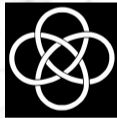


# Higher-order clustering statistics

## in the Intergalactic Medium using Lyman- $\alpha$ forest

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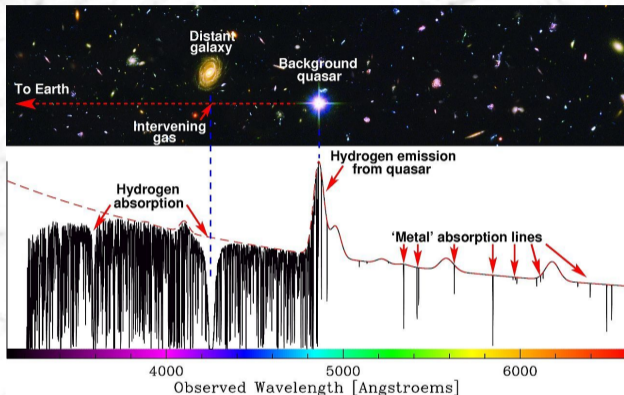
Soumak Maitra  
IUCAA, Pune, India



Collaborators: Prof. Raghunathan Srianand (Guide), Prof. Patrick Petitjean, Prof. Tirthankar Roy Choudhury,  
Dr. Prakash Gaikwad, Prof. Nishikanta Khandai, Prof. Aseem Paranjape,  
Prof. Christophe Pichon, Dr. Hadi Rahmani



- Majority of the baryonic content of the Universe lies in the Intergalactic Medium (IGM).
- Tracer of large scale cosmic density fields.
- Probes the astrophysical processes associated with galaxies and the circumgalactic medium (CGM) at small scales.
- Baryonic pressure broadening retains memory of the thermal history of Universe.

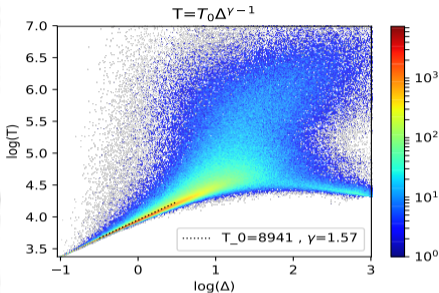


- Matter distribution in the IGM manifests itself in the form of HI Lyman- $\alpha$  forest absorption in the spectra of distant quasars.
- Lyman- $\alpha$  forest probes matter in a quasi-linear regime (experiences the gravitational potential but not a virialized system).



# Ionization state of the IGM: Fluctuating Gunn-Peterson optical depth

- $F_{obs} = F_{cont} e^{-\tau_{HI}}$
- $\tau_{HI} = \int dl n_{HI} \sigma_{HI} \sim 10^5 X_{HI}$
- Non-trivial mapping from dark matter overdensity to  $n_{HI}$ . Interpretation of observed data requires simulations to implement the baryonic physics.



- Under the assumption of thermal and ionization equilibrium, and ignoring the effects of thermal broadening, the Gunn-Peterson optical depth is given as:

$$\tau_{HI,GP} = 0.172 \Delta^{2-0.7\gamma} \left( \frac{\Omega_b h^2}{0.0125} \right)^2 \left( \frac{H(z)/H_0}{5.51 h} \right)^{-1} \left( \frac{1+z}{4} \right)^6 \left( \frac{T_0}{10^4 \text{K}} \right)^{-0.7} \left( \frac{\Gamma}{10^{-12} \text{s}^{-1}} \right)^{-1} \left( 1 + \frac{dv_{los}/dx}{H(z)} \right)^{-1}$$

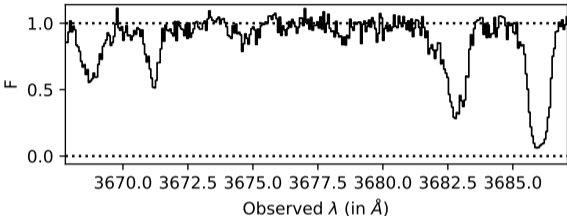
- Larger Overdensities typically correspond to larger  $\tau_{HI}$ . Correlations in transmitted flux can be used as a probe of underlying overdensity field (Non-trivial mapping from density to Flux).
- Alternative approach is to construct a count-based correlation statistics using distinct absorber treatment of Lyman- $\alpha$  forest.



# Clustering study based on cloud picture

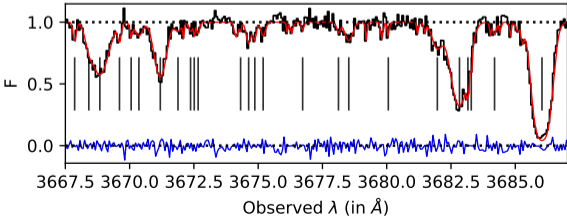
## Flux-based statistics:

- $\xi(\Delta r) = \langle \delta_F(r) \delta_F(r + \Delta r) \rangle$   
where  $\delta_F = F - \langle F \rangle$
- $\zeta(\Delta r_{12}, \Delta r_{13}, \theta) = \langle \delta_F^1 \delta_F^2 \delta_F^3 \rangle$



## Cloud-based statistics:

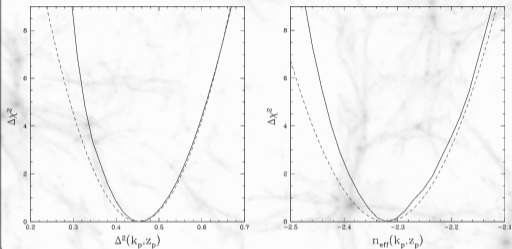
- $\xi = \langle \frac{\text{Data pairs}}{\text{Random pairs}} - 1 \rangle$
- $\zeta = \langle \frac{\text{Data triplets}}{\text{Random triplets}} - 1 \rangle$
- Advantages:
  - Allows column density (or conversely  $\Delta$ ) dependent clustering study.
  - Direct probe of non-gaussianity in clustering.



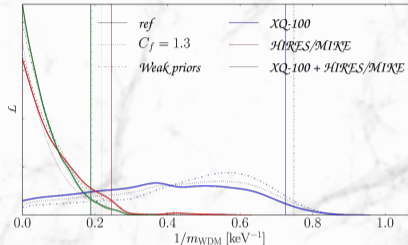


# Lyman- $\alpha$ forest: Cosmological Utility

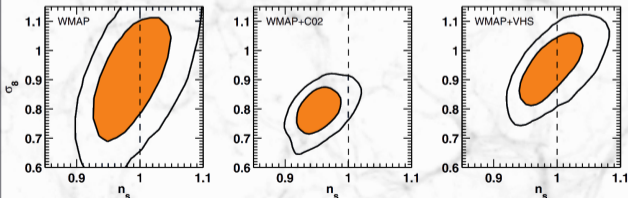
### Linear Theory Power spectrum (McDonald+2005)



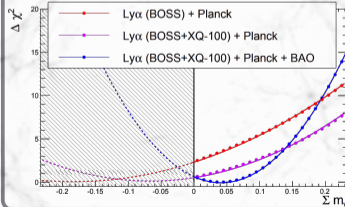
### Warm Dark Matter model (Irsic+2017)



### Primordial Power spectrum (Viel+2004)



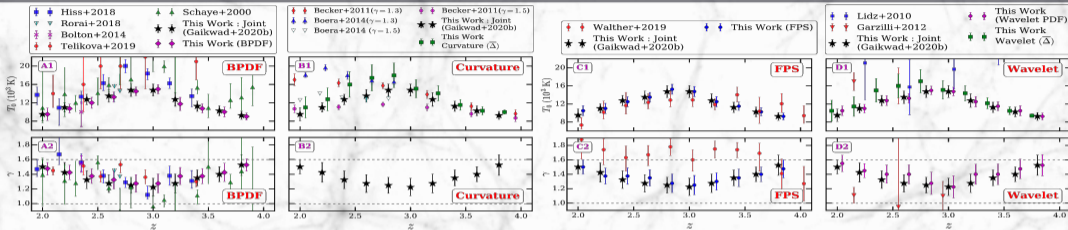
### Neutrino Mass (Yeche+2017)



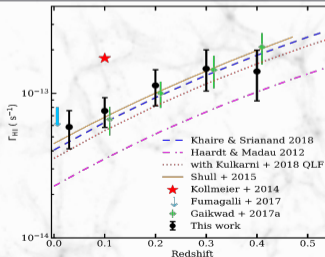


# Lyman- $\alpha$ forest: Astrophysical Utility

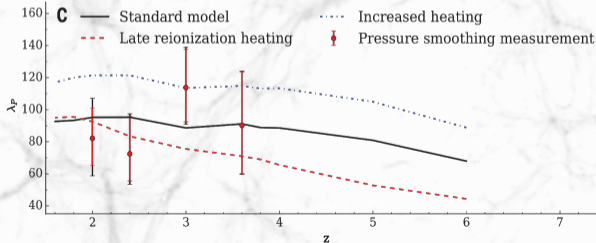
## IGM Thermal Evolution (Gaikwad+2020)



## UV Background (Khair+2019)



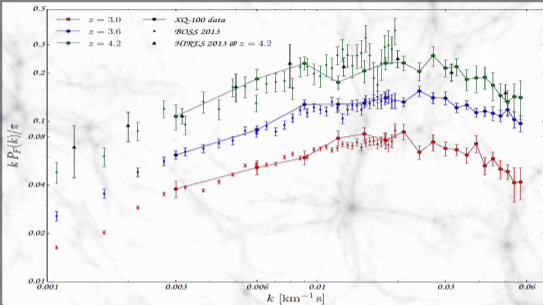
## Pressure broadening scale: Sensitive to thermal history (Rorai+2017)



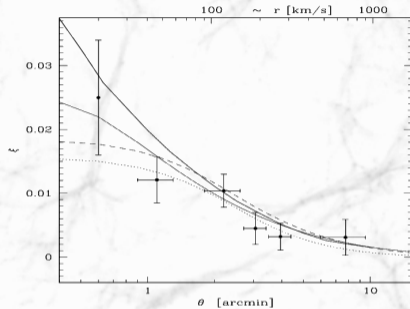


# Clustering in Lyman- $\alpha$ forest

Redshift space (Irsic+2017)



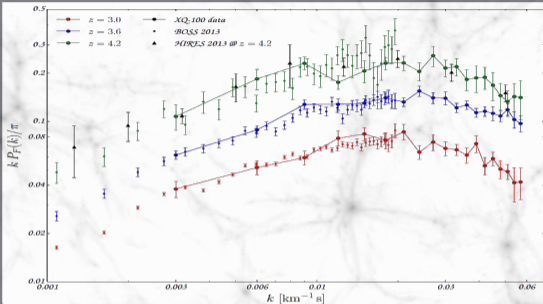
Transverse (Coppolani+2006)



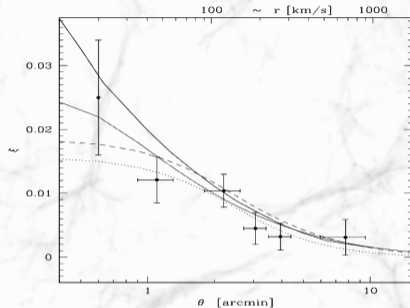


# Clustering in Lyman- $\alpha$ forest

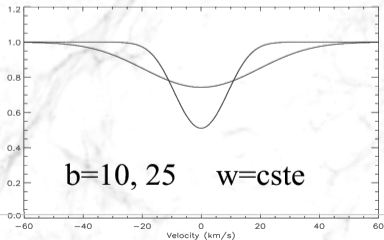
Redshift space (Irsic+2017)



Transverse (Coppolani+2006)



- Peeples+2010a,b demonstrate that redshift space correlations are dominated by thermal broadening ( $b = \sqrt{2kT/m}$ ) effects while transverse correlations are dominated by pressure broadening.
- Thermal broadening washes away clustering informations at small scales.







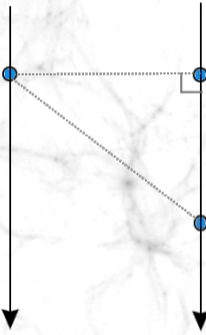
Higher order clustering statistics largely unexplored in the case of Lyman- $\alpha$  forest.

Three-point statistics of clustering in Lyman- $\alpha$  forest would be useful for:

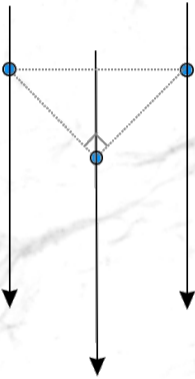
- Non-gaussianity in matter distribution at small scales and at high redshifts. Also calculate higher order bias.
- Act as an independent tool complementing the two-point statistics in constraining the cosmological parameters ([Fry 1994](#), [Verde+2002](#)) and the physical state of the IGM.
- Remove degeneracies between different cosmological parameters.
- Determine the amplitude, slope and curvature of the slope of the matter power spectrum with better precision ([Mandelbaum+2003](#)).
- Probing primordial non-gaussianity ([Hazra & Sarkar 2012](#))
- Probe the influence of large scale fluctuations on small scale power spectrum using squeezed limit bispectrum ([Zaldarriaga+2001](#)).
- Probing the statistical anisotropy of clustering in the cosmic web, using projected quasar triplet sightlines.



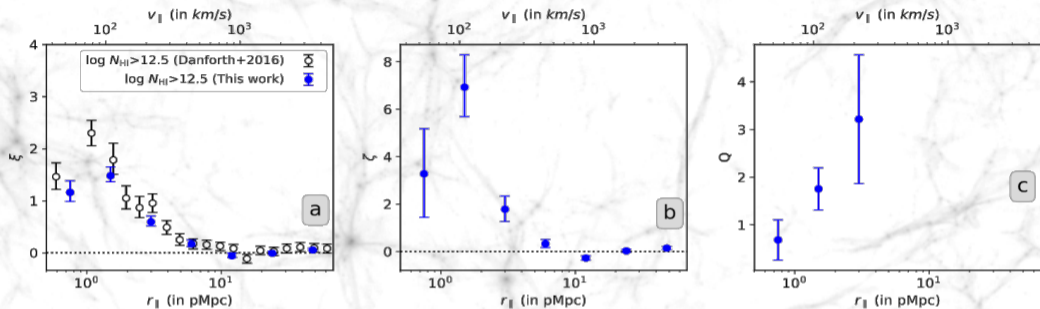
Redshift space correlation.



Partial Redshift space + transverse correlation.



Transverse correlation.

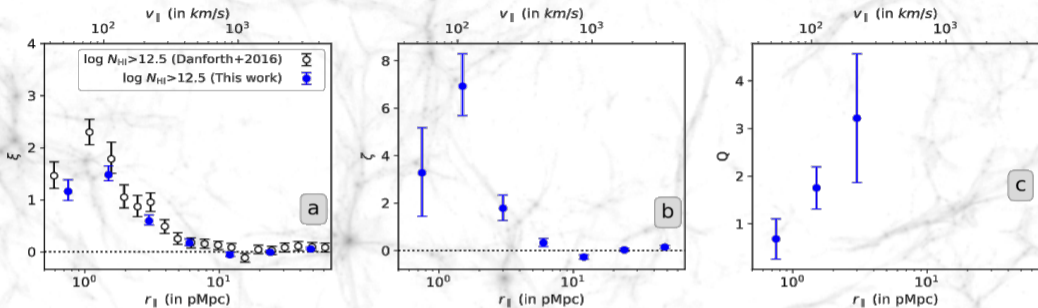


- 82 quasar sightlines from HST-COS
- Redshift based clustering study (colinear triplet configurations probed along quasar sightlines;  $r_1 = r_2 = r_{\parallel}, r_3 = 2r_{\parallel}$ ).
- Lyman- $\alpha$  forest probed in  $z < 0.48$ .

Reduced  $\zeta$  or  $Q = \zeta / (\xi_1 \times \xi_2 + \xi_2 \times \xi_3 + \xi_3 \times \xi_1)$   
[Hierarchical Ansatz]

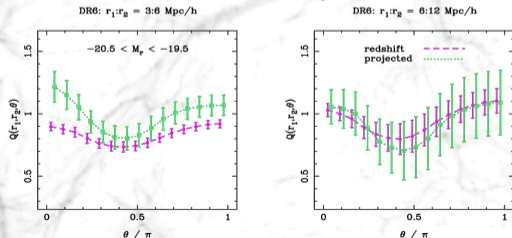


# First detection of non-gaussianity in low- $z$ Lyman- $\alpha$ forest (Maitra+2020b)

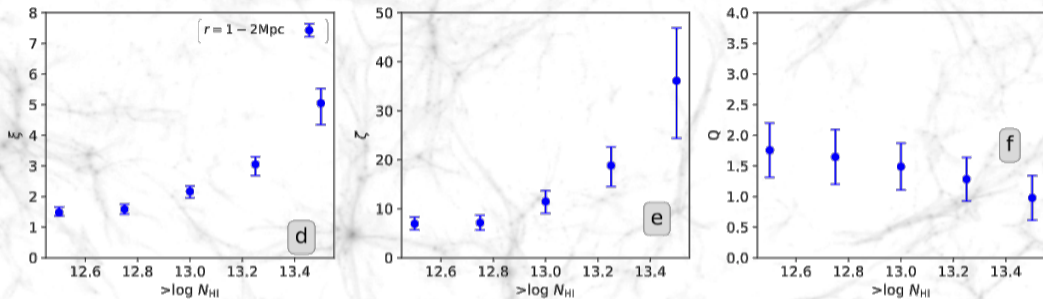


- 82 quasar sightlines from HST-COS
- Redshift based clustering study (colinear triplet configurations probed along quasar sightlines;  $r_1 = r_2 = r_{||}, r_3 = 2r_{||}$ ).
- Lyman- $\alpha$  forest probed in  $z < 0.48$ .

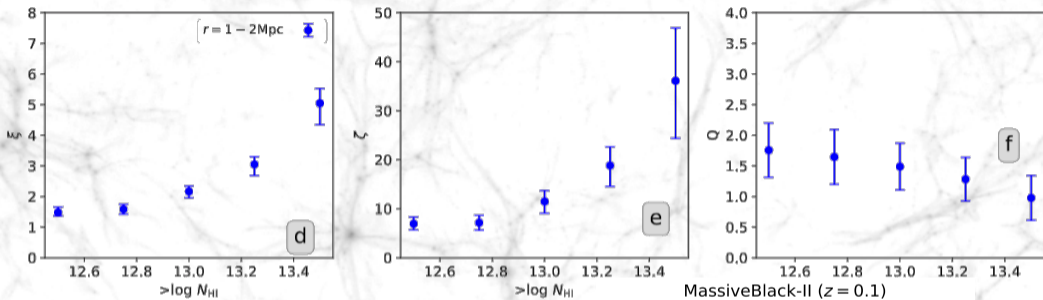
Reduced  $\zeta$  or  $Q = \zeta / (\xi_1 \times \xi_2 + \xi_2 \times \xi_3 + \xi_3 \times \xi_1)$   
[Hierarchical Ansatz]



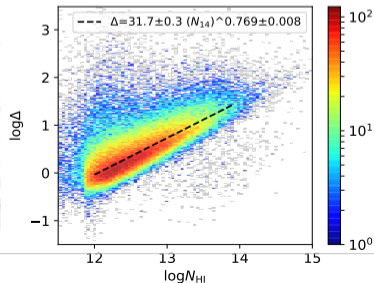
Clustering in SDSS galaxies: [McBride+2010](#)

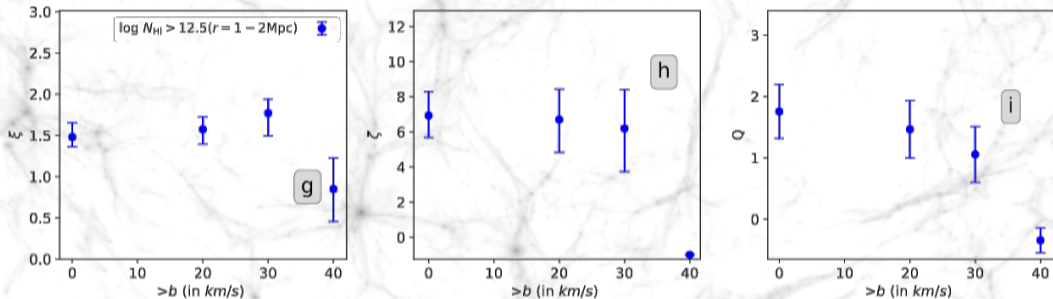


- HI column density ( $N_{\text{HI}}$ )  $\iff$  Baryonic overdensity ( $\Delta$ ).
- Strong dependence of  $\xi$  and  $\zeta$  on  $N_{\text{HI}}$  thresholds.
- Effect on  $Q$  very weak.



- HI column density ( $N_{\text{HI}}$ )  $\iff$  Baryonic overdensity ( $\Delta$ ).
- Strong dependence of  $\xi$  and  $\zeta$  on  $N_{\text{HI}}$  thresholds.
- Effect on  $Q$  very weak.





- Weak dependence on line-width parameter  $b = \sqrt{2kT/m}$  upto a  $b$  threshold of  $30 \text{ km/s}$ . Sharp decrease in correlation amplitude at  $b > 40 \text{ km/s}$  (Broad Lyman- $\alpha$  Absorbers or BLAs).
- Frequency of occurrence of atleast 1 BLAS in triplet systems ( $\sim 88\%$ ) is a factor  $\sim 3$  higher than that found among the full sample ( $\sim 32\%$ ).
- BLAs possibly trace the warm-hot intergalactic medium (WHIM) in the temperature range between  $10^5$  and  $10^6$  K (Richter+2006). Arises from collisionally ionized regions in filaments.



## Association with metal systems and galaxies:

- Only 40% of the total observed Lyman- $\alpha$  triplets have associated metals with them.
- Majority of the triplets have multiple nearby galaxies.
- 84% of the triplets have at least one nearby galaxy within a velocity separation of  $500\text{km/s}$ . The impact parameters of these galaxies range from 62-3854 pkpc (median of 405 pkpc)
- The median impact parameter seems to decrease for higher  $N_{\text{HI}}$  thresholds.
- BLAs occurring more frequently with triplets and association with nearby galaxies suggest Lyman- $\alpha$  triplets originating from filamentary structures.

## Trends in simulations:

- Simulations suggest line of sight peculiar velocities tend to enhance the observed  $\xi$  and  $\zeta$  by  $\sim 60\%$ , whereas the  $Q$  values are suppressed by  $\sim 70\%$ .
- Feedback processes have little effect on the observed clustering.



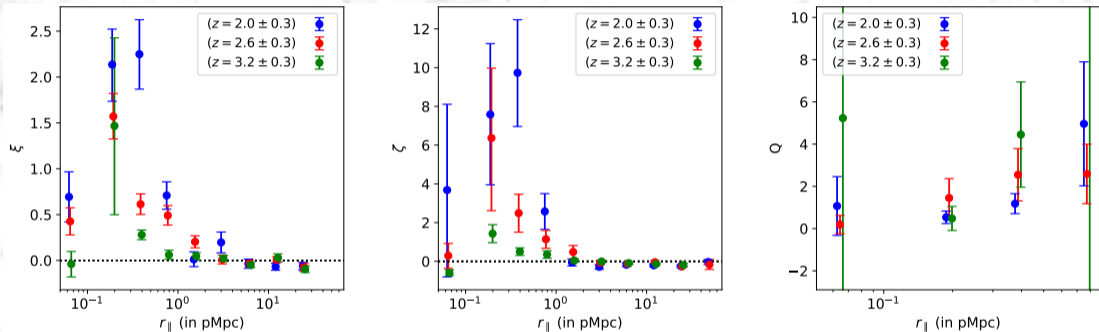
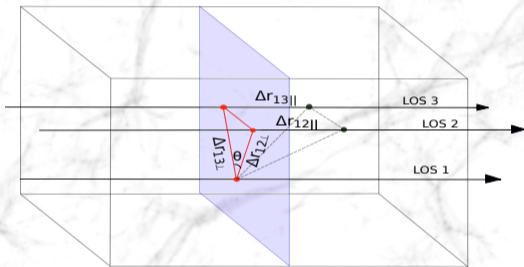


Figure: High- $z$  correlations of  $N_{\text{HI}} > 10^{13.5} \text{cm}^{-2}$  in KODIAQ data.

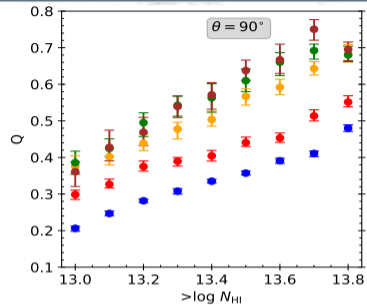
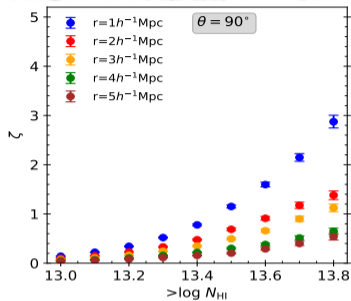
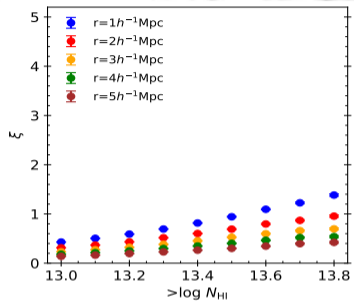
Work in progress ...



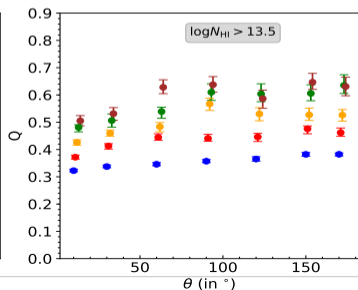
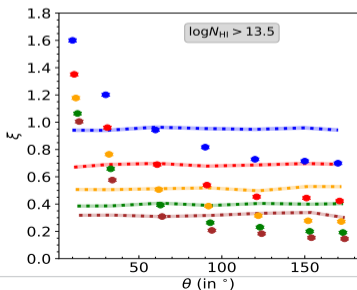
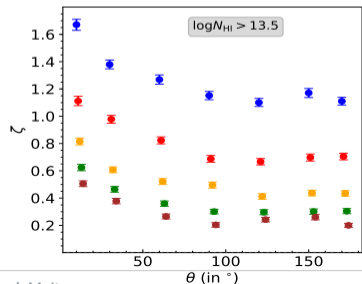
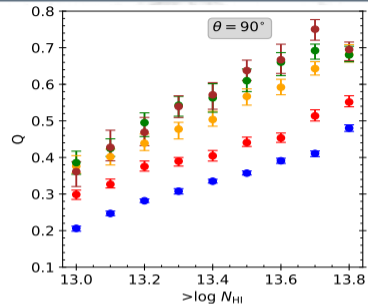
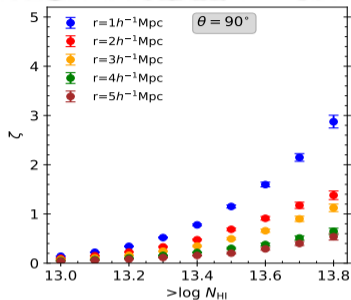
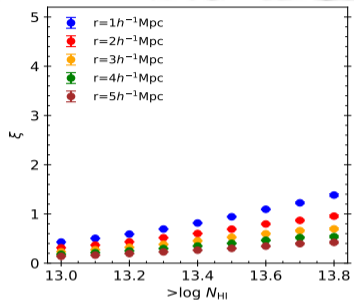
- $\Delta$ ,  $v$ ,  $T$  obtained from GADGET-3 hydrodynamical simulation.
- Shoot triplet sightlines through simulation box.
- Investigate  $\zeta$  and its dependencies on:
  - Scale.
  - Angle.
  - $N_{\text{HI}}$  or conversely  $\Delta$ .
  - Thermal history.
- We consider only isosceles configurations for  $\zeta$  ( $\Delta r_{12\perp} = \Delta r_{13\perp} = r$ ).



# Transverse three-point correlation in Simulations at $z \sim 2$ (Maitra+2020a)

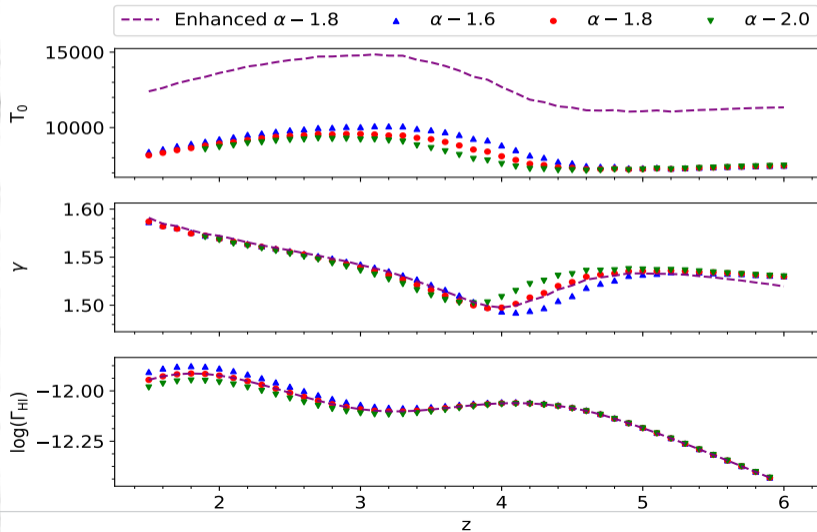


# Transverse three-point correlation in Simulations at $z \sim 2$ (Maitra+2020a)



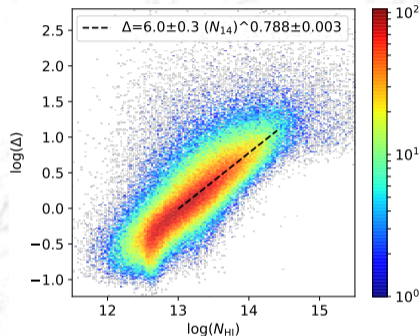
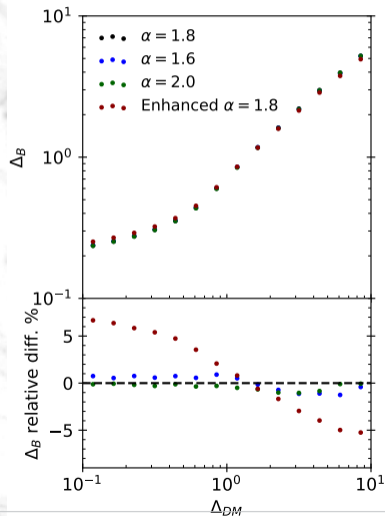


Effect of thermal history:





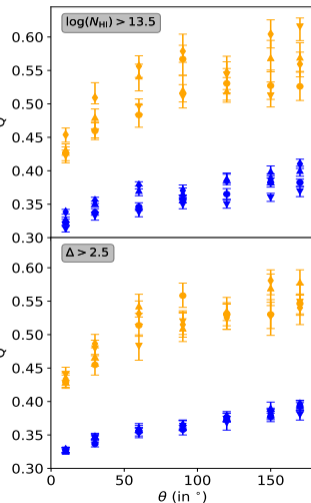
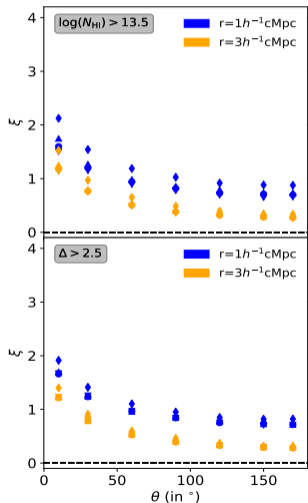
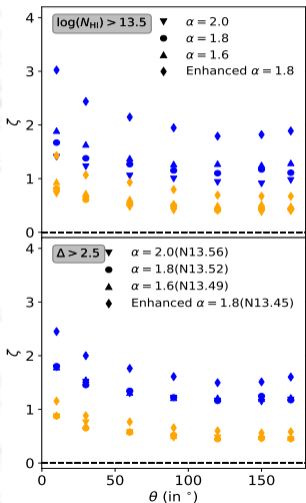
## Effect of thermal history:



- Correlations for a fixed  $N_{\text{HI}}$  threshold depends on  $\Delta$  field + local thermal effects.
- Local thermal effects are imprinted on the  $\Delta$  to  $N_{\text{HI}}$  mapping.
- Using a constant  $\Delta$  threshold should statistically show the effects of pressure broadening.

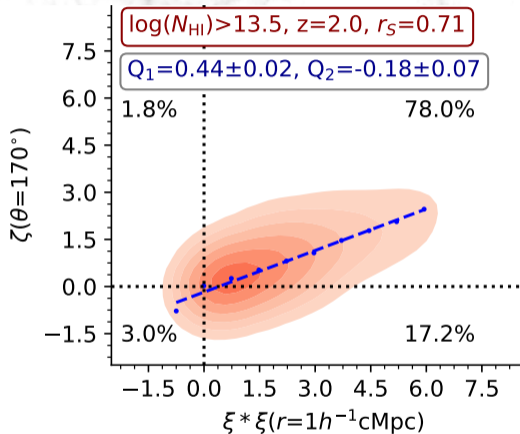


## Effect of thermal history:





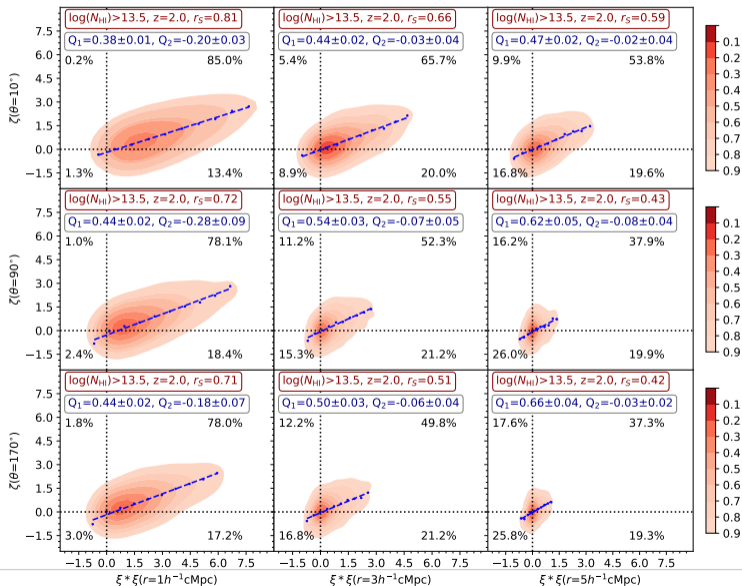
## Validity of Hierarchical Ansatz:

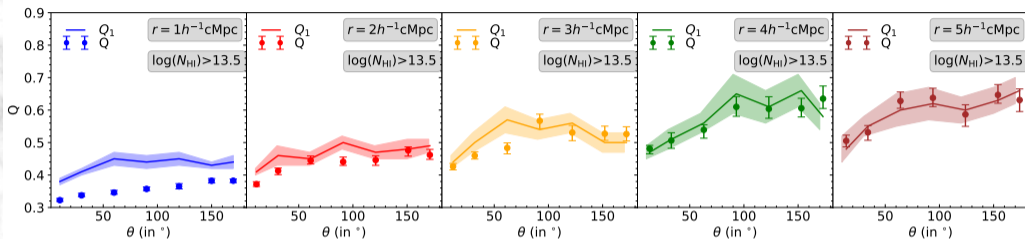


$$\zeta = Q_1(\xi * \xi) + Q_2$$

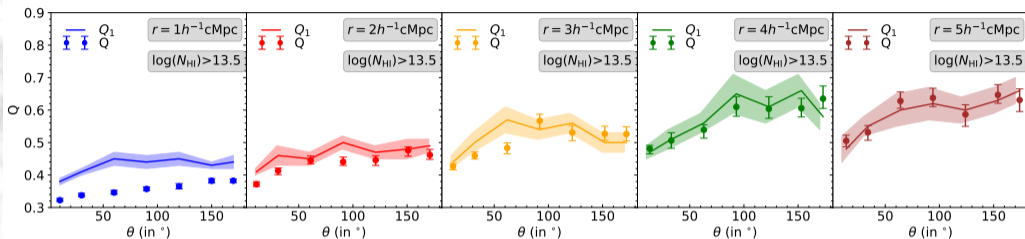


# Transverse three-point correlation in Simulations at $z \sim 2$ (Maitra+2020a)





Three-point correlation suppressed at scales below  $3h^{-1} \text{cMpc}$  [ $Q_2$  -ve]. Source?



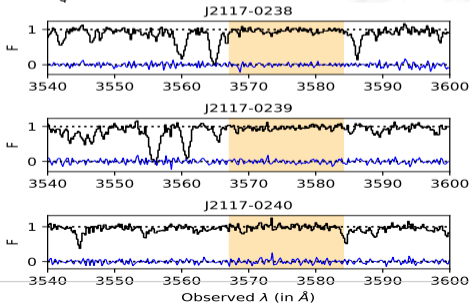
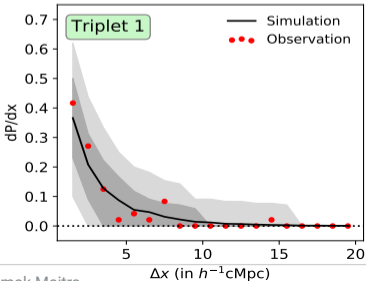
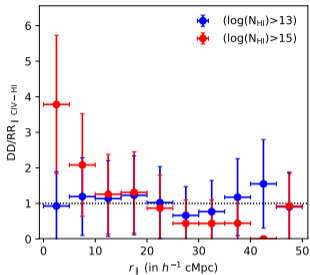
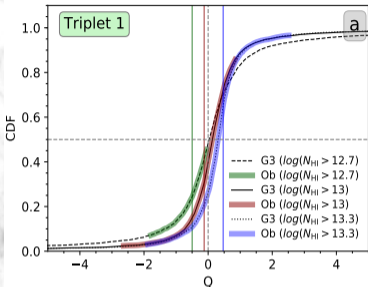
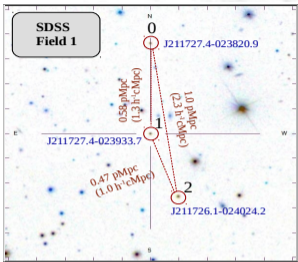
Three-point correlation suppressed at scales below  $3h^{-1}\text{cMpc}$  [ $Q_2$  -ve]. Source?

We used the SDSS catalog to get an estimate of the number of quasar triplets present and achievable significance of three-point correlation detection with these sample of quasars.

- For  $\theta \leq 20^\circ$ ,  $\zeta$  can be observed the scales of 4 and  $5h^{-1}\text{cMpc}$  with  $4.8\sigma$  and  $4.5\sigma$  respectively. For that, we need to observe 70 quasar triplets (210 spectra) having  $r = 4h^{-1}\text{cMpc}$  and 86 quasar triplets (i.e 258 spectra) having  $r = 5h^{-1}\text{cMpc}$ .
- For  $\theta = 90^\circ$ , the most significant detection can be achieved for 2 and  $3h^{-1}\text{cMpc}$  ( $4.4\sigma$  and  $4.7\sigma$  respectively). We need to observe 42 quasar triplets having  $r = 2h^{-1}\text{cMpc}$  and 96 quasar triplets having  $r = 3h^{-1}\text{cMpc}$ .



# Observational prospects with QSO triplet sightlines (Maitra+2019)





- Extend study to non-standard  $\Lambda$ CDM models.
- We would like identify filamentary structures associated with galaxies (near observed Lyman- $\alpha$  triplets) and try to explore the association of such structures with observed Lyman- $\alpha$  triplets.
- Investigate partial redshift space + transverse three-point correlation using projected quasar pairs ([Findlay+2018](#)).
- We identified a unique configuration of 7 quasars (with  $r < 20.5$  and  $z > 2.2$ ) in SDSS catalog that opens the opportunity to probe correlated IGM structures at  $z \sim 2$ . Use these 7 quasar sightlines to study the directional dependence of density/radiation field around the foreground QSOs through the analysis of the transverse proximity effect.
- Theoretical understanding of metal distribution in IGM (project led by Sukanya Mallik, IUCAA).
- Inversion problem: Mapping the observed transmitted flux to underlying overdensity and velocity fields.