

# Perturbations In Some Dark Energy Models

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# The Universe

- ▶ The Universe is described by a spatially flat metric

$$ds^2 = -dt^2 + \overset{\text{scale factor}}{a^2(t)} (dx^2 + dy^2 + dz^2) \quad a_0 = 1$$

- ▶ Large scales  $\rightarrow$  larger than the large scale structures  $\Rightarrow$  Universe is spatially homogeneous and isotropic
- ▶ Size of observable Universe  $\sim 14\text{Gpc}^*$ , our galaxy  $\sim 30\text{Kpc}$ , galaxy cluster  $\sim 1 - 10\text{Mpc}$ , galaxy super-cluster  $\sim 100\text{Mpc}$
- ▶ Small scales ( $\lesssim 100 - 300\text{Mpc}$ )  $\Rightarrow$  Universe is not so uniform  $\rightarrow$  start seeing the structures — galaxies, galaxy clusters, voids ...
- ▶ Large scale structures evolved from some initial **fluctuations**
- ▶ Evolution of fluctuations depend on background dynamics

**Goal:** If some dark energy models can provide a congenial environment for structure formation

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\*  $1\text{pc} = 3.0857 \times 10^{16}\text{m} = 3.26\text{lightyears}$

# Perturbations In A Scalar Field Model With Virtues Of $\Lambda$ CDM

# Scalar Field Model

(P. J. E. Peebles, B. Ratra, ApJL 1988, V. Sahni and A. A. Starobinsky, IJMPD 2000)

**Assume:** Cold dark matter (CDM) is like the perfect fluid distribution & a scalar field ( $\phi$ ) with a potential  $V(\phi)$  is acting as dark energy with

Kinetic:  $E_K$

► Energy density  $\Rightarrow \rho_\phi = \frac{1}{2a^2} \phi'^2 + V(\phi)$

► Pressure  $\Rightarrow p_\phi = \frac{1}{2a^2} \phi'^2 - V(\phi)$  Potential:  $E_P$

► EoS parameter  $\Rightarrow w_\phi = \frac{p_\phi}{\rho_\phi} = \frac{\frac{1}{2a^2} \phi'^2 - V(\phi)}{\frac{1}{2a^2} \phi'^2 + V(\phi)}$

► When  $E_K \gg E_P \Rightarrow$  scalar field behaves as a **stiff fluid** with  $w_\phi = 1$

► when  $E_P \gg E_K \Rightarrow$  scalar field behaves a **cosmological constant** with  $w_\phi = -1$

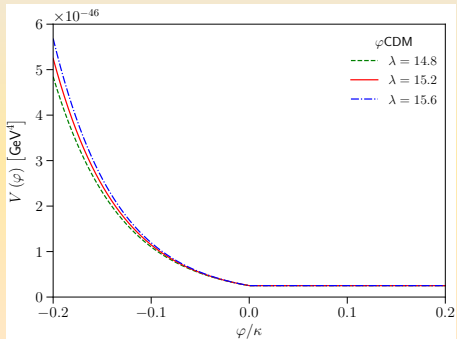
Klein-Gordon equation  $\Rightarrow \phi'' + 2\mathcal{H}\phi' + a^2 \frac{dV}{d\phi} = 0$

# Potential

$$V(\varphi) = V_0 e^{-\lambda \kappa \varphi} \Theta(-\varphi) + V_0 \Theta(\varphi),$$

$$\Theta(\varphi - \varphi_0) = \begin{cases} 0 & \text{for } \varphi < \varphi_0 \\ 1 & \text{for } \varphi \geq \varphi_0 \end{cases}$$

- **Free Parameter-1**  $\Rightarrow \lambda \rightarrow$  slope
- $\lambda$  **constrained** by BBN condition  $\Omega_\varphi(a \sim 10^{-10}) \lesssim 0.09$  (C. Wetterich, NPB 1988, E. J. Copeland *et al.*, PRD 1998)
- $V_0$  **depends** on  $\Omega_b h^2, \Omega_c h^2, H_0$
- $\Omega_{\varphi_0}$  **depends** on the height of the slow-roll region  $\rightarrow V_0$
- At late time  $w_\varphi = -1 \rightarrow$  **independent** of  $V_0$  or  $\lambda$  or initial conditions
- **Free Parameter-2**  $\Rightarrow \varphi_0 \rightarrow$  transition point
- Once in tracking region, evolution of  $\rho_\varphi$  is independent of  $\varphi_0 \rightarrow$  used  $\varphi_0 = 0$



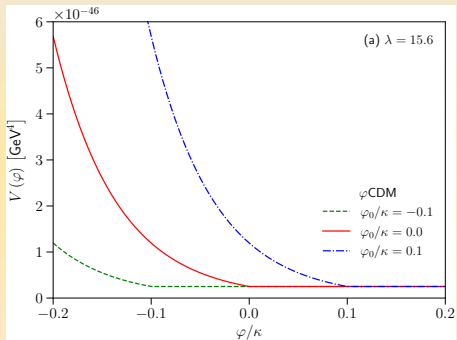
$$\lambda = 15.6 \rightarrow \Omega_\varphi(a \sim 10^{-10}) = 0.01642$$

$$V_0 = 2.510 \times 10^{-47} \text{ GeV}^4 \rightarrow \Omega_\varphi(a = 1) = 0.6840$$

# Potential

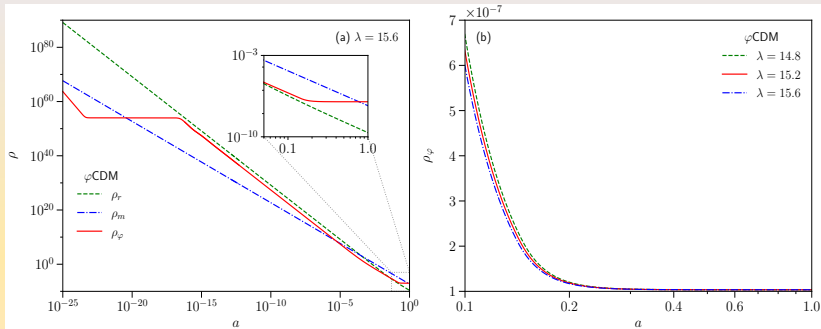
$$V(\varphi) = V_0 e^{-\lambda \kappa(\varphi - \varphi_0)} \Theta(-\varphi + \varphi_0) + V_0 \Theta(\varphi - \varphi_0),$$

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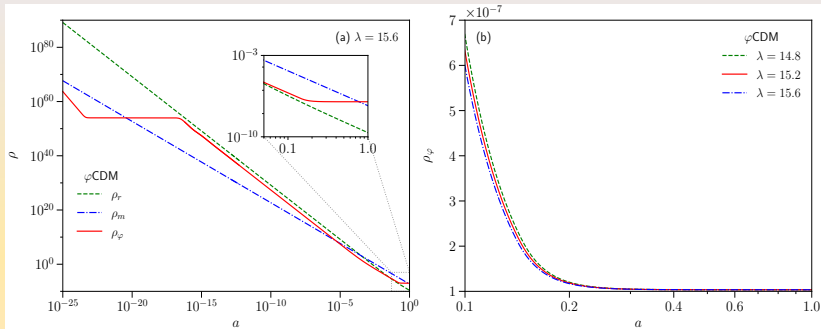
$V_0 e^{-\lambda \kappa \varphi} \rightarrow V_0 e^{-\lambda \kappa(\varphi - \varphi_0)}$  to accommodate for the continuity of  $V(\varphi)$

# Evolution Of Scalar Field



- (1)  $\phi$  rolls down the potential,  $E_K \gg E_P \implies \rho_\phi \propto a^{-6} \rightarrow \rho_\phi$  is dominated by  $E_K$

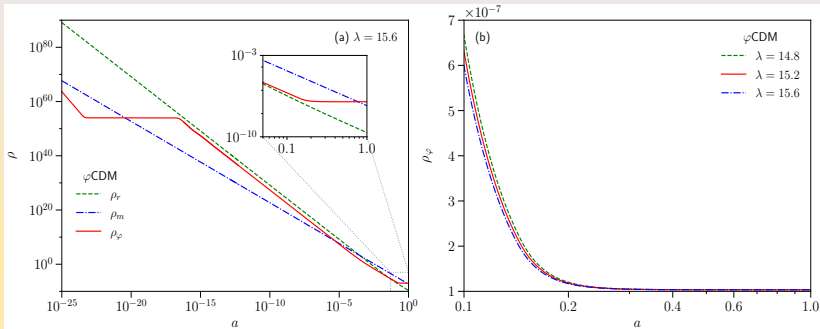
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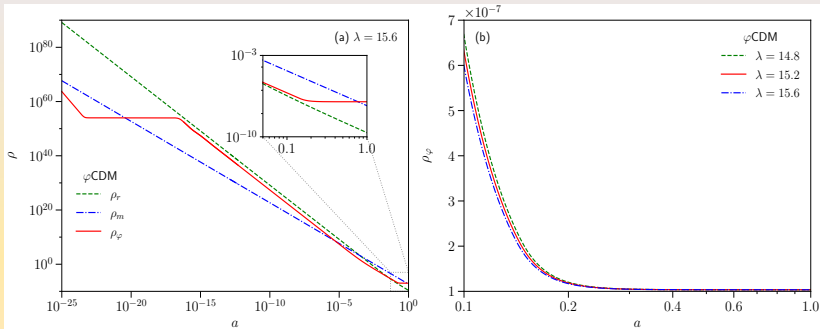


# Evolution Of Scalar Field



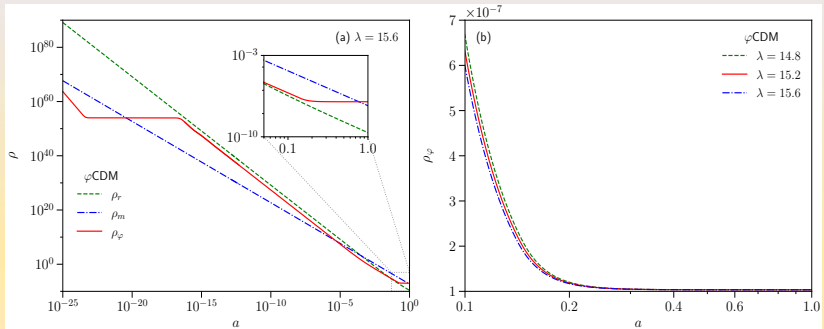
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- (5)  $V_0$  takes over  $\rightarrow \rho_\phi$  behaves like the cosmological constant

# Evolution Of Perturbations

- In synchronous gauge, perturbed metric takes the form (H. Kodama, M. Sasaki, *PTPS* 1984, C.-P. Ma, E. Bertschinger, *ApJ* 1995, K. A. Malik *et al.*, *PRD* 2003)

$$ds^2 = a^2(\tau) \left\{ -d\tau^2 + [(1 - 2\psi)\delta_{ij} + 2\partial_i\partial_j E] dx^i dx^j \right\}$$

- $\psi = \eta$  &  $k^2 E = -h/2 - 3\eta \rightarrow (\eta, h)$  are synchronous gauge fields in the Fourier space,  $k \rightarrow$  comoving wavenumber
- DM density contrasts  $\Rightarrow \delta_c = \delta\rho_c/\rho_c$ , DM velocity perturbation  $\Rightarrow v_c$
- Scalar field density contrasts  $\Rightarrow \delta_\phi = \delta\rho_\phi/\rho_\phi$
- Perturbed energy and momentum conservation equations are

$$\begin{aligned} \delta'_c + kv_c + \frac{h'}{2} &= 0 \\ v'_c + \mathcal{H}v_c &= 0 \end{aligned}$$

# Evolution Of Perturbations

- The perturbation  $\delta\varphi$  in the scalar field has the equation of motion (J. Martin, D. J. Schwarz, PRD 1998, P. Brax *et al.*, PRD 2000)

$$\delta\varphi'' + 2\mathcal{H}\delta\varphi' + k^2\delta\varphi + \alpha^2 \frac{d^2V}{d\varphi^2}\delta\varphi + \frac{1}{2}\varphi'h' = 0$$

$$\text{where, } \frac{d^2V}{d\varphi^2} \approx \frac{3}{2} \frac{\mathcal{H}^2}{a^2} \left[ -\frac{1}{2} (c_{s,\varphi}^2 - 1) (3c_{s,\varphi}^2 + 5) + \frac{\mathcal{H}'}{\mathcal{H}} (c_{s,\varphi}^2 - 1) \right]$$

- Adiabatic sound speed sq.  $\rightarrow c_{s,\varphi}^2 = 1 + \frac{2\alpha^2}{3\mathcal{H}\varphi'} \frac{dV}{d\varphi}$
- The perturbation in energy density  $\delta\rho_\varphi$  and pressure  $\delta p_\varphi$  are given as

$$\delta\rho_\varphi = -\delta T_{0(\varphi)}^0 = \frac{\varphi'\delta\varphi'}{a^2} + \delta\varphi \frac{dV}{d\varphi},$$

$$\delta T_{0(\varphi)}^j = -\frac{ik_j\varphi'\delta\varphi}{a^2}, \quad i \equiv \sqrt{-1}$$

$$\delta p_\varphi \delta_j^i = \delta T_{j(\varphi)}^i = \left( \frac{\varphi'\delta\varphi'}{a^2} - \delta\varphi \frac{dV}{d\varphi} \right) \delta_j^i,$$

# Evolution Of Perturbations

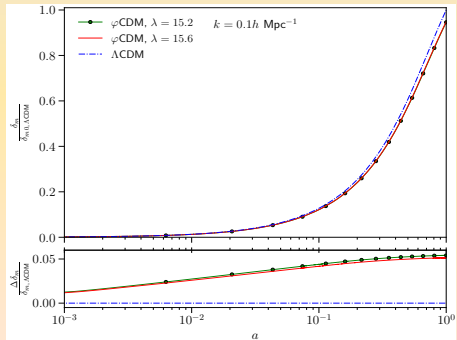
- Solved with adiabatic initial conditions
- Matter density contrast  $\Rightarrow \delta_m = \frac{\delta\rho_m}{\rho_m} = \frac{(\delta_c\rho_c + \delta_b\rho_b)}{(\rho_c + \rho_b)}$

• Evolution of  $\delta_m$  for  $\varphi$ CDM and  $\Lambda$ CDM

•  $\delta_m$  for both  $\varphi$ CDM and  $\Lambda$ CDM have been scaled by  $\delta_{m0} = \delta_m(a = 1)$  of  $\Lambda$ CDM

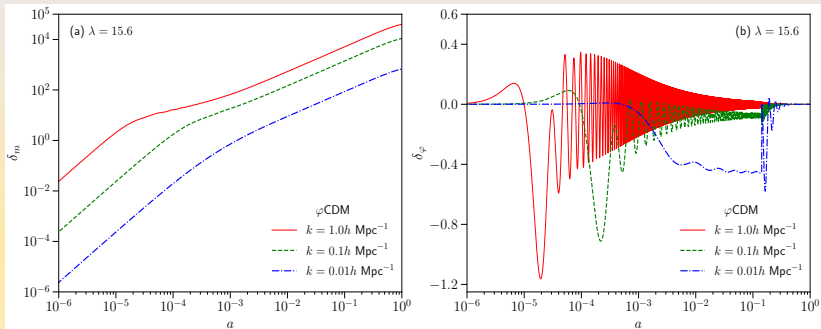
•  $\delta_m$  for  $\lambda = 15.2$  takes a slightly smaller value compared to that of  $\delta_m$  for  $\lambda = 15.6$

• Growth of  $\delta_m$  decreases with decrease in  $\lambda$



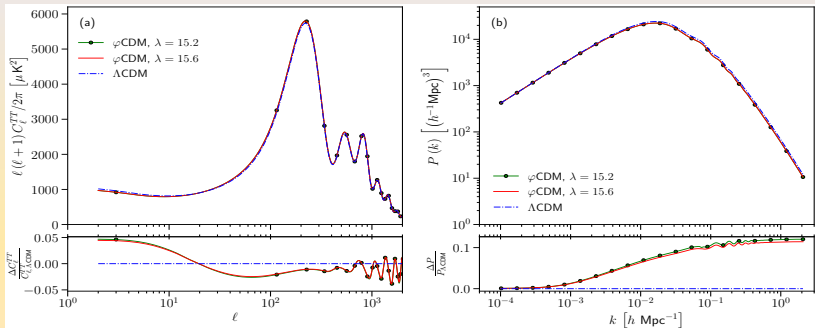
Note: For fractional change,  
 $\Delta\delta_m = (\delta_{m,\Lambda\text{CDM}} - \delta_m)$

# Evolution Of Perturbations



- In the matter dominated era, the modes of  $\delta_m$  grow in a very similar fashion
- The modes of  $\delta_\phi$  oscillate rapidly with decreasing amplitude after entering the horizon

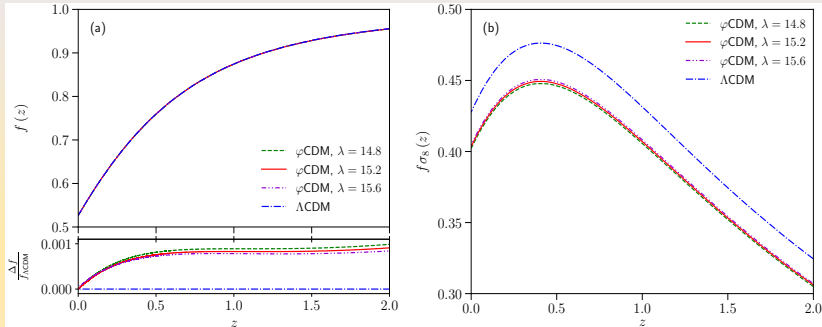
# Power Spectra



- $C_\ell^{TT}$  are almost independent of  $\lambda$
- Less matter  $\lambda$  content  $\Rightarrow$  higher oscillation amplitudes in  $C_\ell^{TT}$
- Smaller  $\lambda \Rightarrow$  slightly lower low- $\ell$  modes
- Larger  $\lambda \Rightarrow$  marginally lower  $P(k)$  at small scales



# Growth Rate



- $f = \frac{d \ln \delta_m}{d \ln a}$  is almost same for all the models at low redshift ( $z = \frac{1}{a} - 1$ )
- Smaller  $\lambda \Rightarrow$  lower  $f$
- Substantial difference in  $f\sigma_8$  for  $\varphi$ CDM and  $\Lambda$ CDM
- A low  $f\sigma_8 \rightarrow$  characteristic distinguishing feature

Model	$\lambda$	$\sigma_8$
$\varphi$ CDM	14.8	0.7638
	15.2	0.7664
	15.6	0.7687
$\Lambda$ CDM	—	0.8123

# Differentiating Interaction In The Dark Sector With Perturbation

# Motivation

- ▶ Interaction in the dark sector may not be ruled out *a priori*
- ▶ Question: **When** is the interaction significant in the evolution history of the Universe?
- ▶ Possibilities: **(a)** Interaction was there from the beginning of the Universe and exists through its evolution, **(b)** Interaction is a recent phenomenon **(c)** Interaction was entirely an early phenomenon and not at all present today
- ▶ An **evolving** coupling parameter instead of being a constant may answer

To assess if there is any stage of evolution when the interaction is significant

# Interaction In The Dark Sector

$$\rho'_C + 3\mathcal{H}\rho_C = -aQ \quad Q > 0: \text{DM} \rightarrow \text{DE}$$

cold dark matter

$$\rho'_{de} + 3\mathcal{H}(1 + w_{de})\rho_{de} = aQ \quad Q < 0: \text{DE} \rightarrow \text{DM}$$

dark energy

# Interaction In The Dark Sector

$$\rho'_C + 3\mathcal{H}\rho_C = -aQ$$

cold dark matter

$$\rho'_{de} + 3\mathcal{H}(1 + w_{de})\rho_{de} = aQ$$

dark energy

$$Q = \frac{\mathcal{H}\rho_{de}\beta(a)}{a}$$

- ▶ EoS of DE:  $w_{de} = w_0 + w_1(1 - a)$
- ▶ Ansatz for coupling parameter  $\beta(a)$  are :

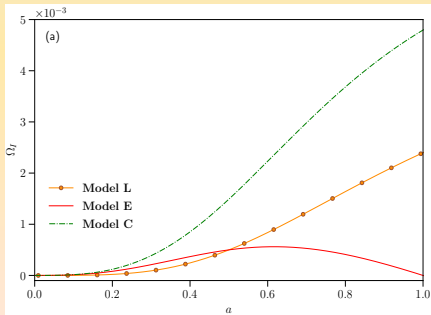
**Model L:** significant at late time  $\Rightarrow$

$$\beta(a) = \beta_0 \left( \frac{2a}{1+a} \right)$$

**Model E:** significant at early time  $\Rightarrow$

$$\beta(a) = \beta_0 \left( \frac{1-a}{1+a} \right)$$

**Model C:** a constant  $\Rightarrow$   $\beta(a) = \beta_0$



$$\Omega_i = \frac{Q}{3H^3/\kappa}, w_0 = -0.9995, w_1 = 0.005, \beta_0 = 0.007$$

# Evolution of Perturbations

- Perturbed energy and momentum conservation equations are

$$\delta'_c + kv_c + \frac{h'}{2} = \mathcal{H} \beta(a) \frac{\rho_{de}}{\rho_c} (\delta_c - \delta_{de})$$
$$v'_c + \mathcal{H} v_c = 0$$

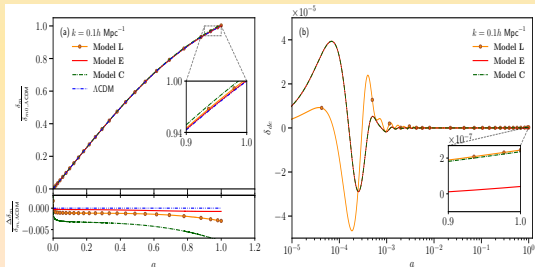
$$\delta'_{de} + 3\mathcal{H} (c_{s,de}^2 - w_{de}) \delta_{de} + (1 + w_{de}) \left( kv_{de} + \frac{h'}{2} \right)$$
$$+ 3\mathcal{H} \left[ 3\mathcal{H} (1 + w_{de}) (c_{s,de}^2 - w_{de}) \right] \frac{v_{de}}{k} + 3\mathcal{H} w'_{de} \frac{v_{de}}{k}$$
$$= 3\mathcal{H}^2 \beta(a) (c_{s,de}^2 - w_{de}) \frac{v_{de}}{k}$$

$$v'_{de} + \mathcal{H} (1 - 3c_{s,de}^2) v_{de} - \frac{k \delta_{de} c_{s,de}^2}{(1 + w_{de})} = \frac{\mathcal{H} \beta(a)}{(1 + w_{de})} \left[ v_c - (1 + c_{s,de}^2) v_{de} \right]$$

# Evolution of Perturbations

- Solved with adiabatic initial conditions
- To avoid the instability in dark energy perturbations  $\Rightarrow c_{s,de}^2 = 1$
- Matter density contrast  $\Rightarrow \delta_m = \frac{\delta\rho_m}{\rho_m} = \frac{(\delta_c\rho_c + \delta_b\rho_b)}{(\rho_c + \rho_b)}$

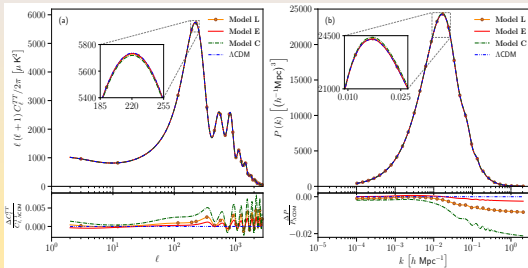
- $\delta_m$  for Model E evolves close to the  $\Lambda$ CDM model
- $\delta_m$  for Model L & Model C grow to a little higher value
- At early time,  $\delta_{de}$  oscillates and then decays to very small values
- Early time evolution of  $\delta_{de}$  in Model E is similar to Model C
- Late time evolution of  $\delta_{de}$  in Model L is similar to Model C



The origin on the x-axis is actually  $10^{-5}$

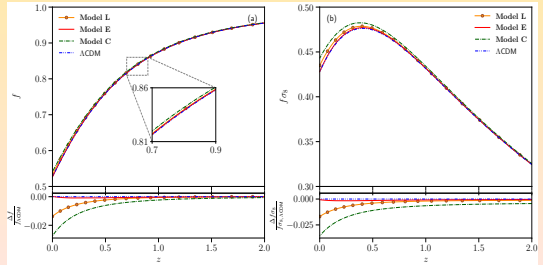
Note: For fractional change,  $\Delta\delta_m = (\delta_{m,\Lambda\text{CDM}} - \delta_m)$

# Power Spectra & Growth Rate



- ▶ Lower oscillation amplitudes in  $C_{\ell}^{TT} \rightarrow$  Model C < Model L < Model E <  $\Lambda$ CDM
- ▶ Less dark energy  $\Rightarrow$  less ISW effect  $\rightarrow$  Model C < Model L < Model E <  $\Lambda$ CDM
- ▶ Higher  $P(k) \rightarrow$  Model C > Model L > Model E >  $\Lambda$ CDM

- ▶ Model L & Model C have slightly higher values of  $f$  and  $f\sigma_8$  at  $z=0$
- ▶ Model E &  $\Lambda$ CDM have same values of  $f$  and  $f\sigma_8$  at  $z=0$
- ▶ Model E had a slightly larger value of  $f$  and  $f\sigma_8$  than  $\Lambda$ CDM, in the recent past





# Priors & Datasets

$$\mathcal{P} \equiv \{\Omega_b h^2, \Omega_c h^2, 100\theta_{MC}, \tau, \beta_0, w_0, w_1, \ln(10^{10} A_s), n_s\}$$

Parameter	Prior
$\Omega_b h^2$	[0.005, 0.1]
$\Omega_c h^2$	[0.001, 0.99]
$100\theta_{MC}$	[0.5, 10]
$\tau$	[0.01, 0.8]
$\beta_0$	[-1.0, 1.0]
$w_0$	[-0.9999, -0.3333]
$w_1$	[0.005, 1.0]
$\ln(10^{10} A_s)$	[1.61, 3.91]
$n_s$	[0.8, 1.2]

# Priors & Datasets

model  
parameters

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**Planck:** CMB anisotropies measurements from *Planck* 2018 collaboration (*Planck* TT, TE, EE + lowE + lensing) (N. Aghanim *et al.* (*Planck* Collaboration), *A&A* 2020)

**BAO:** distance measurements from **(a)** 6dFGS at  $z = 0.106$  (F. Beutler, *MNRAS* 2011), **(b)** SDSS-MGS at  $z = 0.15$  (A. J. Ross, *MNRAS* 2015) & **(c)** DR12 of BOSS-SDSS III at  $z = 0.38, 0.51$  and  $0.61$  (S. Alam *et al.*, *MNRAS* 2017)

**Pantheon:** 'Pantheon' catalogue for the luminosity distance measurements of the Type Ia supernovae (SNe Ia) (D. M. Scolnic *et al.*, *ApJ* 2018)

**RSD:**  $f\sigma_8$  data compilation (S. Nesseris, *PRD* 2017, B. Sagredo *et al.*, *PRD* 2018, F. Skara & L. Perivolaropoulos, *PRD* 2020)

# Redshift Space Distortion Data

Survey	$z$	$f\sigma_8(z)$	$\Omega_m$	Refs.
6dFGS+Snlc	0.02	$0.428 \pm 0.0465$	0.3	(D. Huterer <i>et al.</i> , JCAP 2017)
Snlc+IRAS	0.02	$0.398 \pm 0.065$	0.3	(S. J. Turnbull <i>et al.</i> , MNRAS 2017, M. J. Hudson <i>et al.</i> , ApJL 2012)
2MASS	0.02	$0.314 \pm 0.048$	0.266	(M. Davis <i>et al.</i> , MNRAS 2011, M. J. Hudson <i>et al.</i> , ApJL 2012)
SDSS-veloc	0.10	$0.370 \pm 0.130$	0.3	(M. Feix <i>et al.</i> , PRL 2015)
SDSS-MGS	0.15	$0.490 \pm 0.145$	0.31	(C. Howlett <i>et al.</i> , MNRAS 2015)
2dFGRS	0.17	$0.510 \pm 0.060$	0.3	(Y.-S. Song <i>et al.</i> , JCAP 2009)
GAMA	0.18	$0.360 \pm 0.090$	0.27	(C. Blake <i>et al.</i> , MNRAS 2013)
GAMA	0.38	$0.440 \pm 0.060$		(C. Blake <i>et al.</i> , MNRAS 2013)
SDSS-LRG-200	0.25	$0.3512 \pm 0.0583$	0.25	(L. Samushia <i>et al.</i> , MNRAS 2012)
SDSS-LRG-200	0.37	$0.4602 \pm 0.0378$		(L. Samushia <i>et al.</i> , MNRAS 2012)
BOSS-LOWZ	0.32	$0.384 \pm 0.095$	0.274	(A. G. Sánchez <i>et al.</i> , MNRAS 2014)
SDSS-CMASS	0.59	$0.488 \pm 0.060$	0.307115	(C.-H. Chuang <i>et al.</i> , MNRAS 2016)
WiggleZ	0.44	$0.413 \pm 0.080$	0.27	(C. Blake <i>et al.</i> , MNRAS 2012)
WiggleZ	0.60	$0.390 \pm 0.063$	$\mathbf{C}_{\text{WiggleZ}}$	(C. Blake <i>et al.</i> , MNRAS 2012)
WiggleZ	0.73	$0.437 \pm 0.072$		(C. Blake <i>et al.</i> , MNRAS 2012)
VIPERS PDR-2	0.60	$0.550 \pm 0.120$	0.3	(A. Pezzotta <i>et al.</i> , A&A 2017)
VIPERS PDR-2	0.86	$0.400 \pm 0.110$		(A. Pezzotta <i>et al.</i> , A&A 2017)
FastSound	1.40	$0.482 \pm 0.116$	0.27	(T. Okumura <i>et al.</i> , PASJ 2016)
SDSS-IV	0.978	$0.379 \pm 0.176$	0.31	(G.-B. Zhao <i>et al.</i> , MNRAS 2018)
SDSS-IV	1.23	$0.385 \pm 0.099$	$\mathbf{C}_{\text{SDSS-IV}}$	(G.-B. Zhao <i>et al.</i> , MNRAS 2018)
SDSS-IV	1.526	$0.342 \pm 0.070$		(G.-B. Zhao <i>et al.</i> , MNRAS 2018)
SDSS-IV	1.944	$0.364 \pm 0.106$		(G.-B. Zhao <i>et al.</i> , MNRAS 2018)
VIPERS PDR2	0.60	$0.49 \pm 0.12$	0.31	(F. G. Mohammad <i>et al.</i> , A&A 2018)
VIPERS PDR2	0.86	$0.46 \pm 0.09$		(F. G. Mohammad <i>et al.</i> , A&A 2018)
BOSS DR12 voids	0.57	$0.501 \pm 0.051$	0.307	(S. Nadathur <i>et al.</i> , PRD 2019)
2MTF 6dFGSv	0.03	$0.404 \pm 0.0815$	0.3121	(F. Qin <i>et al.</i> , MNRAS 2019)
SDSS-IV	0.72	$0.454 \pm 0.139$	0.31	(M. Icoza-Lizola <i>et al.</i> , MNRAS 2019)

$\Omega_m \rightarrow$  corresponding fiducial cosmology used to convert redshift to distance

# Redshift Space Distortion

- ▶ The anisotropic red-shift space clustering of galaxies along the line-of-sight due to non-negligible galaxy peculiar velocities  $\Rightarrow$  **Redshift-space distortion (RSD)**
- ▶ Likelihood  $\mathcal{L} \propto e^{-\chi^2/2}$ , where  $\chi^2 = V^i \mathbf{C}_{ij}^{-1} V^j$
- ▶ For RSD data  $\rightarrow \chi_{f\sigma_8}^2 = V_{f\sigma_8}^i \mathbf{C}_{ij, f\sigma_8}^{-1} V_{f\sigma_8}^j$ , where

$$\mathbf{C}_{ij, f\sigma_8} = \begin{pmatrix} \sigma_1^2 & 0 & \dots & 0 & \dots & 0 \\ 0 & \sigma_2^2 & \dots & 0 & \dots & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 0 & 0 & \dots & \mathbf{C}_{\text{WiggleZ}} & \dots & 0 \\ 0 & 0 & \dots & 0 & \mathbf{C}_{\text{SDSS-IV}} & 0 \\ 0 & 0 & \dots & 0 & \dots & \sigma_N^2 \end{pmatrix} \quad \mathbf{C}_{\text{WiggleZ}} = 10^{-3} \begin{pmatrix} 6.400 & 2.570 & 0.000 \\ 2.570 & 3.969 & 2.540 \\ 0.000 & 2.540 & 5.184 \end{pmatrix},$$

$$\mathbf{C}_{\text{SDSS-IV}} = 10^{-2} \begin{pmatrix} 3.098 & 0.892 & 0.329 & -0.021 \\ 0.892 & 0.980 & 0.436 & 0.076 \\ 0.329 & 0.436 & 0.490 & 0.350 \\ -0.021 & 0.076 & 0.350 & 1.124 \end{pmatrix}$$

- ▶ For vector  $V_{f\sigma_8}^i \rightarrow$  the theoretical predictions ( $f\sigma_8^{\text{th}}$ ) are divided by a correction term  $\mathcal{R}$

$$V_{f\sigma_8}^i(z_i, \mathcal{P}) \equiv f\sigma_{8,i}^{\text{obs}} - \frac{f\sigma_8^{\text{th}}(z_i, \mathcal{P})}{\mathcal{R}(z_i)}, \quad \mathcal{R} \rightarrow \text{Alcock-Paczyński (AP) correction}$$

# Alcock-Paczyński (AP) Effect

- ▶ The anisotropies due to incorrect fiducial cosmology while converting the relative redshifts to comoving coordinates  $\Rightarrow$  **Alcock-Paczyński (AP) effect**  
(Alcock & Paczyński, Nature 1979, E. Macaulay *et al.*, PRL 2013)

- ▶ Distance between two galaxies for true model

$$dL_{\perp} = (1+z)D_A(z)d\theta, \quad dL_{\parallel} = \frac{cdz}{H(z)}$$

- ▶ Distance between two galaxies for fiducial model

$$dL_{\perp}^{\text{fid}} = (1+z)D_A^{\text{fid}}(z)d\theta = \left(\frac{D_A^{\text{fid}}}{D_A}\right)dL_{\perp}, \quad dL_{\parallel}^{\text{fid}} = \frac{cdz}{H^{\text{fid}}(z)} = \left(\frac{H}{H^{\text{fid}}}\right)dL_{\parallel}$$

- ▶ Amount of anisotropy included is

$$F = \left(\frac{H^{\text{fid}}}{H}\right) \left(\frac{D_A^{\text{fid}}}{D_A}\right)$$

- ▶ The corrected observed quantity is (B. Sagredo *et al.*, PRD 2018, L. Kazantzidis & L. Perivolaropoulos, PRD 2018, F. Skara & L. Perivolaropoulos, PRD 2020)

$$f\sigma_8(z) \simeq \frac{H(z)D_A(z)}{H^{\text{fid}}(z)D_A^{\text{fid}}(z)} f\sigma_8^{\text{fid}}(z) \equiv \mathcal{R}(z, \Omega_{0m}, \Omega_{0m}^{\text{fid}}) f\sigma_8^{\text{fid}}(z)$$

# Observational constraints

Presence of interaction for a brief period in the evolutionary history  $\implies$  **Model E**  $\longrightarrow$  describes the evolutionary history of the Universe better than Model L & Model C

# Observational constraints

Parameter	<i>Planck</i>	<i>Planck</i> + $f\sigma_8$	<i>Planck</i> + BAO	<i>Planck</i> + BAO + Pantheon	<i>Planck</i> + BAO + Pantheon + $f\sigma_8$
$\Omega_b h^2$	$0.022358 \pm 0.000165$	$0.022490 \pm 0.000162$	$0.022489 \pm 0.000156$	$0.022500 \pm 0.000152$	$0.022546 \pm 0.000151$
$\Omega_c h^2$	$0.12008 \pm 0.00126$	$0.11848 \pm 0.00117$	$0.11850 \pm 0.00101$	$0.118405 \pm 0.000970$	$0.117845 \pm 0.000909$
$100\theta_{MC}$	$1.040769 \pm 0.000324$	$1.040941 \pm 0.000318$	$1.040941 \pm 0.000313$	$1.040945 \pm 0.000315$	$1.040999 \pm 0.000313$
$\tau$	$0.05466^{+0.00699}_{-0.00779}$	$0.05630^{+0.00703}_{-0.00797}$	$0.05704^{+0.00704}_{-0.00792}$	$0.05697 \pm 0.00749$	$0.05778^{+0.00700}_{-0.00790}$
$\beta_0$	$0.0339 \pm 0.0372$	$0.0395 \pm 0.0381$	$0.0432 \pm 0.0376$	$0.0448 \pm 0.0377$	$0.0446 \pm 0.0370$
$w_0$	$< -0.914$	$< -0.977$	$< -0.969$	$< -0.981$	$< -0.985$
$w_1$	$< 0.168$	$< 0.0645$	$< 0.0707$	$< 0.0604$	$< 0.0489$
$\ln(10^{10} A_s)$	$3.0486 \pm 0.0147$	$3.0488 \pm 0.0148$	$3.0509 \pm 0.0148$	$3.0507 \pm 0.0144$	$3.0511 \pm 0.0146$
$n_s$	$0.96315 \pm 0.00453$	$0.96681 \pm 0.00434$	$0.96652 \pm 0.00419$	$0.96672 \pm 0.00418$	$0.96802 \pm 0.00404$
$H_0$ [km s <sup>-1</sup> Mpc <sup>-1</sup> ]	$64.12^{+2.40}_{-1.39}$	$67.00^{+1.02}_{-0.702}$	$66.787^{+0.775}_{-0.600}$	$67.200^{+0.577}_{-0.516}$	$67.631 \pm 0.516$
$\Omega_m$	$0.3492^{+0.0149}_{-0.0282}$	$0.31569^{+0.00834}_{-0.0114}$	$0.31765^{+0.00678}_{-0.00812}$	$0.31353^{+0.00590}_{-0.00658}$	$0.30842 \pm 0.00588$
$\sigma_8$	$0.7836^{+0.0221}_{-0.0138}$	$0.80265^{+0.00992}_{-0.00800}$	$0.8019^{+0.0102}_{-0.00866}$	$0.80539 \pm 0.00830$	$0.80573 \pm 0.00774$



1-D marginalised values with errors at  $1\sigma$  (68% Confidence Level) for **Model E**



# Observational constraints

Parameter	<i>Planck</i>	<i>Planck</i> + $f\sigma_8$	<i>Planck</i> + BAO	<i>Planck</i> + BAO + Pantheon	<i>Planck</i> + BAO + Pantheon + $f\sigma_8$
$\Omega_b h^2$	$0.022358 \pm 0.000165$	$0.022490 \pm 0.000162$	$0.022489 \pm 0.000156$	$0.022500 \pm 0.000152$	$0.022546 \pm 0.000151$
$\Omega_c h^2$	$0.12008 \pm 0.00126$	$0.11848 \pm 0.00117$	$0.11850 \pm 0.00101$	$0.118405 \pm 0.000970$	$0.117845 \pm 0.000909$
$100\theta_{MC}$	$1.040769 \pm 0.000324$	$1.040941 \pm 0.000318$	$1.040941 \pm 0.000313$	$1.040945 \pm 0.000315$	$1.040999 \pm 0.000313$
$\tau$	$0.05466^{+0.00699}_{-0.00779}$	$0.05630^{+0.00703}_{-0.00797}$	$0.05704^{+0.00704}_{-0.00792}$	$0.05697 \pm 0.00749$	$0.05778^{+0.00700}_{-0.00790}$
$\beta_0$	$0.0339 \pm 0.0372$	$0.0395 \pm 0.0381$	$0.0432 \pm 0.0376$	$0.0448 \pm 0.0377$	$0.0446 \pm 0.0370$
$w_0$	$< -0.914$	$< -0.977$	$< -0.969$	$< -0.981$	$< -0.985$
$w_1$	$< 0.168$	$< 0.0645$	$< 0.0707$	$< 0.0604$	$< 0.0489$
$\ln(10^{10} A_s)$	$3.0486 \pm 0.0147$	$3.0488 \pm 0.0148$	$3.0509 \pm 0.0148$	$3.0507 \pm 0.0144$	$3.0511 \pm 0.0146$
$n_s$	$0.96315 \pm 0.00453$	$0.96681 \pm 0.00434$	$0.96652 \pm 0.00419$	$0.96672 \pm 0.00418$	$0.96802 \pm 0.00404$
$H_0$ [km s <sup>-1</sup> Mpc <sup>-1</sup> ]	$64.12^{+2.40}_{-1.39}$	$67.00^{+1.02}_{-0.702}$	$66.787^{+0.775}_{-0.600}$	$67.200^{+0.577}_{-0.516}$	$67.631 \pm 0.516$
$\Omega_m$	$0.3492^{+0.0149}_{-0.0282}$	$0.31569^{+0.00834}_{-0.0114}$	$0.31765^{+0.00678}_{-0.00812}$	$0.31353^{+0.00590}_{-0.00658}$	$0.30842 \pm 0.00588$
$\sigma_8$	$0.7836^{+0.0221}_{-0.0138}$	$0.80265^{+0.00992}_{-0.00800}$	$0.8019^{+0.0102}_{-0.00866}$	$0.80539 \pm 0.00830$	$0.80573 \pm 0.00774$

- 👉  $\beta_0 > 0 \Rightarrow$  Energy flows from DM  $\rightarrow$  DE
- 👉 For *Planck* data,  $\beta_0 = 0$  lies within the  $1\sigma$  error region
- 👉 For other datasets,  $\beta_0 = 0$  lies outside the  $1\sigma$  error region
- 👉  $w_0$  and  $w_1$  are unconstrained


# Observational constraints

Parameter	<i>Planck</i>	<i>Planck</i> + $f\sigma_8$	<i>Planck</i> + BAO	<i>Planck</i> + BAO + Pantheon	<i>Planck</i> + BAO + Pantheon + $f\sigma_8$
$\Omega_b h^2$	$0.022358 \pm 0.000165$	$0.022490 \pm 0.000162$	$0.022489 \pm 0.000156$	$0.022500 \pm 0.000152$	$0.022546 \pm 0.000151$
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$100\theta_{MC}$	$1.040769 \pm 0.000324$	$1.040941 \pm 0.000318$	$1.040941 \pm 0.000313$	$1.040945 \pm 0.000315$	$1.040999 \pm 0.000313$
$\tau$	$0.05466^{+0.00699}_{-0.00779}$	$0.05630^{+0.00703}_{-0.00797}$	$0.05704^{+0.00704}_{-0.00792}$	$0.05697 \pm 0.00749$	$0.05778^{+0.00700}_{-0.00790}$
$\beta_0$	$0.0339 \pm 0.0372$	$0.0395 \pm 0.0381$	$0.0432 \pm 0.0376$	$0.0448 \pm 0.0377$	$0.0446 \pm 0.0370$
$w_0$	$< -0.914$	$< -0.977$	$< -0.969$	$< -0.981$	$< -0.985$
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$n_s$	$0.96315 \pm 0.00453$	$0.96681 \pm 0.00434$	$0.96652 \pm 0.00419$	$0.96672 \pm 0.00418$	$0.96802 \pm 0.00404$
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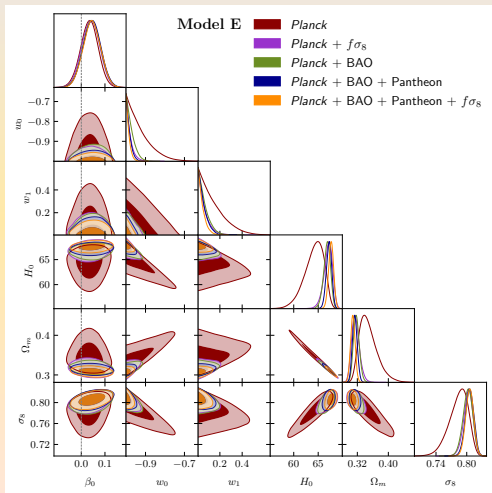
- Derived parameters,  $H_0$ ,  $\Omega_m$  and  $\sigma_8$  are also listed
- For *Planck* data, central value of  $H_0$  is small and error bars are high
- For *Planck* data,  $\sigma_8$  is skewed towards the galaxy cluster value of  $\sigma_8 = 0.77^{+0.04}_{-0.03}$
- Addition of datasets, changes the central values and decreases the error bars

# Observational constraints

Parameter	<i>Planck</i>	<i>Planck</i> + $f\sigma_8$	<i>Planck</i> + BAO	<i>Planck</i> + BAO + Pantheon	<i>Planck</i> + BAO + Pantheon + $f\sigma_8$
$\Omega_b h^2$	$0.022358 \pm 0.000165$	$0.022490 \pm 0.000162$	$0.022489 \pm 0.000156$	$0.022500 \pm 0.000152$	$0.022546 \pm 0.000151$
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$\tau$	$0.05466^{+0.00699}_{-0.00779}$	$0.05630^{+0.00703}_{-0.00797}$	$0.05704^{+0.00704}_{-0.00792}$	$0.05697 \pm 0.00749$	$0.05778^{+0.00700}_{-0.00790}$
$\beta_0$	$0.0339 \pm 0.0372$	$0.0395 \pm 0.0381$	$0.0432 \pm 0.0376$	$0.0448 \pm 0.0377$	$0.0446 \pm 0.0370$
$w_0$	$< -0.914$	$< -0.977$	$< -0.969$	$< -0.981$	$< -0.985$
$w_1$	$< 0.168$	$< 0.0645$	$< 0.0707$	$< 0.0604$	$< 0.0489$
$\ln(10^{10} A_s)$	$3.0486 \pm 0.0147$	$3.0488 \pm 0.0148$	$3.0509 \pm 0.0148$	$3.0507 \pm 0.0144$	$3.0511 \pm 0.0146$
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$H_0$ [km s <sup>-1</sup> Mpc <sup>-1</sup> ]	$64.12^{+2.40}_{-1.39}$	$67.00^{+1.02}_{-0.702}$	$66.787^{+0.775}_{-0.600}$	$67.200^{+0.577}_{-0.516}$	$67.631 \pm 0.516$
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$\sigma_8$	$0.7836^{+0.0221}_{-0.0138}$	$0.80265^{+0.00992}_{-0.00800}$	$0.8019^{+0.0102}_{-0.00866}$	$0.80539 \pm 0.00830$	$0.80573 \pm 0.00774$

 For all the combined datasets, the values shift towards the *Planck*  $\Lambda$ CDM values

# Observational constraints



# Comparison

Parameter	Model L	Model E	Model C
$\beta_0$	$0.00788 \pm 0.00815$	$0.0339 \pm 0.0372$	$0.00624 \pm 0.00673$
$w_0$	$< -0.909$	$< -0.914$	$< -0.907$
$w_1$	$< 0.174$	$< 0.168$	$< 0.174$
$H_0$	$63.98^{+2.45}_{-1.47}$	$64.12^{+2.40}_{-1.39}$	$63.93^{+2.51}_{-1.44}$
$\Omega_m$	$0.3507^{+0.0157}_{-0.0292}$	$0.3492^{+0.0149}_{-0.0282}$	$0.3513^{+0.0153}_{-0.0299}$
$\sigma_8$	$0.7825^{+0.0228}_{-0.0141}$	$0.7836^{+0.0221}_{-0.0138}$	$0.7821^{+0.0232}_{-0.0140}$

Compared w.r.t. *Planck* data

- ▶ Model L and Model C have very close parameter central values
- ▶ Model E has larger  $\beta_0$  compared to Model L and Model C
- ▶ Model E has larger  $H_0$ ,  $\sigma_8$  & smaller  $\Omega_m$  compared to Model L and Model C

# When

## From Perturbation Analysis

- Evolution of growth rate, CMB temperature spectrum and matter power spectrum show Model E behaves **closely** as the  $\Lambda$ CDM model
- Model E performs **better** than Model L and Model C in describing the evolutionary history of the Universe.

# When

## From Perturbation Analysis

- Evolution of growth rate, CMB temperature spectrum and matter power spectrum show Model E behaves closely as the  $\Lambda$ CDM model
- Model E performs better than Model L and Model C in describing the evolutionary history of the Universe.

Interaction, if present, is likely to be significant only at some early stage of evolution of the Universe

# Summary & Conclusion

- Scalar field with a potential that drives the recent acceleration like the cosmological constant starting from arbitrary initial conditions
  - The evolution of perturbations is similar to the  $\Lambda$ CDM model
- Considered 'evolving' coupling parameter for interaction
  - **(a)** interaction is a more recent phenomenon &
  - (b)** interaction is a phenomenon in the distant past
    - Early interaction describes the evolution of the perturbations better than the late interaction



Thank You

Extra

# Power Spectra & Growth Rate

$$C_\ell^{\mathcal{P}} = \frac{2}{k} \int k^2 dk P_\zeta(k) \Delta_{T\ell}^2(k)$$

$$P(k, a) = A_s k^{n_s} T^2(k) D^2(a)$$

$$f(a) = \frac{d \ln \delta_m}{d \ln a}$$

$$\sigma_8(a) = \sigma_8(1) \frac{\delta_m(a)}{\delta_m(1)}$$

$$f \sigma_8(a) \equiv f(a) \sigma_8(a)$$