

Importance of Granular Structure in the Initial Conditions for the Elliptic Flow

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HDM 2008, Mumbai India

Outline

- 1 Motivation
 - Fluctuating Initial Conditions
 - Granular Structure of IC
- 2 Fundamental tool: NeXSPheRIO
- 3 What is expected from the hot blobs?
- 4 Results
 - Transverse-momentum spectra
 - Elliptic-Flow Coefficient $\langle v_2 \rangle$
- 5 Summary
- 6 Outlook

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Hydrodynamic Model

In hydrodynamic approach of nuclear collisions, it is assumed that, after a complex process involving microscopic collisions of nuclear constituents, at a certain early instant a hot and dense matter is formed, which would be in local thermal equilibrium. Usually, this state is characterized by some **initial conditions** (IC), parametrized as smooth distributions of thermodynamic quantities and four-velocity.

Fluctuating Initial Conditions

- However, since our systems are small, **important event-by-event fluctuations** are expected in real collisions.
- In previous works, we introduced **fluctuating initial conditions** in hydrodynamics and studied several effects.
- In particular, we studied the **fluctuations of v_2** , where we showed that they are quite large.
T. Osada, C.E. Aguiar, Y. Hama and T. Kodama, *nucl-th/0102011*;
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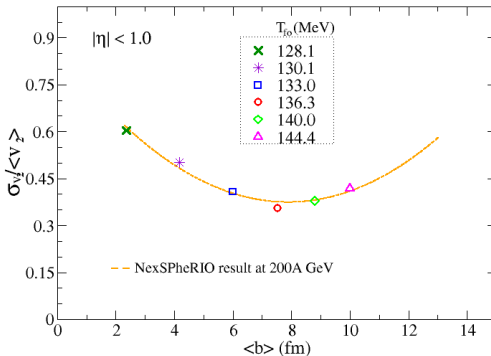
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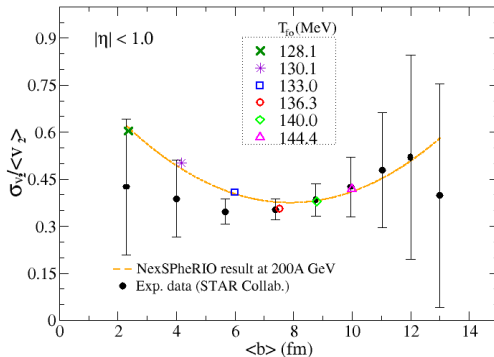
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$$\sigma_{V_2} / \langle V_2 \rangle$$



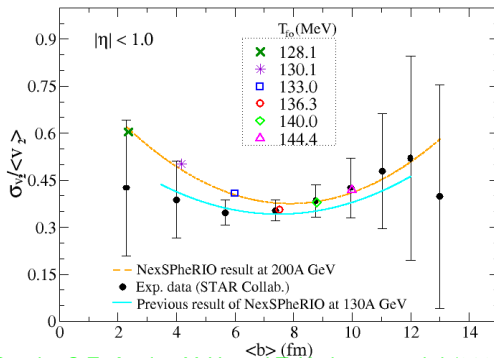
Curve: Y.H. *et al.*, [arXiv:0711.4544 \[hep-ph\]](https://arxiv.org/abs/0711.4544)

$\sigma_{v_2} / \langle v_2 \rangle$ - Comparison with data (STAR Collab.)



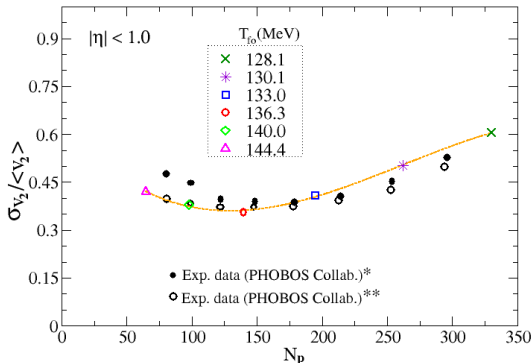
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Data: * C. Loizides [PHOBOS Collab.], QM 2006, nucl-ex/0701049;

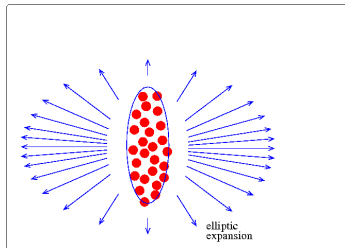
** B. Alver *et al.*, nucl-ex/0702036

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Granular Structure of IC

The IC for high-energy nuclear collisions are not only event-by-event fluctuating but, if the thermalization is verified at very early time, they should have **granular structure**.



Granular Structure of IC

The main object of this talk is to show **effects of such granular structure of IC** on some observables, **especially on the elliptic-flow parameter v_2** .

Fundamental tool: NeXSPheRIO

SPheRIO

NeXSPheRIO is a junction of two codes.

SPheRIO (Smoothed Particle hydrodynamic evolution of Relativistic heavy Ion collisions) is used to compute the hydrodynamic evolution

- **Smoothed Particle Hydrodynamics** was originally developed in astrophysics and adapted to relativistic heavy ion collisions
C.E.Aguiar, T.Kodama, T.Osada & Y.Hama, J.Phys.G27(2001)75;
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Fundamental tool: NeXSPheRIO

NeXus

NeXus is used to generate the **initial conditions** (IC)

[H.J. Drescher, F.M. Liu, S. Ostrapchenko, T. Pierog and K. Werner, *Phys. Rev. C* **65** (2002) 054902.]

- Its main advantage is that, once a pair of incident nuclei and their incident energy are chosen, it can produce, in the **event-by-event basis**, detailed space distributions of energy-momentum tensor, baryon-number, strangeness and charge densities, at a given initial time $\tau = \sqrt{t^2 - z^2} \sim 1$ fm.
- One important characteristic of such fluctuating IC is that **each set of IC is highly irregular**.
- Many simulators, based on microscopic models, show such event-by-event fluctuations. Here we use **NeXus**.

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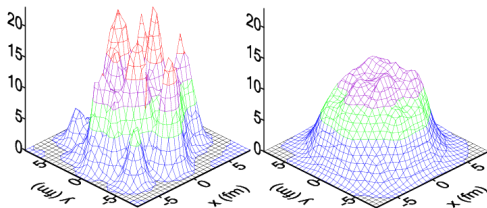
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Initial Conditions

Energy density for central Au+Au collisions at 130 A GeV, given by NeXus simulator, at mid-rapidity

One random event

Average over 30 events



Fundamental tool: NeXSPheRIO

Method of analysis

In the present work, we perform two sets of computations:

- 1 First, we average over random NeXus events, obtaining smooth IC, which are used to compute the observables by using the SPheRIO code.
This is similar to the usual hydro calculation.
- 2 In the second set, NeXSPheRIO is run many times and an average over final results is performed.
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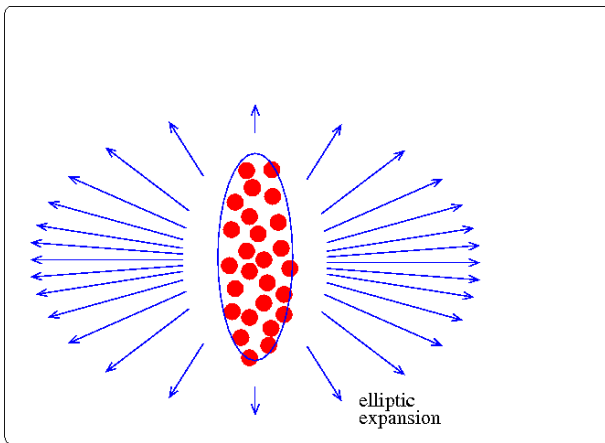
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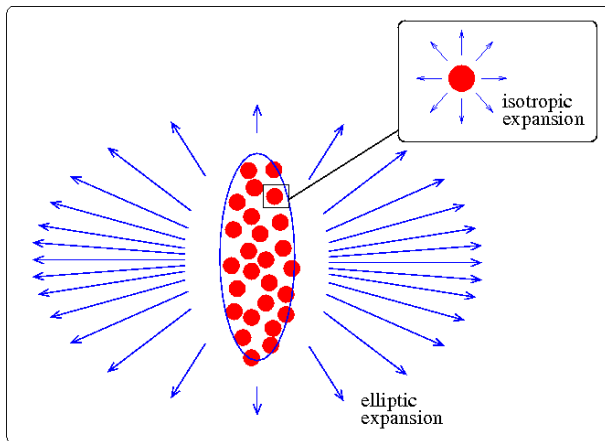
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What is expected from the hot blobs?



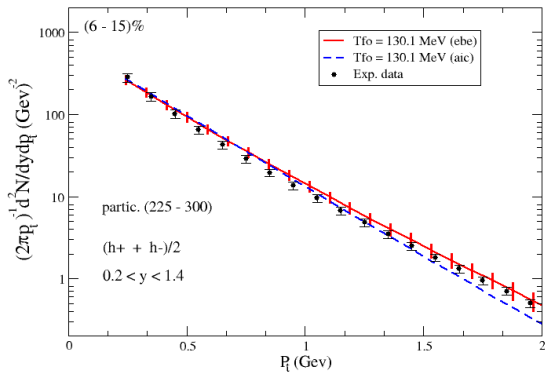
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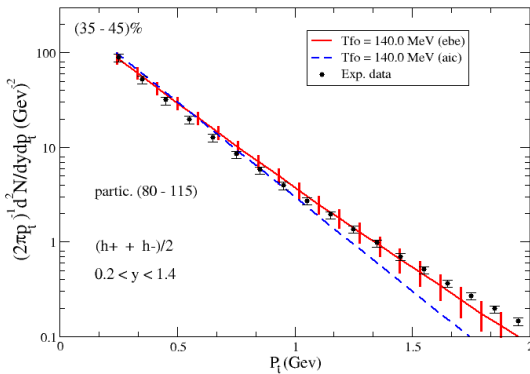
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Results: p_T distribution



Data: PHOBOS Collab., B.B. Back *et al.* Phys.Lett. B578 297 (2004)

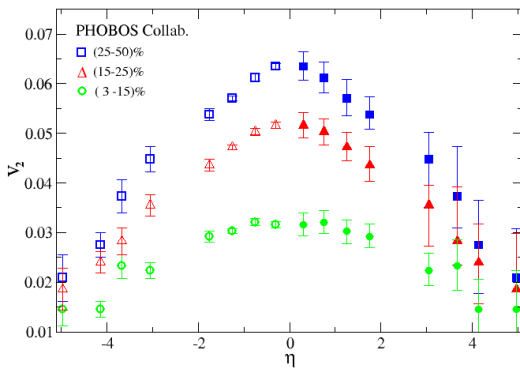
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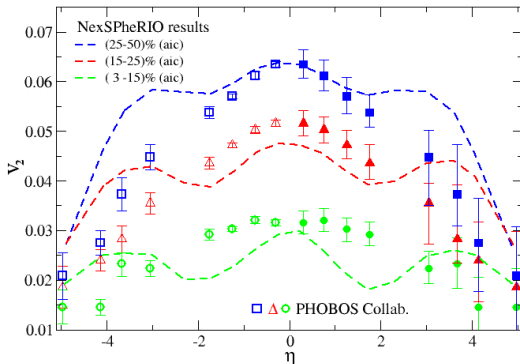
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$\langle v_2 \rangle (\eta)$ - Data

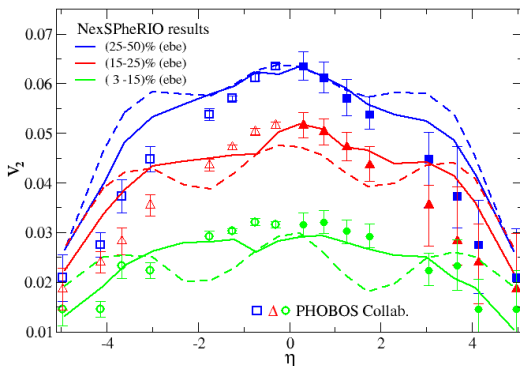
Data: PHOBOS Collab., B.B. Back *et al.* Phys.Rev. C72 051901 (2005)

Results: $\langle v_2 \rangle (\eta)$ - Averaged (smooth) IC



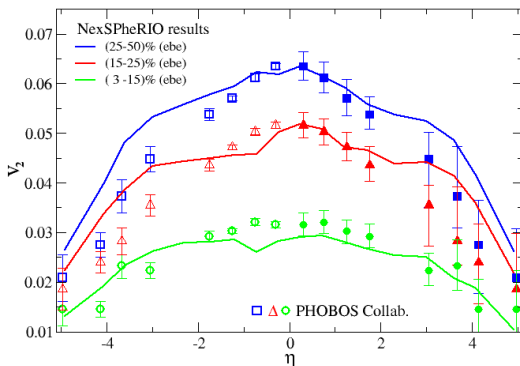
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Results: $\langle v_2 \rangle (\eta)$ - Fluctuating IC (with blobs)

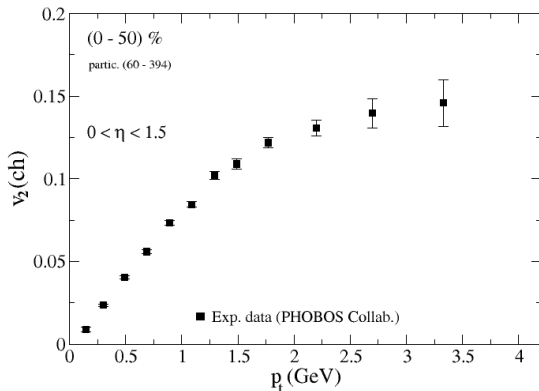


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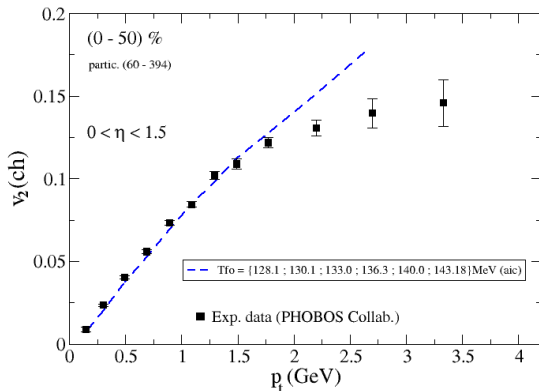
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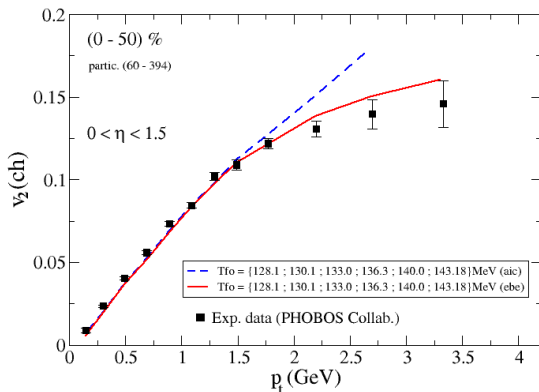
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$\langle v_2 \rangle (p_T)$ - Data

Data: PHOBOS Collab., B.B. Back *et al.* Phys.Rev. C72 051901 (2005)

Results: $\langle v_2 \rangle (p_T)$ - Smooth IC

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Results: $\langle v_2 \rangle (p_T)$ - Bumpy IC

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Summary

- **Granular structure** in the IC produces more high- p_T particles.
- **Granular structure** in the IC reduces the elliptic flow.
- This effect is enhanced where the average matter density is small. So, it decreases v_2 in the large pseudorapidity regions.
- As function of p_T , the mechanism becomes more effective as p_T increases, because those high-density blobs cause violent expansion, producing high- p_T particles.
- **NeXSPheRIO, with fluctuating IC**, reproduce approximately both the p_T -distribution and η -distribution of v_2 for different centrality windows.

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Outlook

The effect of **continuous emission** is being computed. Probably it makes the curve of v_2 at high- p_T even flatter and the η -distribution narrower.

Additional remarks - NeXSPheRIO

Previous Results - 1

NeXSpheRIO has been used to study a range of problems:

- effect of fluctuating initial conditions on particle distributions [C.E. Aguiar *et al.* Nucl.Phys. **A698** 639c \(2002\)](#)
- energy dependence of the kaon effective temperature [M. Gaździcki *et al.* Braz.J.Phys. **34** 322 \(2004\); Acta Phys. Pol. **B35** 179 \(2004\)](#)
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- effect of the nature of the quark-hadron transition and of the particle emission mechanism [Y. Hama *et al.* QM05 proceedings, Nucl.Phys. A774 169 \(2006\)](#)
- how to experimentally obtain the true $\langle v_2 \rangle$ [R. Andrade *et al.*, Phys.Rev.Lett. 97 202302 \(2006\)](#)

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- how to experimentally obtain the true $\langle v_2 \rangle$ [R. Andrade *et al.*, Phys.Rev.Lett. **97** 202302 \(2006\)](#)

Additional remarks - NeXSPheRIO

Previous Results - 2

- effect of the different theoretical and experimental binnings
[R.Andrade *et al.* Braz.J.Phys. **34** 319 \(2004\)](#)
- effect of the nature of the quark-hadron transition and of the particle emission mechanism [Y. Hama *et al.* QM05 proceedings, Nucl.Phys. **A774** 169 \(2006\)](#)
- how to experimentally obtain the true $\langle v_2 \rangle$ [R. Andrade *et al.*, Phys.Rev.Lett. **97** 202302 \(2006\)](#)