle p_{t} \right\rangle \right\rangle \right) \left( p_{t,j} - \left\langle \left\langle p_{t} \right\rangle \right\rangle \right)$$

$$\left\langle p_{t} \right\rangle_{k} = \left( \sum_{i=1}^{N_{k}} p_{t,i} \right) / N_{k}$$

$$\langle\langle p_t \rangle\rangle = \left(\sum_{k=1}^{N_{event}} \langle p_t \rangle_k\right) / N_{event}$$

$$\left\langle p_{t}\right\rangle _{k}=\left(\sum_{i=1}^{N_{k}}p_{t,i}\right)/N_{t}$$

