

Constraining Cosmic Reionization with 21cm & Fast Radio Bursts

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21cm cosmology constraints, based on paper with the HERA Collaboration & Theory team
(especially Julian B. Muñoz, Jordan Mirocha, and Yuxiang Qin):

HERA Phase I Limits on the Cosmic 21-cm Signal: Constraints on Astrophysics and Cosmology During the Epoch of Reionization
[ApJ 924 51, [arXiv 2108.07282](#)]

Fast Radio Burst forecast, based on paper with Nina Sartorio, Anastasia Fialkov & Duncan Lorimer

What it takes to Measure Reionization with Fast Radio Bursts
[[arXiv 2107.14242](#)]

Two ways to probe the era of reionization

21cm – probing neutral hydrogen in the Universe

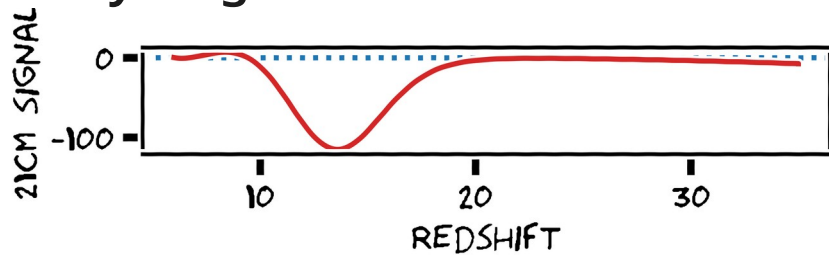


Foto credit: HERA

FRBs – radio bursts that probe the ionized medium

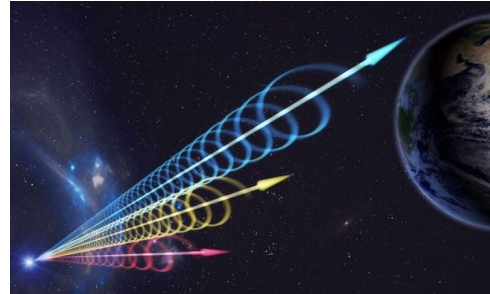


Image credit: Jingchuan Yu, Beijing Planetarium



Foto credit: Absolute Cosmos

Reionization – the missing piece in the cosmological puzzle

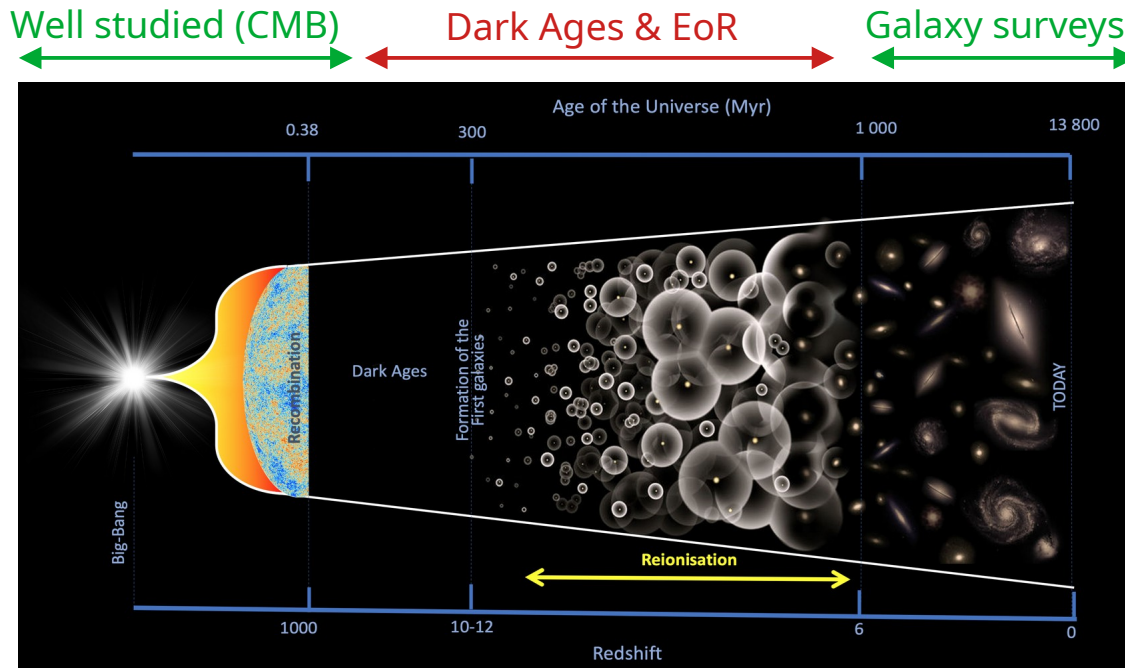


Image credit: Nicolas Laporte

Cosmological standard model
(Planck analysis incl. BAO):

$$\ln A_s \pm 0.5\%$$

$$n_s \pm 0.4\%$$

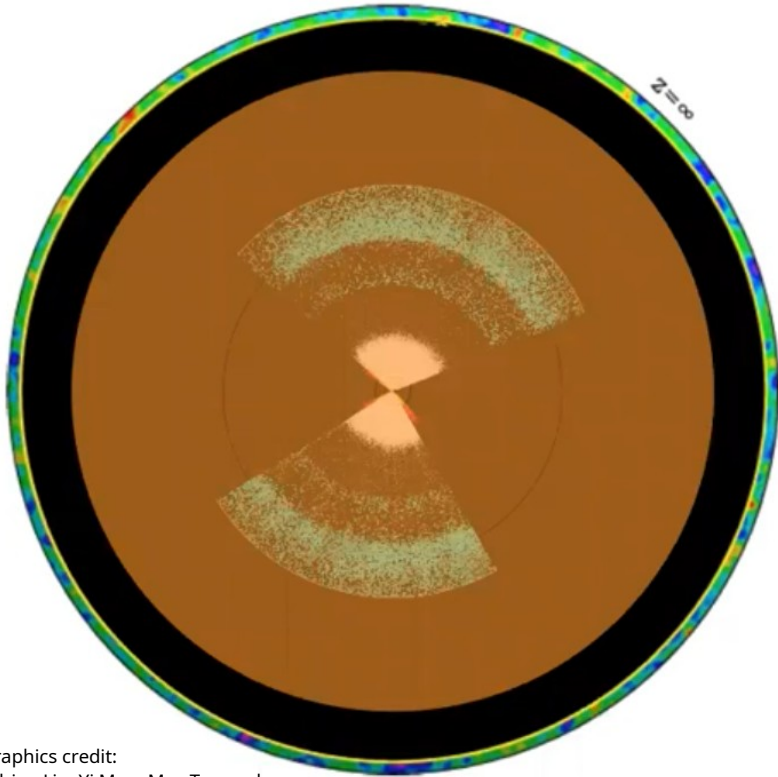
$$\Omega_m h^2 \pm 0.6\%$$

$$\Omega_b h^2 \pm 0.6\%$$

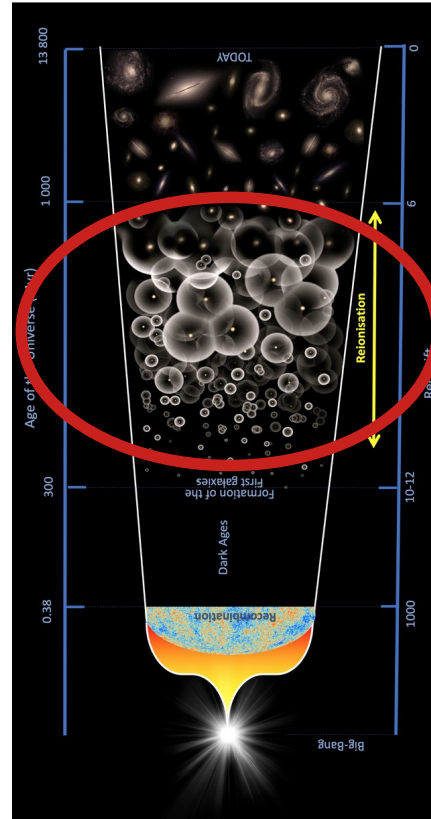
$$H_0 \pm 0.6\%*$$

$$\tau \pm 12\%$$

21-cm Cosmology



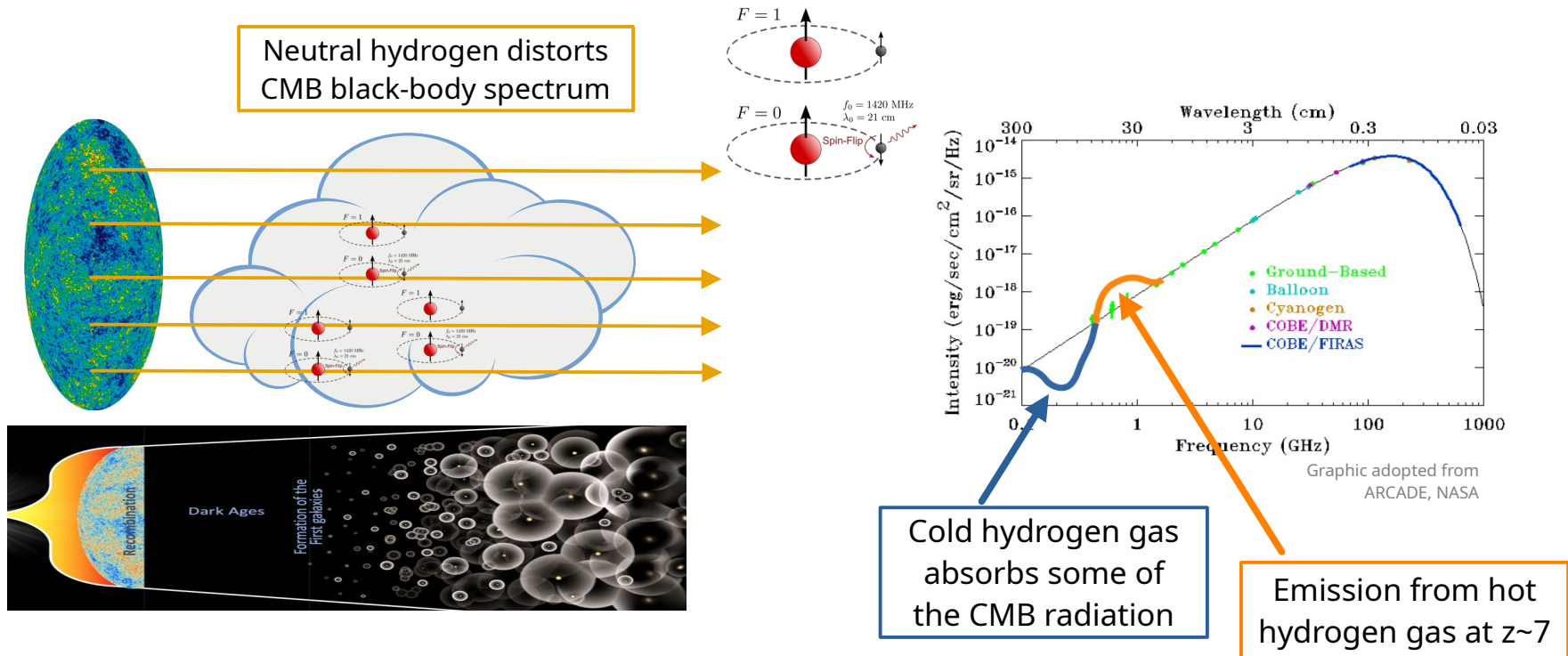
Graphics credit:
Adrian Liu, Yi Mao, Max Tegmark



Graphics credit: Nicolas Laporte

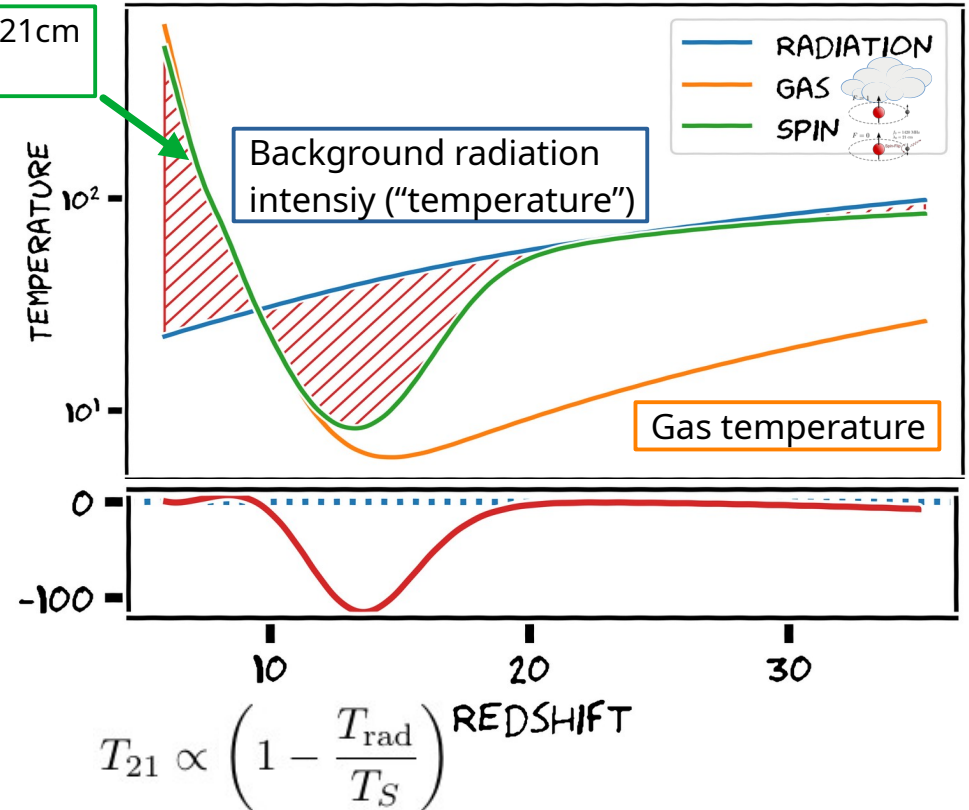
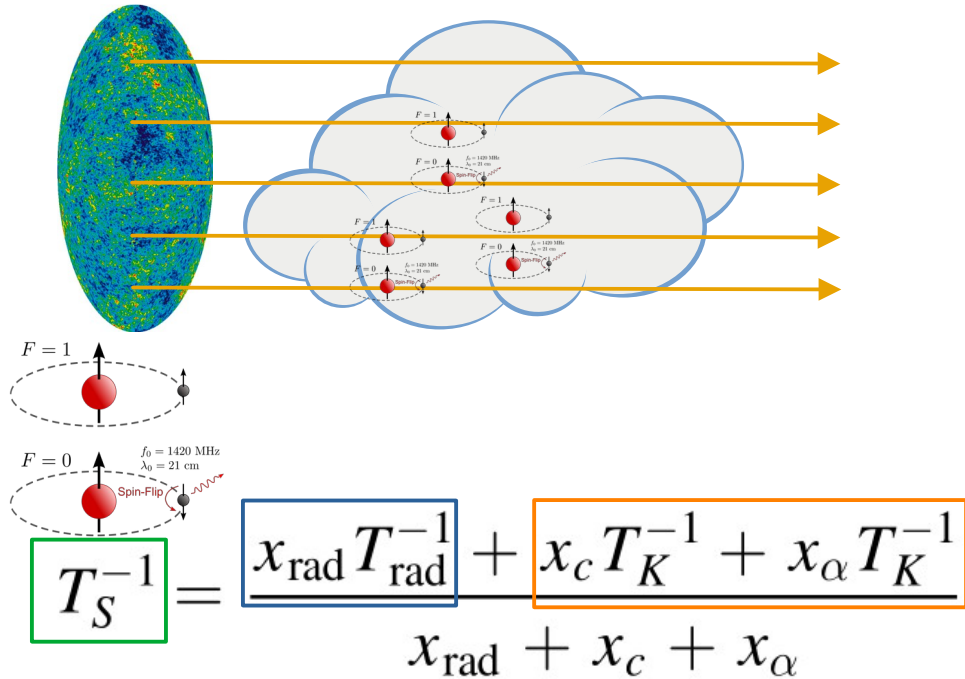
Observe all the Hydrogen
in the Universe, from
redshift $z=6$ to ~ 100
(in principle)

The 21cm signal

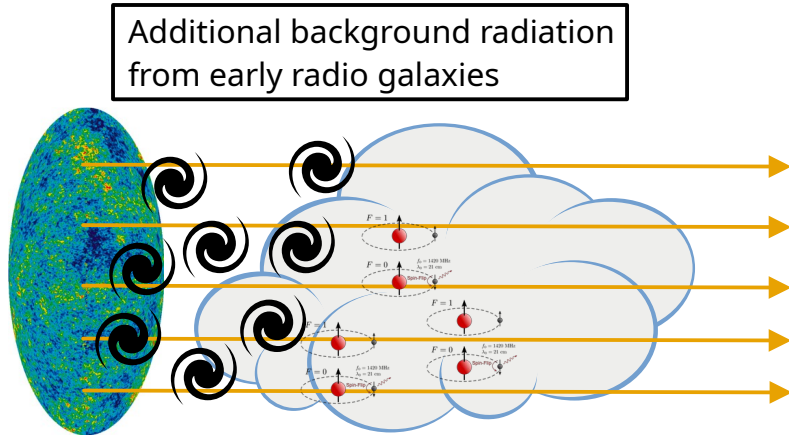


The spin temperature

Spin distribution ("temperature") of neutral hydrogen determines 21cm absorption/emission. Coupled to gas temperature and radiation.

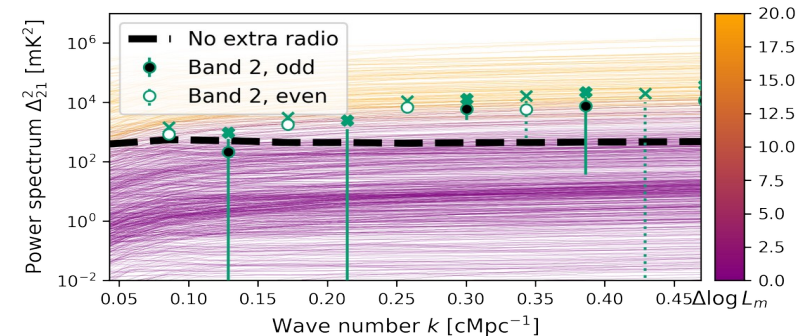
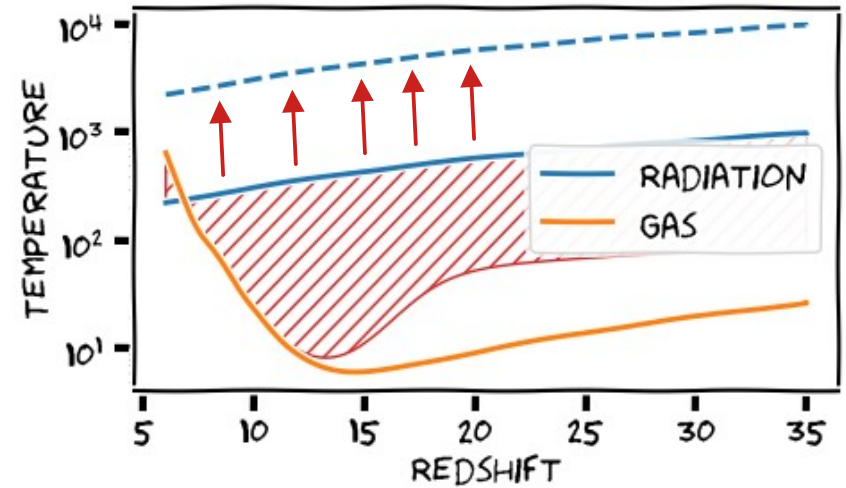


Radio backgrounds

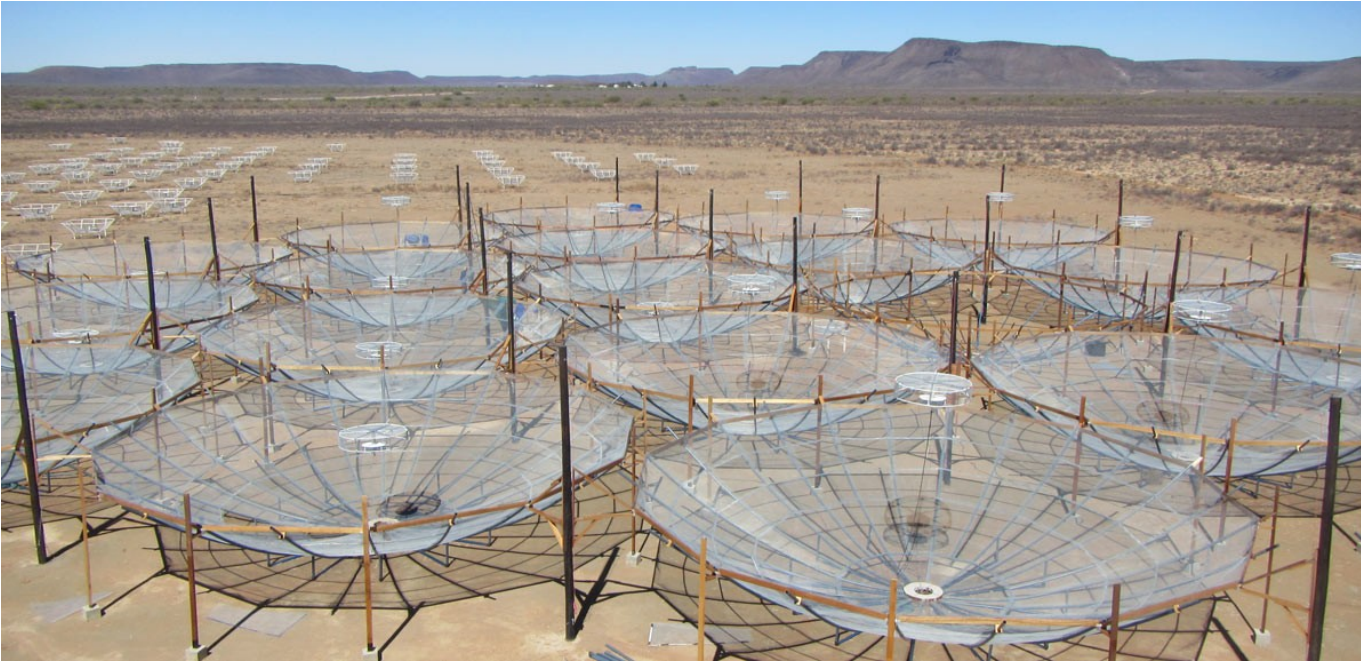


Extra radio background from

- Early galaxies \sim SFR
- Exotic sources \sim Synchrotron



The HERA radio interferometer

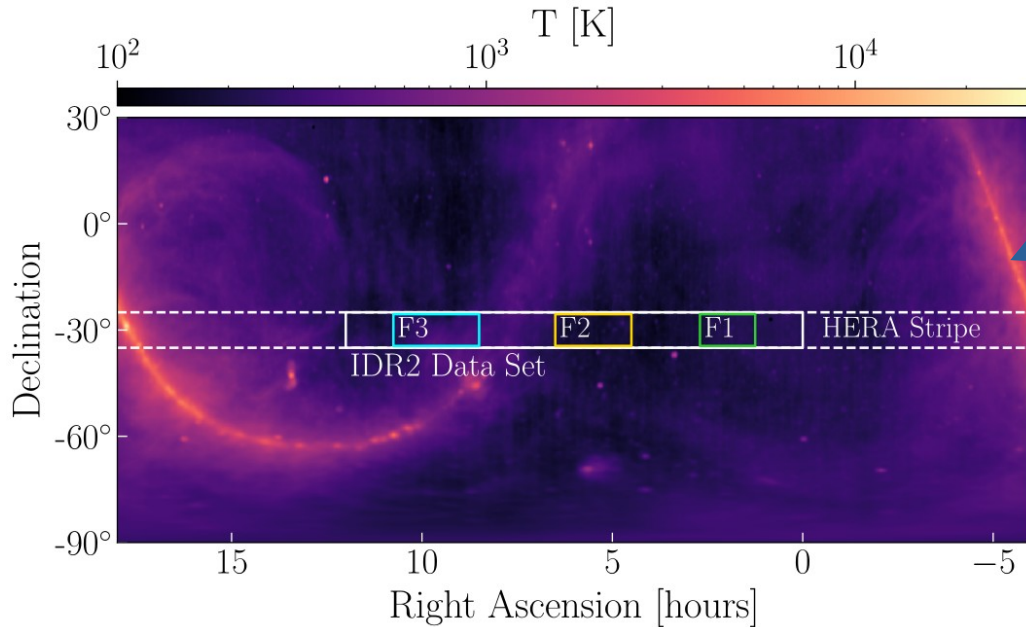


Hydrogen Epoch of Reionization Array, Karoo desert, South Africa

This data: 39 science-quality antennas operational

Foto credit: HERA

21cm signal & foregrounds



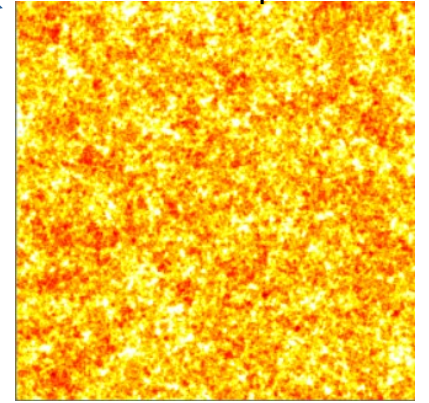
Driftscan observations of sky, 18 nights

(Figure: HERA Collaboration 2021a)

Foregrounds: Much brighter than cosmological signal ($<1K$), but spectrally smooth

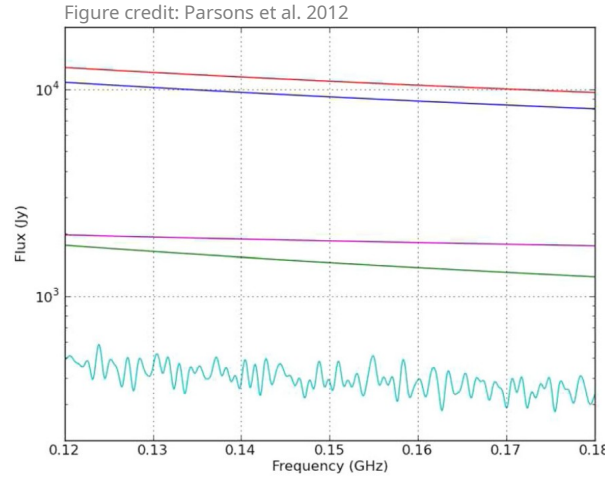
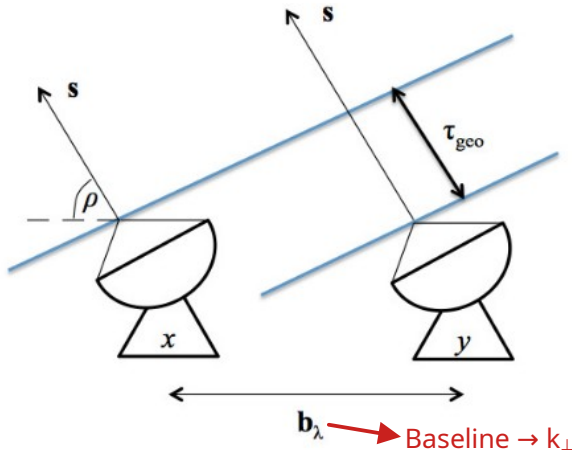
21cm signal not smooth in redshift

Simulation snapshot:



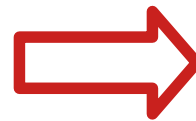
(Figure: HERA Collaboration 2021b)

What do we measure? Baselines & delays



Interferometer

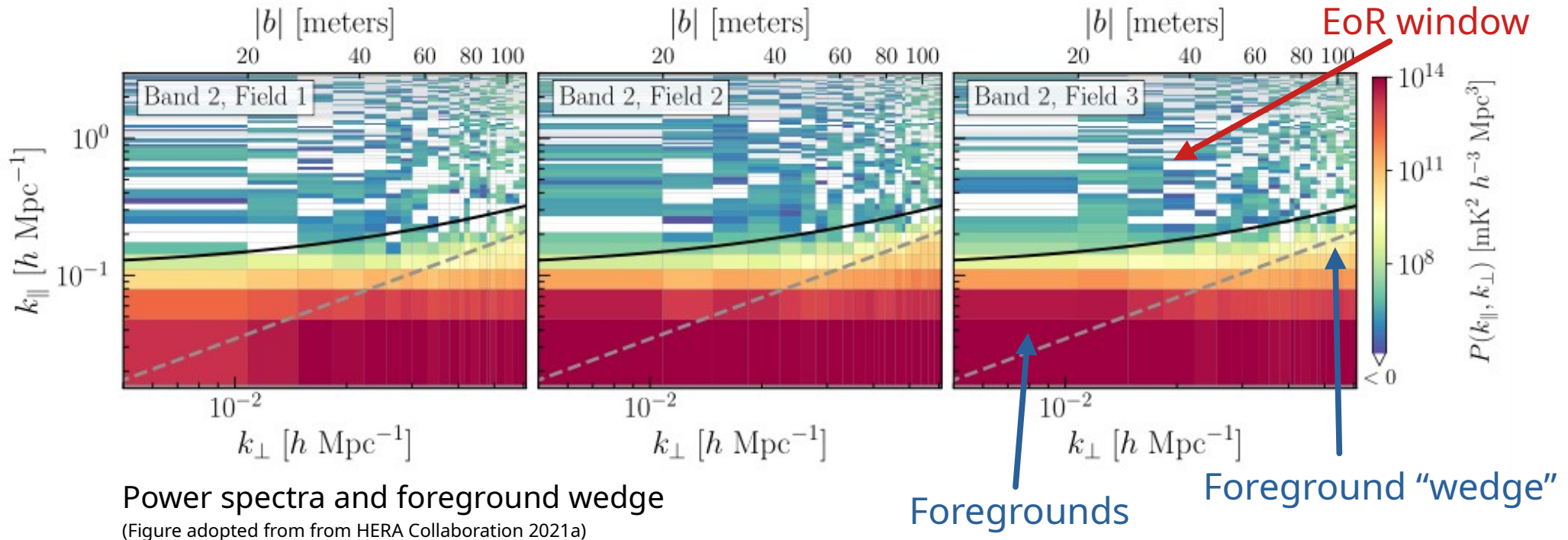
- Baseline $\sim k_\perp$
- Frequency $\sim k_\parallel$



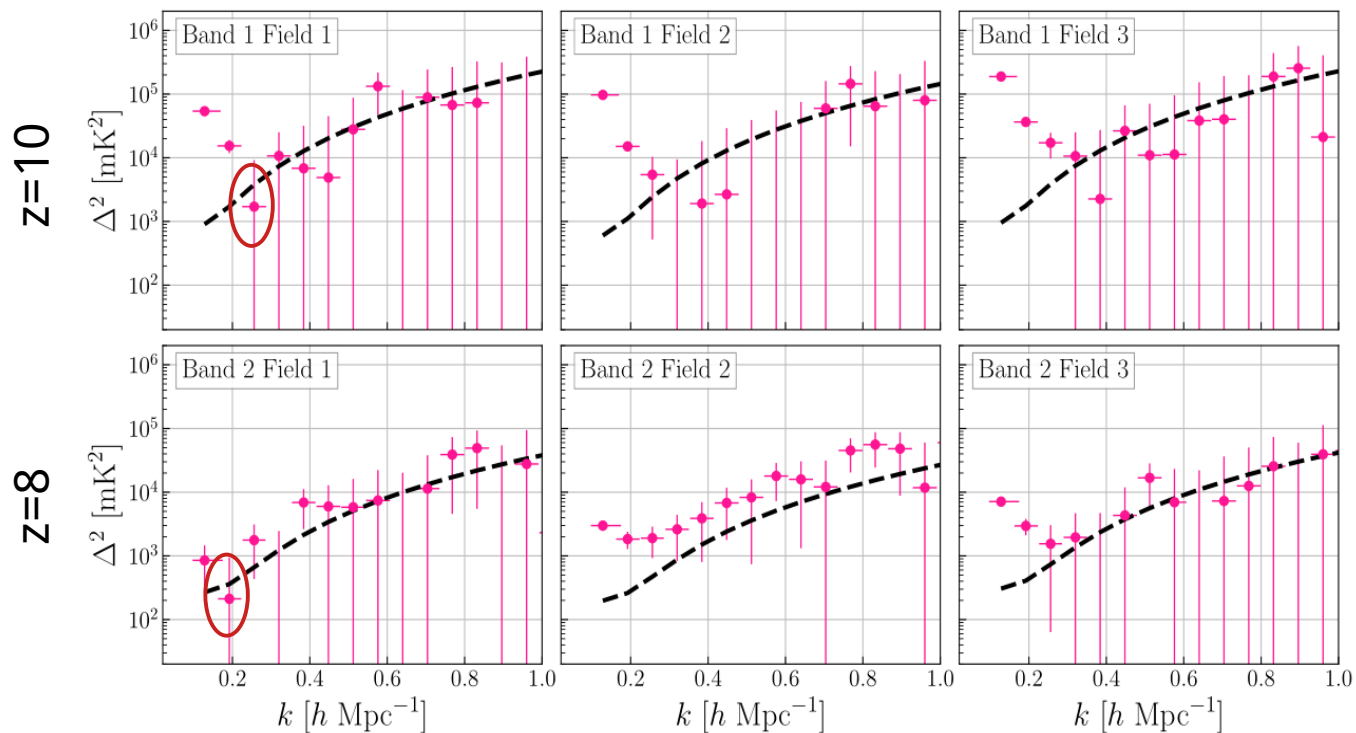
Cylindrical power spectrum $P(k_\perp, k_\parallel)$

Graphics credit: Avison & George, arXiv 1211.0228

The 21cm signal EoR window



21cm power spectrum



$$\Delta^2(k) = \frac{k^3 P(k)}{2\pi^2}$$

(Figure: HERA Collaboration 2021a)

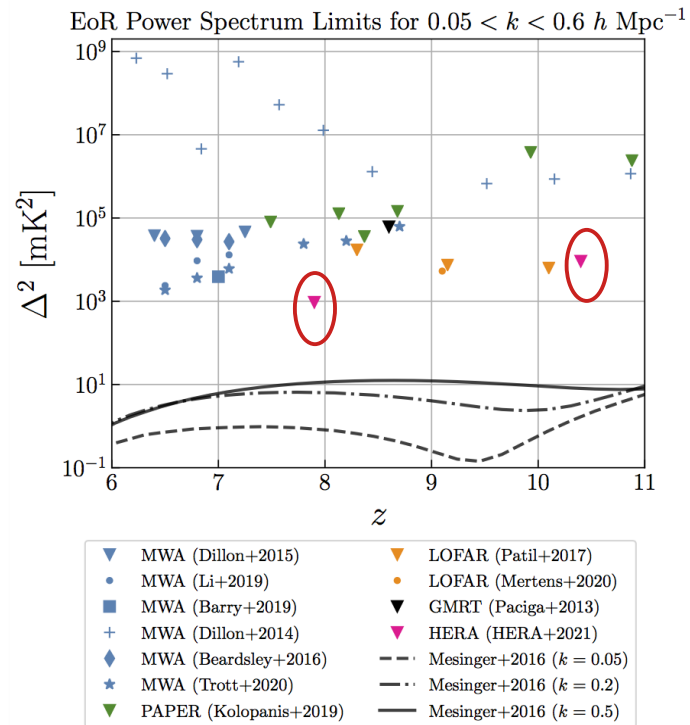


Figure: HERA (<http://reionization.org/science/public-data-release-1/>)

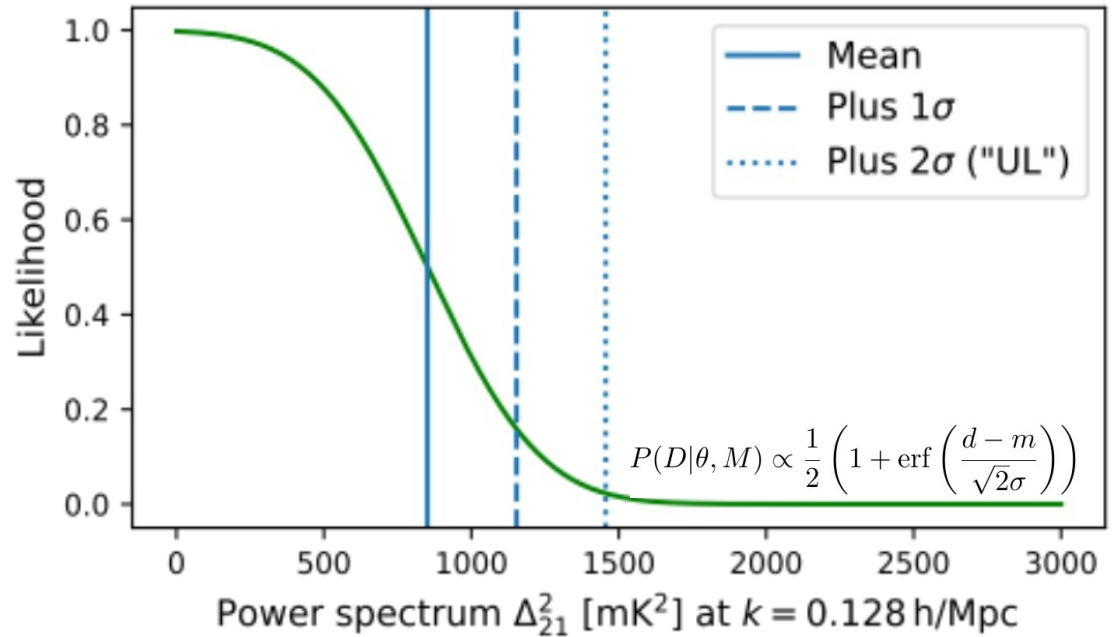
What do we mean by an "upper limit"?

k $h \text{ Mpc}^{-1}$	Δ^2 $(\text{mK})^2$	1σ $(\text{mK})^2$	Δ_{UL}^2 $(\text{mK})^2$
0.128	$(29.17)^2$	$(17.39)^2$	$(38.16)^2$
0.192	$(14.55)^2$	$(19.17)^2$	$(30.76)^2$

**Measurement ($14^2 \pm 19^2 \text{ mK}^2$) =
Cosmological + Systematics**

→ Cosmological signal anywhere
between 0 and measurement

Δ^2 $(\text{mK})^2$	1σ $(\text{mK})^2$	Δ_{UL}^2 $(\text{mK})^2$
$(29.17)^2$	$(17.39)^2$	$(38.16)^2$
$(14.55)^2$	$(19.17)^2$	$(30.76)^2$



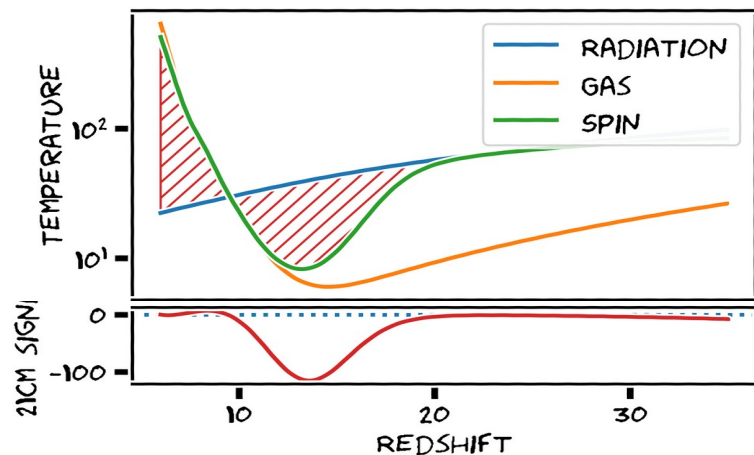
Intuitive interpretation of HERA limits

(lead by Julian B. Muñoz)

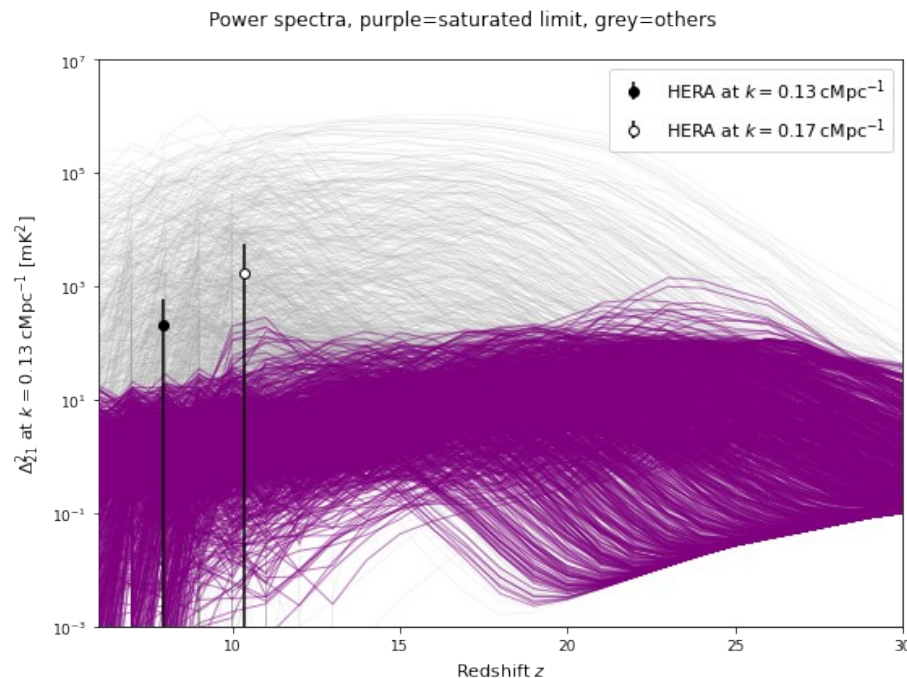
$$T_{21} \propto \left(1 - \frac{T_{\text{rad}}}{T_S}\right)$$

Positive: Emission,
saturated at ~30 mK

Negative: Absorption,
up to 100% in principle



Emission not yet detectable:



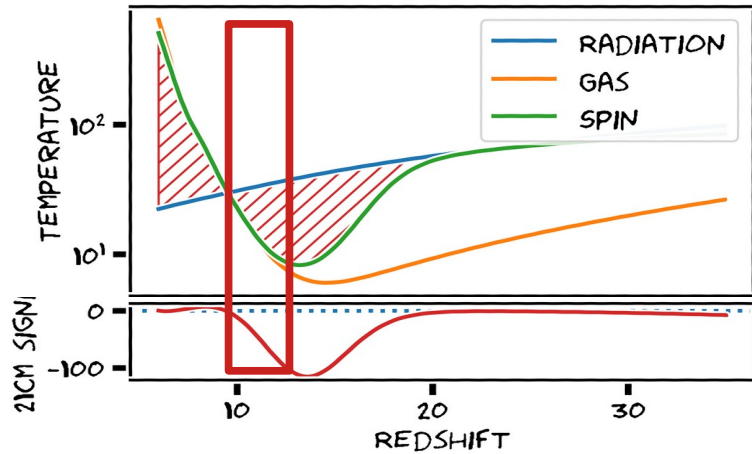
Intuitive interpretation of HERA limits

(lead by Julian B. Muñoz)

If 21cm PS traces matter power spectrum (“bias approach”)

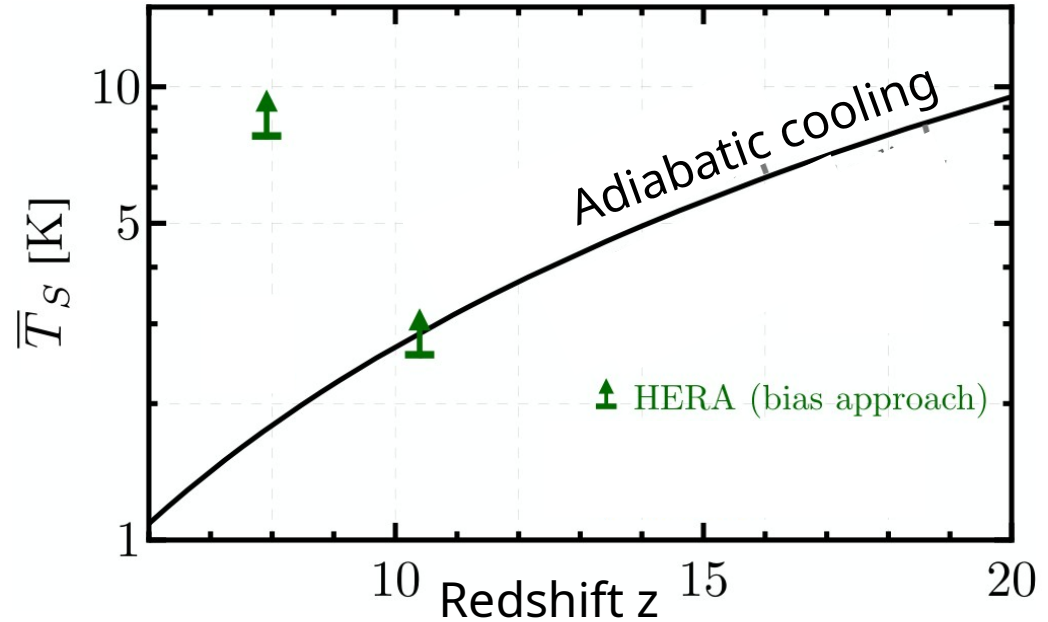
$$\Delta_{21}^2(k, z) = b_m^2(z) \Delta_m^2(k, z)$$

$$b_m = T_0 x_{\text{HI}} \left\{ (1 + \mu) - \frac{T_{\text{rad}}}{\bar{T}_S} [(1 + \mu) - C_T] \right\}$$



Absorption:

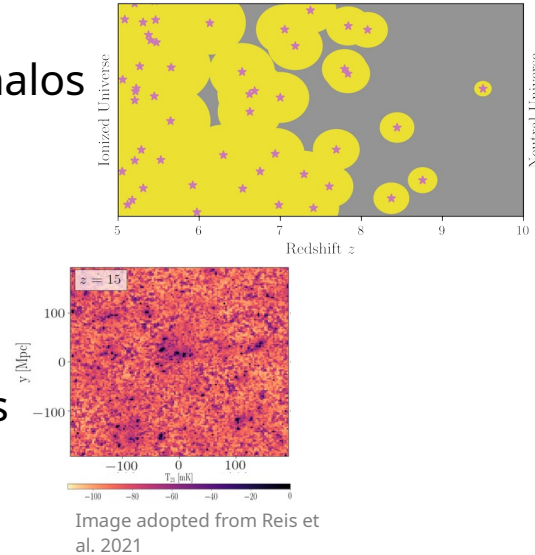
Upper limit on $|T_{21}| \rightarrow$ Lower limit on T_S/T_{rad}



Seminumerical codes (Mesinger et al. & Fialkov et al.)

Numerical simulations: $(384 \text{ cMpc})^3$ size, 3 cMpc cells

- Evolve density field & identify star-forming halos (parameterized by M_{min} or V_c)
- Model emission of UV, X-Ray, Radio, LyA etc.
 - (parameterized by τ , f_x , f_r , f_*)
- Compute 21cm brightness temperature fields and derive power spectra



Parameters
 $(V_c \tau f_* f_x f_r)$



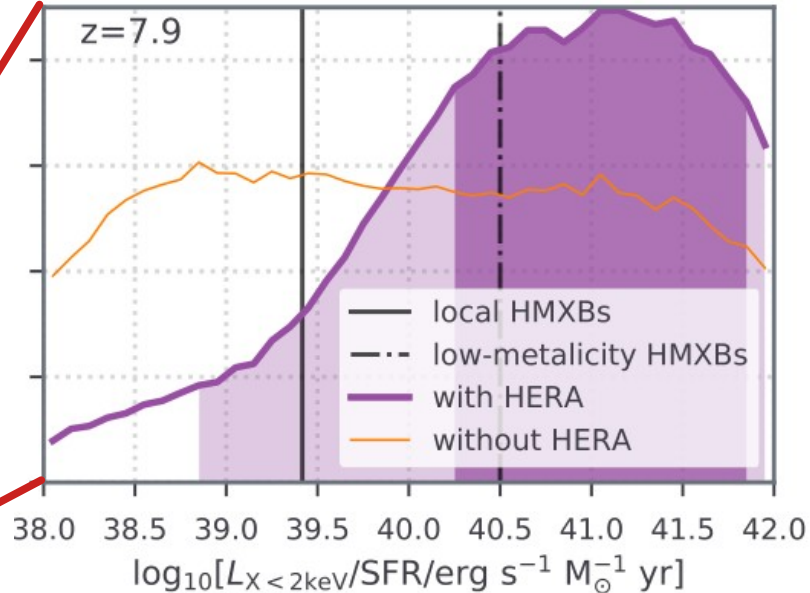
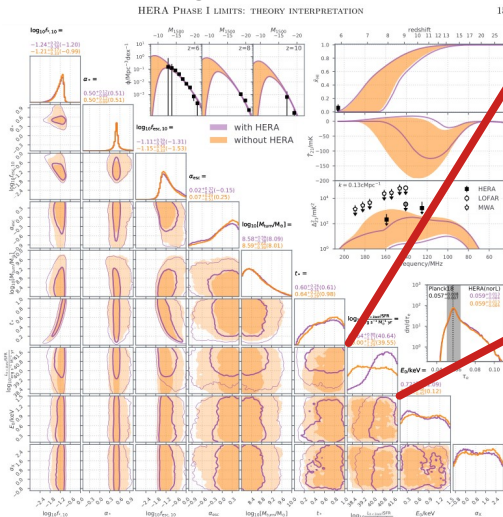
Power spectrum $\Delta^2_{21\text{cm}}(\mathbf{k}, z)$

HERA improving complementary constraints

(lead by Yuxiang Qin, with Bradley Greig and Andrei Mesinger)

HERA

- + CMB optical depth
- + QSO Dark Fraction
- + Galaxy UV LF



- **Constraints on galaxies X-ray luminosity**
 - Slightly disfavour X-ray faint galaxies
(CMB-only radio background)

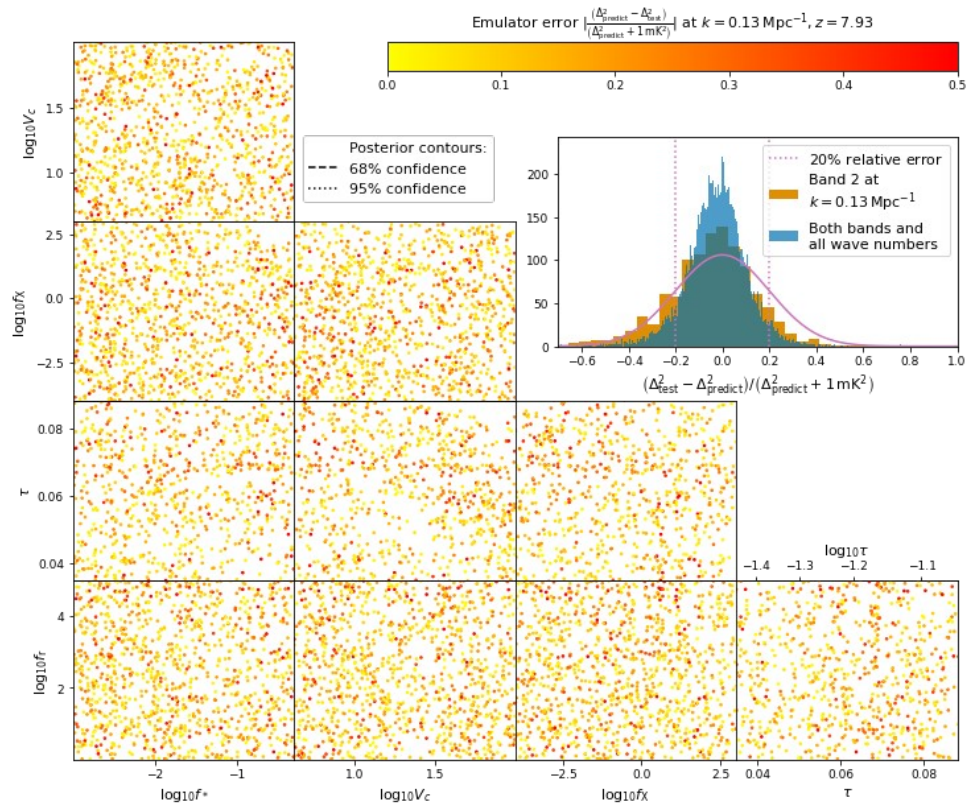
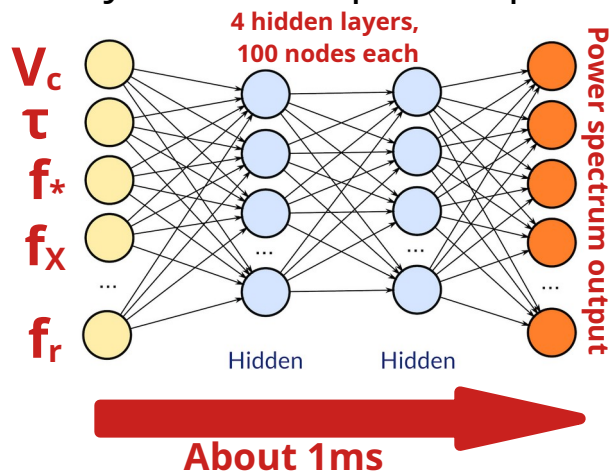
Note: This uses a different numerical code (21cmFAST) → Slightly different parameterization

Emulator for Fialkov et al.'s simulations

(lead by S.H., with Anastasia Fialkov)

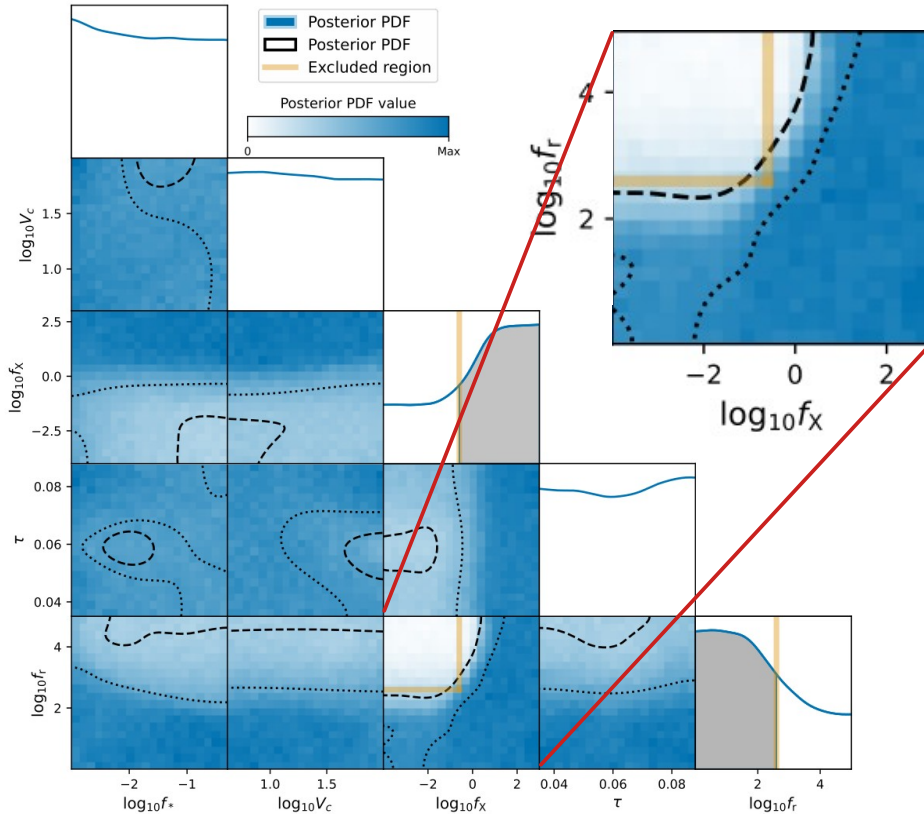
Neural network

- Use to “emulate” simulation. i.e. effectively interpolate between existing simulations
- 10,000 simulations in 5D parameter space
- Uncertainty ca. 20% of power spectrum



Constraints from HERA limits (alone) on models

(lead by S.H., with Anastasia Fialkov)



Rule out cold IGM together with strong radio background

- Preference for high f_x and low f_r , models with both, *low f_x and high f_r* are *excluded* ($f_x < 25\%$ today's X-ray efficiency, $f_r > 400$ times today's radio emissivity)
- Similar constraints: Low f_x with *synchrotron radio background* $> 5 \times \text{CMB}$ (large, but lower than ARCADE 2 limits, $50 \times \text{CMB}$, Fixsen et al. 2011) ruled out

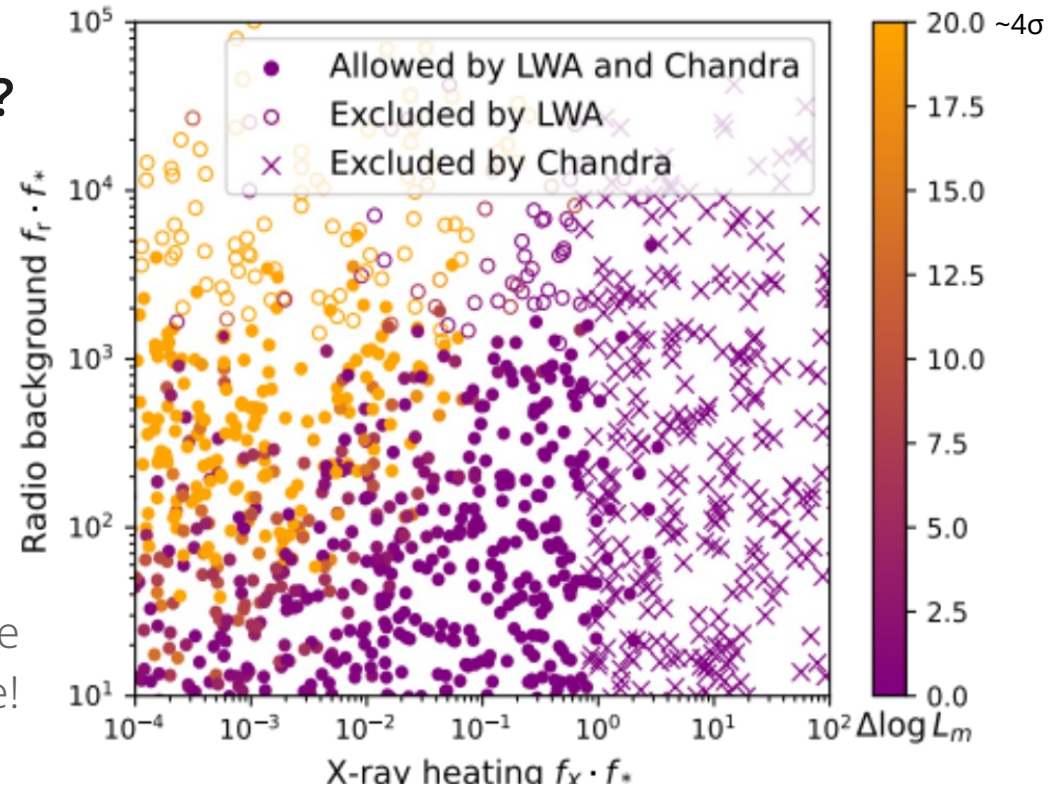
Reality check: Compatible at all with X-ray / radio today?

(lead by S.H., with Anastasia Fialkov)

Are these models consistent with observed radio- and X-ray background?

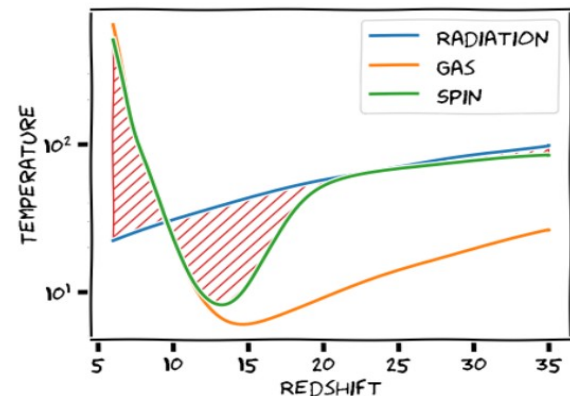
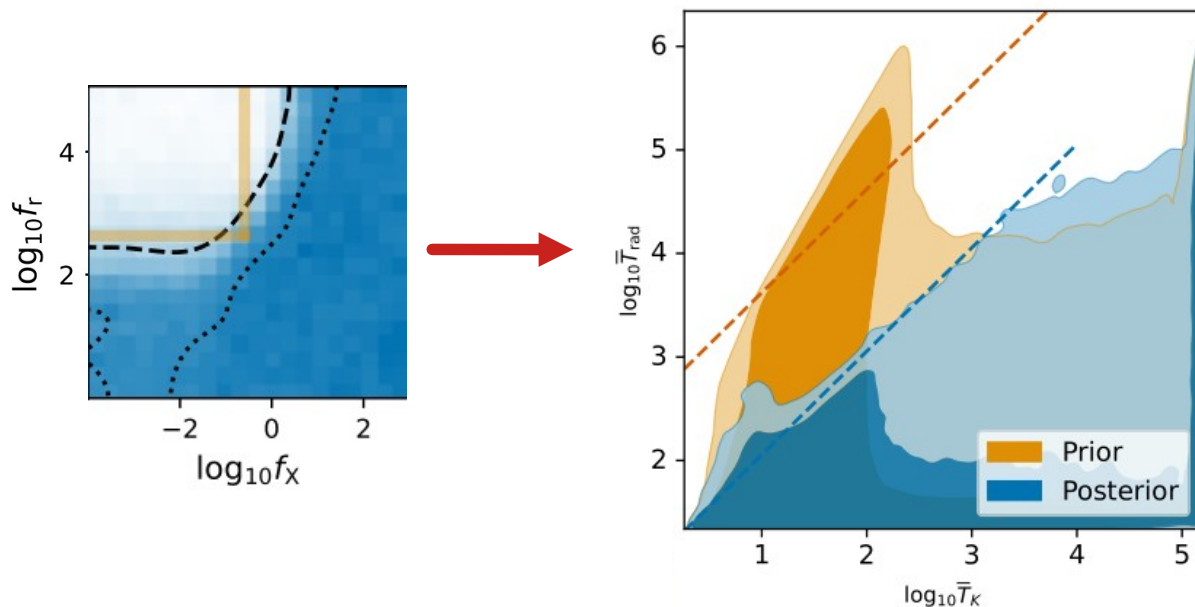
- **LWA:** Models with $f_r f_* > 10^3$ (approx) would produce too much radio background by $z=8$
- **Chandra:** Unresolved X-ray background allows for (approx) $f_x f_* < 1$

HERA clearly reduces the allowed parameter space!



More useful quantities: IGM temperatures

(lead by S.H., with Anastasia Fialkov)

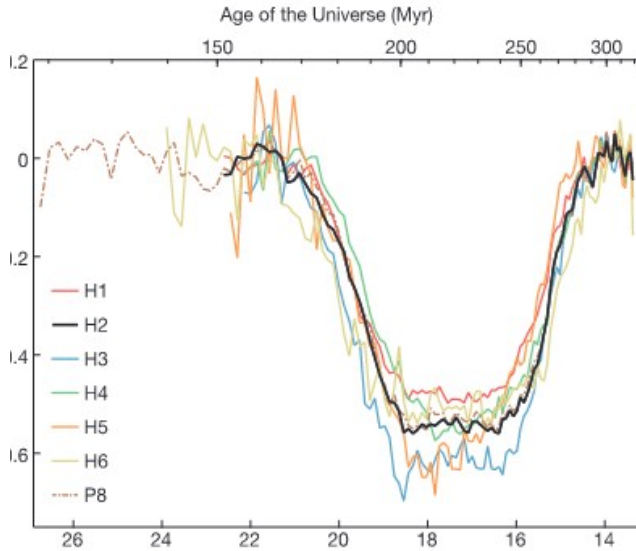


High contrast corresponds to large signal:

$$T_{21} \propto \left(1 - \frac{T_{\text{rad}}}{T_S} \right)$$

Excluded models correspond to those with **high radio** background and **relatively low gas temperature** ($T_{\text{rad}} / T_K > 10$ excluded)

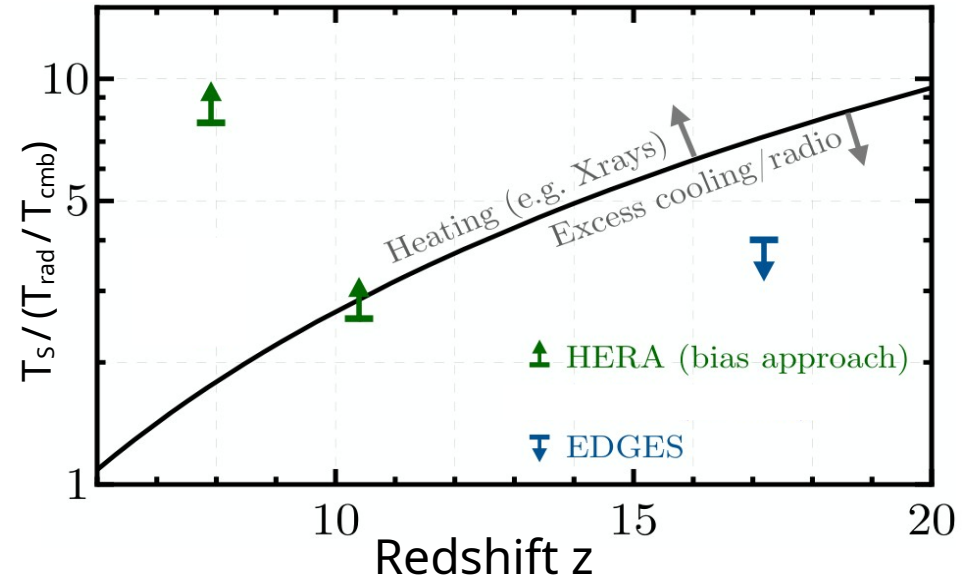
Comparison to EDGES claimed detection and models



Bowman et al. 2018

HERA → Lower limit on T_S/T_{rad}

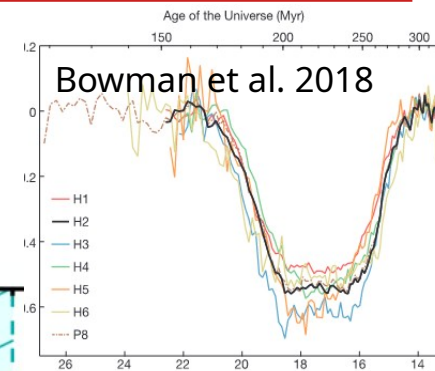
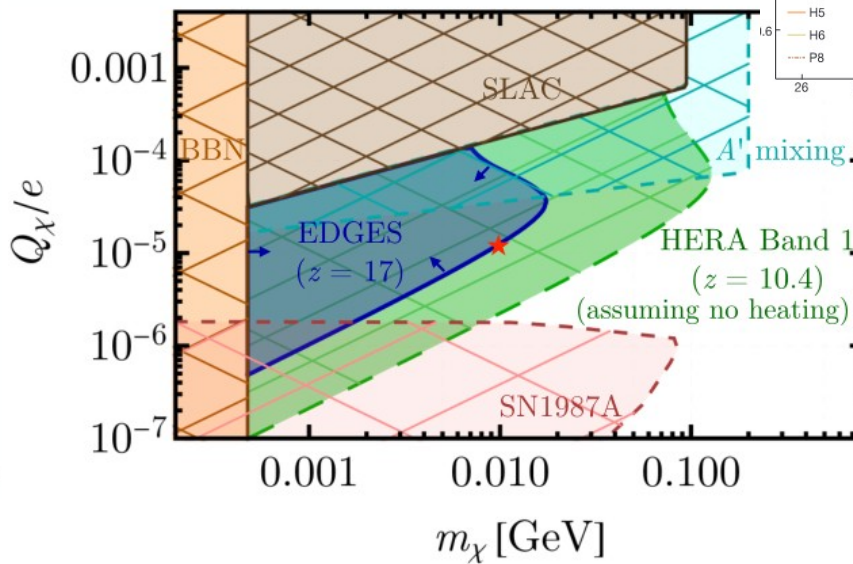
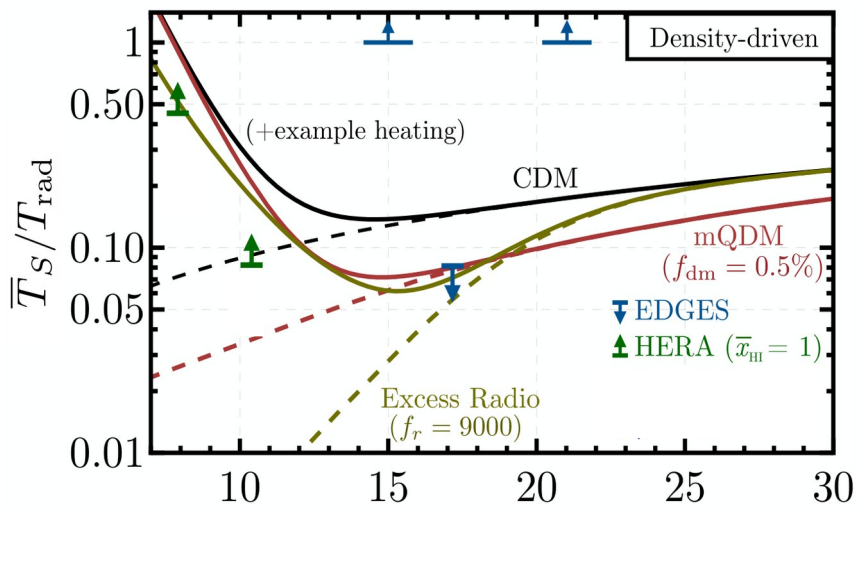
EDGES → Upper limit on T_S/T_{rad}



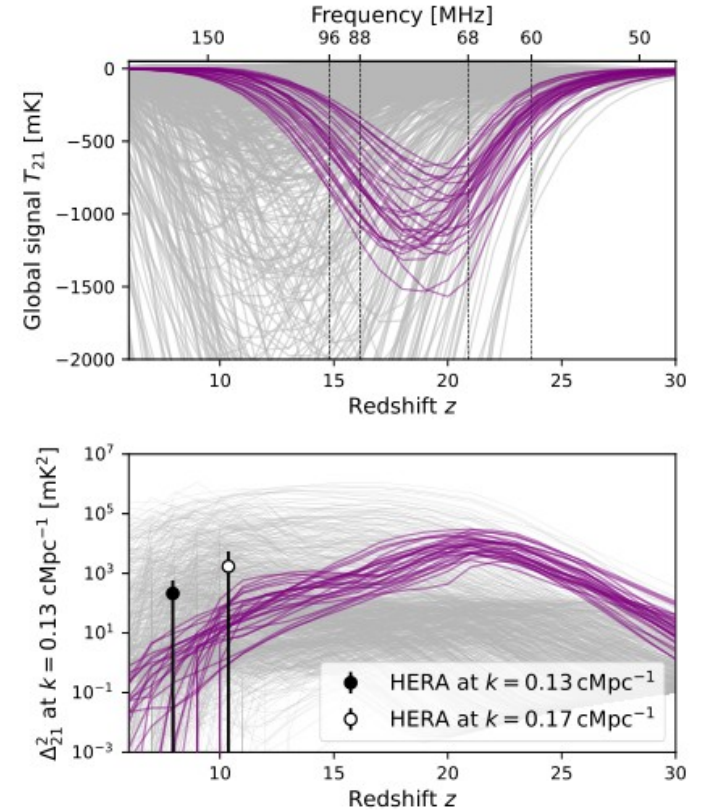
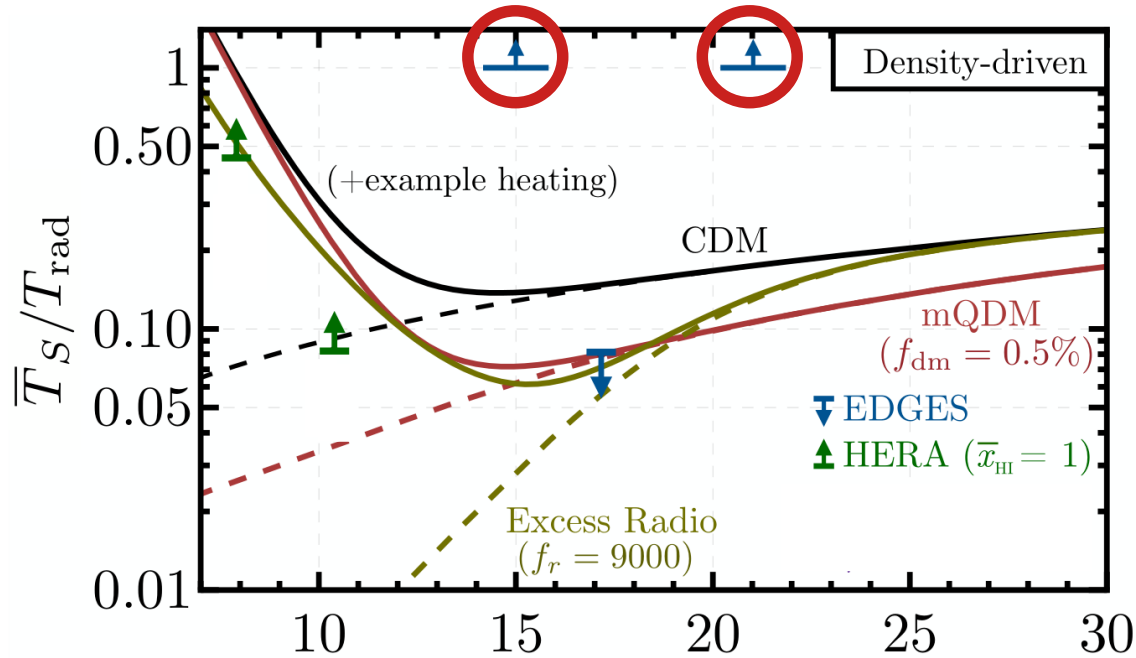
Millicharged Dark Matter constraints

(lead by Julian B. Muñoz)

DM interacting with baryons (e.g. millicharge) cools gas
→ Explains claimed EDGES detection → Ruled out by HERA (unless heated again)



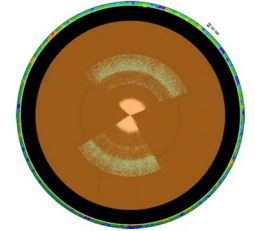
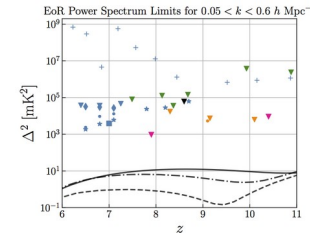
Comparison to full claimed EDGES trough



Intermediate summary – HERA 21cm constraints

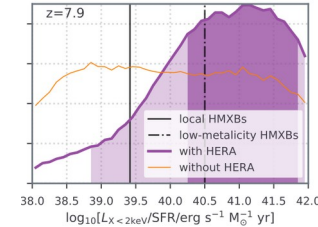
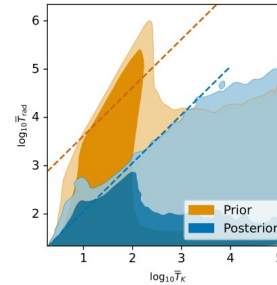
- **21cm cosmology will probe a large part of the observable Universe**

- Current most stringent power spectrum limits from HERA, $(14.55\text{mK})^2 \pm (19.17\text{mK})^2$ at $z=7.93$, $k=0.2 \text{ h/Mpc}$



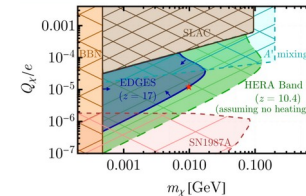
- **Constrain IGM & radiation temperature**

- Require heating of IGM by redshift 8
- Ratio $T_{\text{rad}}/T_{\text{gas}} < 10$



- **Constrain astrophysical models**

- Rule out some parts of astrophysical parameter space (those leading to high radio / less heating)



Fast Radio Bursts – the next probe of reionization!

- Short, bright, radio signals
- Extra-galactic (up to $z \sim 3$)

- Velocity frequency-dependent
→ Arrival times shifted $\propto 1/\nu^2$

$$DM = \int \frac{n_e}{1+z} dl$$

- Well known effect in pulsars:

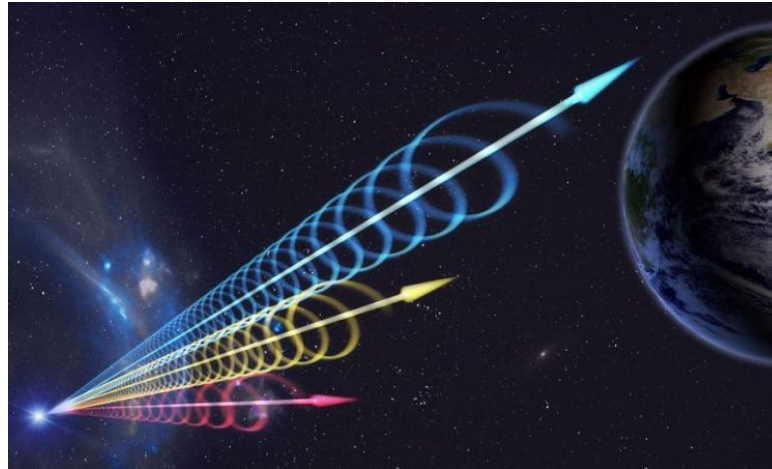
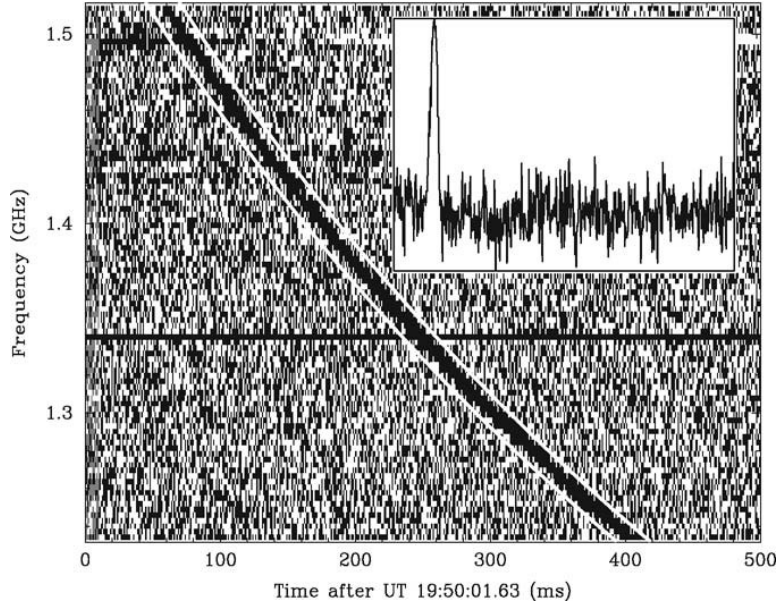
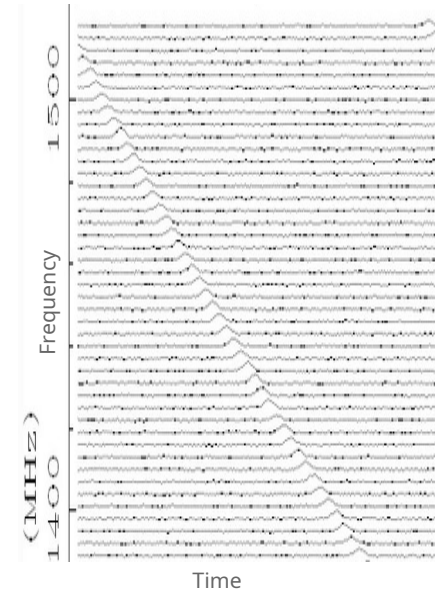


Image credit: Jingchuan Yu, Beijing Planetarium

Plot from Lorimer 2008



Fast Radio Bursts – the next great probe of reionization?

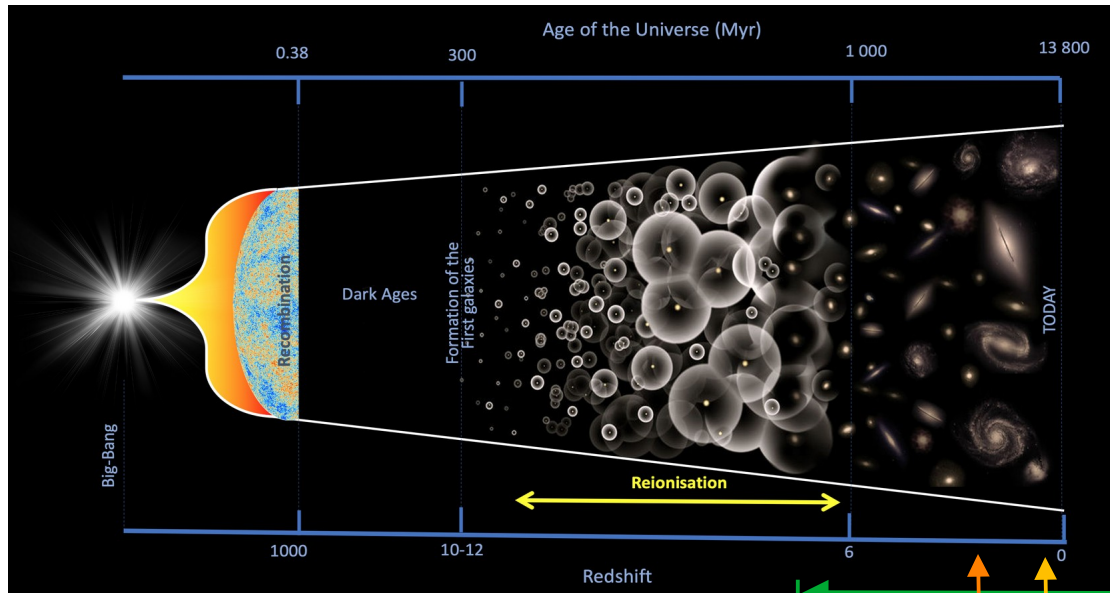
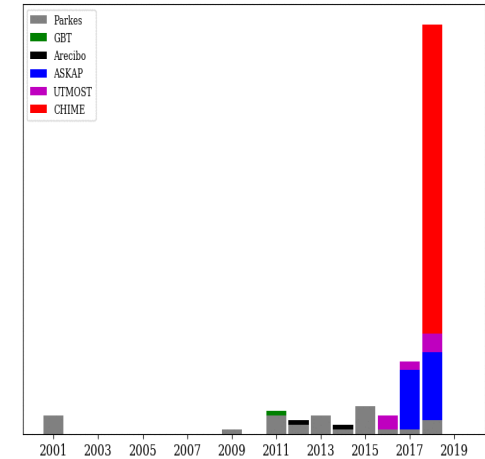


Image credit: Nicolas Laporte



Animation: Cherry Ng, (CHIME), Dunlap Institute
github.com/cherryng

Current constraints:

- Quasars $z < 7.7$
- Galaxies $z < 8$

Possible range of FRB sources

Localized FRBs

Farthest FRBs today

Where do FRBs come from

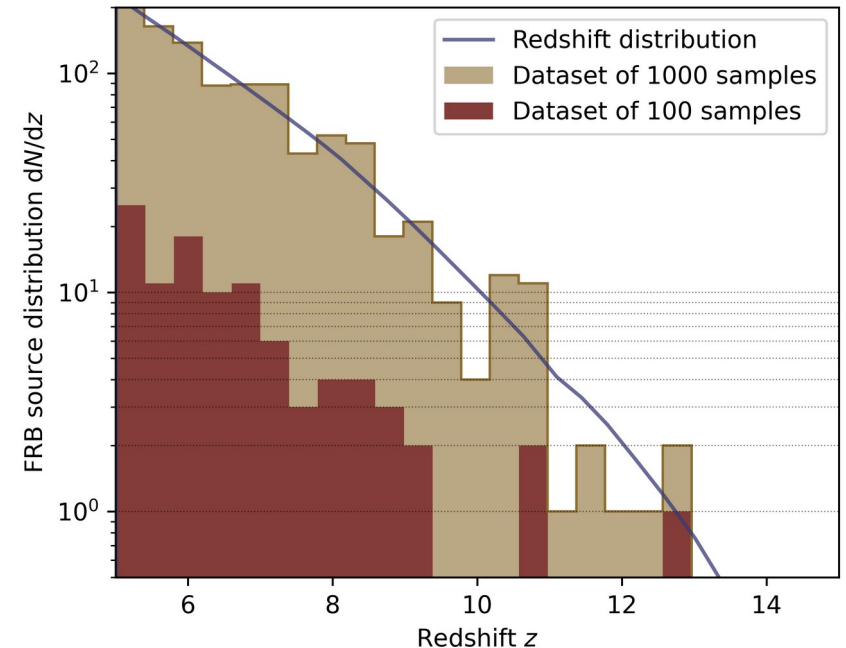
- **Origin of FRBs unknown – progenitor candidates:**

- Magnetars
 - FRB200428 was a magnetar but much weaker than extragalactic FRBs
- Mergers of compact objects
 - White dwarfs / neutron stars / black holes
- And about 50 further theories at frbtheorycat.org
 - From Alien light sails to Axion mini clusters

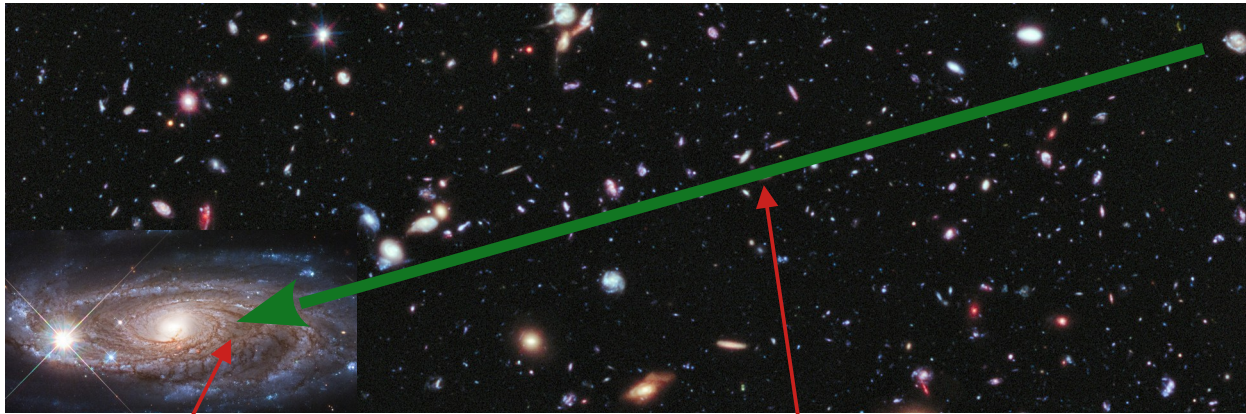
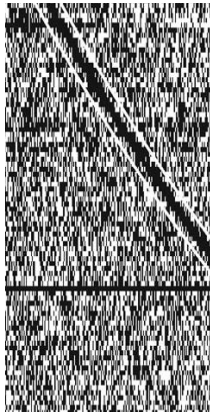


- **Many mechanisms approximately follow Star Formation Rate**

- Forecasts for SKA predict up to *100 FRBs/sky/day* at $z > 6$ (Hashimoto et al. 2020 [2008.00007])



Free electrons between Earth and the FRB source



Host galaxy – **unknown properties** $\sim 200 \pm 100$ pc/cm³

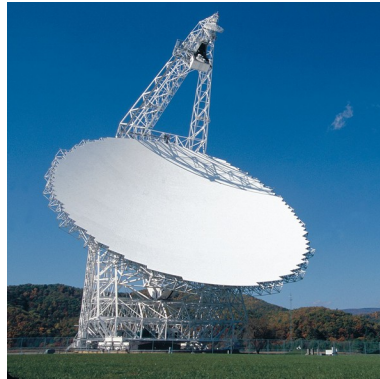
Milky Way – from 10 to 500 pc/cm³ but **known** from MW model

Intergalactic medium – depending on the **distance**, and **ionization** of the IGM along the line of sight

$$DM(z)^{\text{IGM}} = \int_{\text{earth}}^{\text{source}} \frac{n_e^{\text{IGM}}(z)}{(1+z)} dl \sim 4000 - 6000 \text{ pc/cm}^3 \pm 5-9\% \text{ (for } z=5 \text{ to } 15)$$

Image credits: NASA; ESA; B. Holwerda; Illingworth, Oesch, Bouwens and the HUDF09 Team

Observational prospects



CHIME: Thousands of low- z FRBs

GBT: Search for high- z high-DM FRBs



FAST: Forecast FRBs up to $z=10$

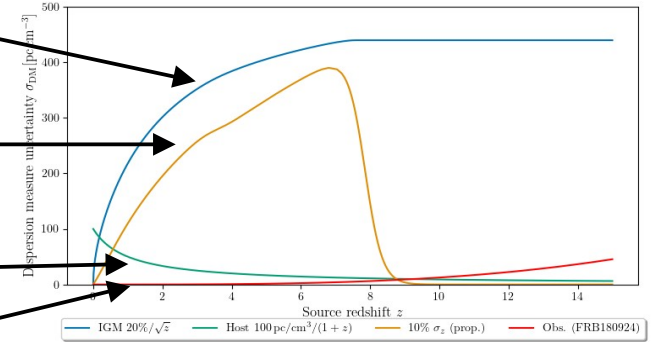
Image credits: CHIME; Absolute Cosmos; NRAO/AUI/NSF

Main uncertainty: IGM inhomogeneity

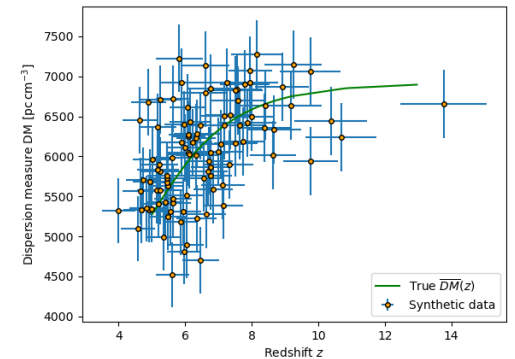
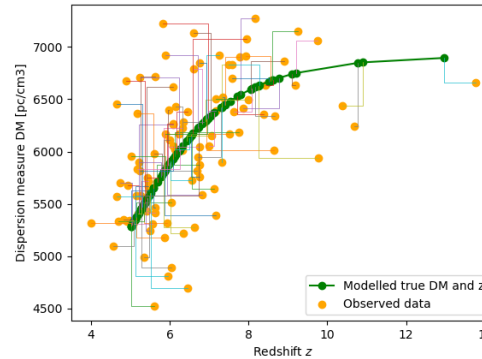
Redshift error (DM-equivalent)

Unknown host contribution

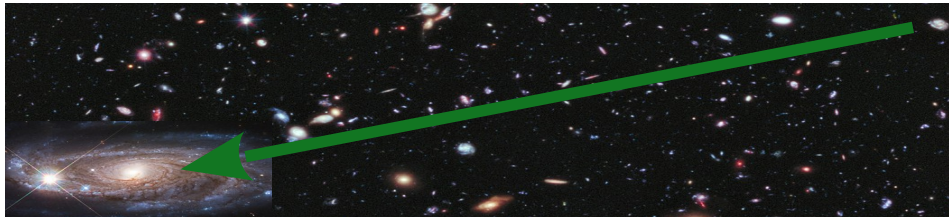
Observational error



Simulated synthetic observations:

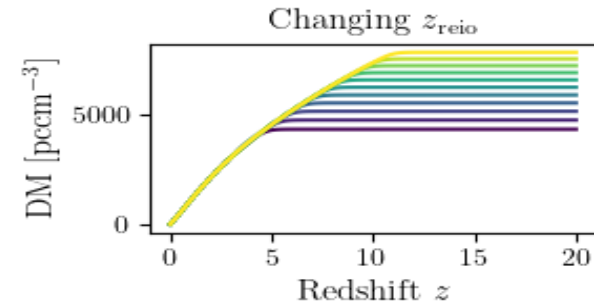
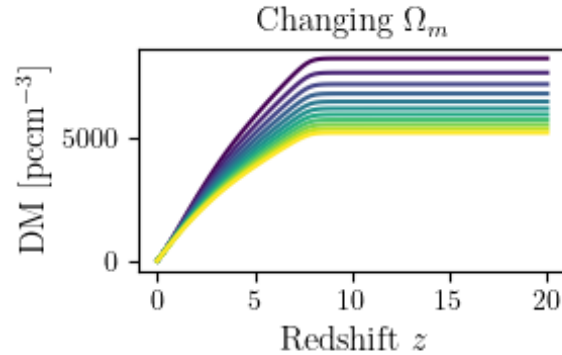
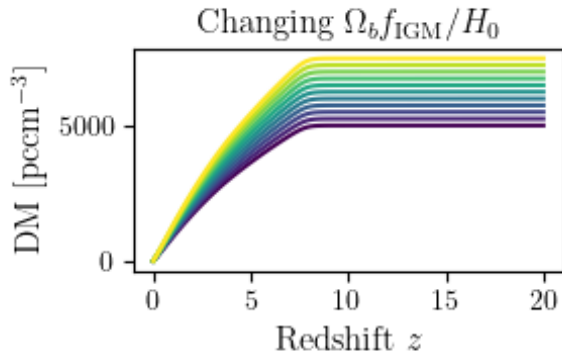
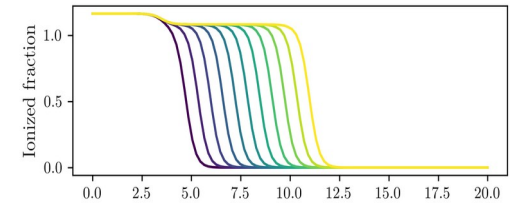


How Reio affects FRBs



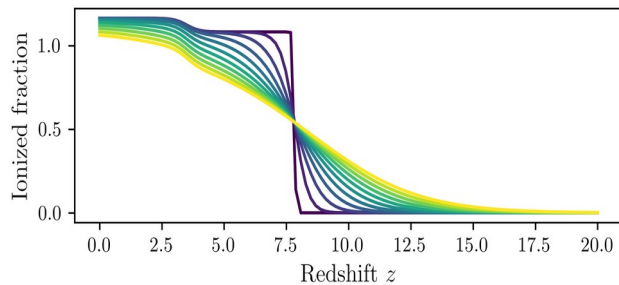
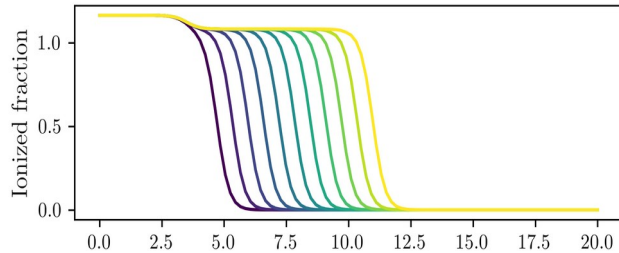
$$\overline{\text{DM}}^{\text{IGM}}(z) = \int_0^z c \underbrace{\frac{\Omega_b}{H(z)}}_{\text{Cosmology}} \underbrace{\frac{\bar{n}_e(z')/\Omega_b}{(1+z')^2}}_{\text{Ionization}} dz'$$

$H_0, \Omega_b, \Omega_m, w(z)$
 Hagstotz et al. 2021, Qiu et al. 2021
 Macquart et al. 2020
 E.g. Zhou et al. 2014 (forecast)



Parameterizing reionization history function

Common *tanh* parameterization:



Planck 2018 results

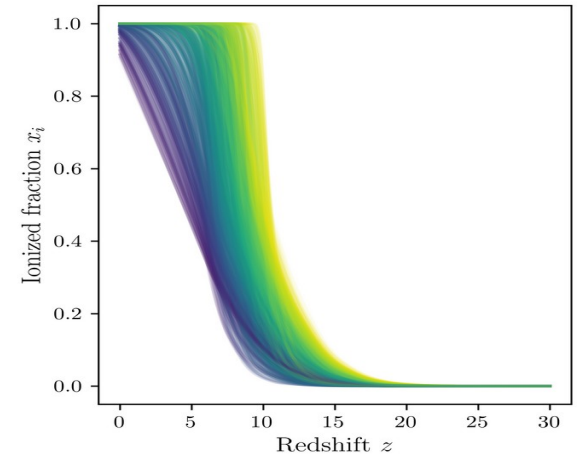
VI. Cosmological parameters

SEVEN-YEAR WILKINSON MICROWAVE ANISOTROPY PROBE (WMAP^{*}) OBSERVATIONS: COSMOLOGICAL INTERPRETATION

Results from EDGES High-band. I. Constraints on Phenomenological Models for the Global 21 cm Signal

Reconstruction of Reionization History through Dispersion Measure of Fast Radio Bursts

Reionization simulations (Fialkov et al.):



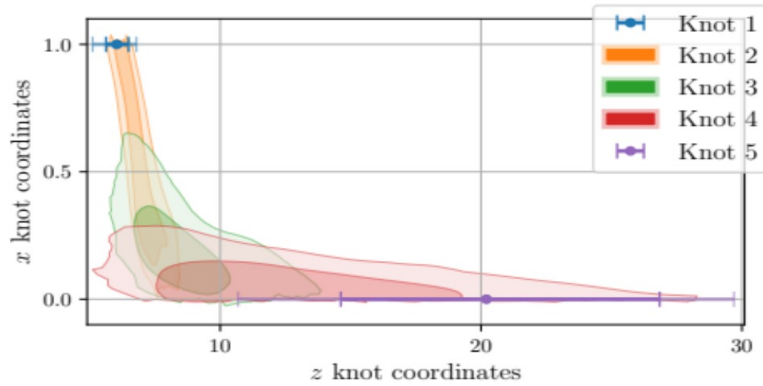
Problem: Assuming a model \rightarrow Wrong result if model \neq reality

E.g. the standard *tanh* step function reionization underestimates τ by 10%

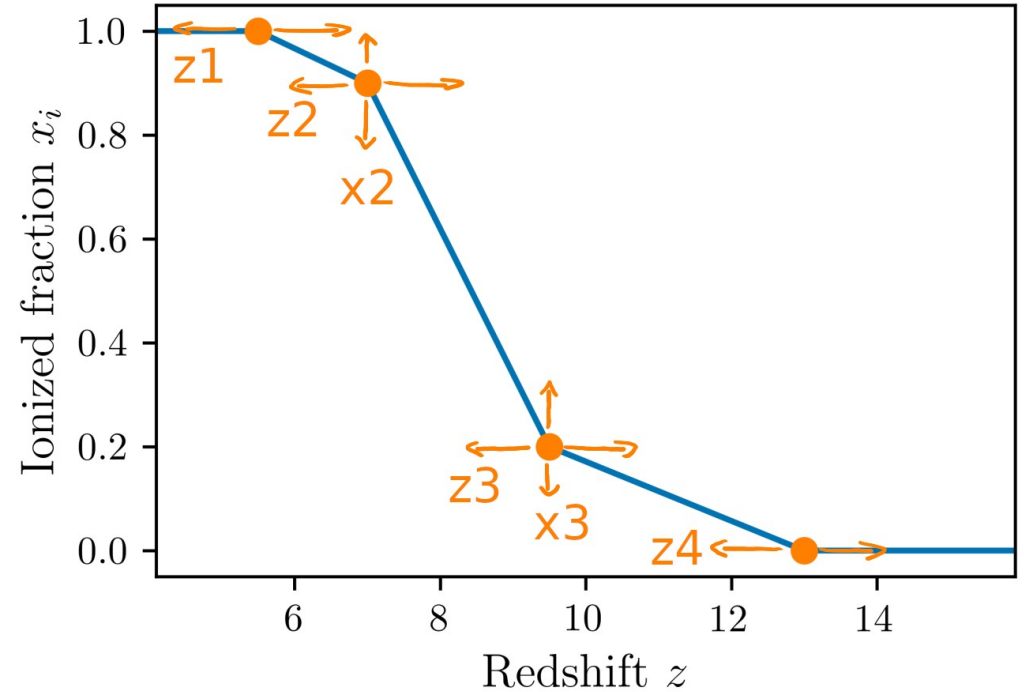
$$\tau_{\text{tanh}} = 0.052 \pm 0.002 \text{ for } \tau_{\text{true}} = 0.057 \text{ (1,000 FRBs)}$$

Model-independent parameterization FlexKnot

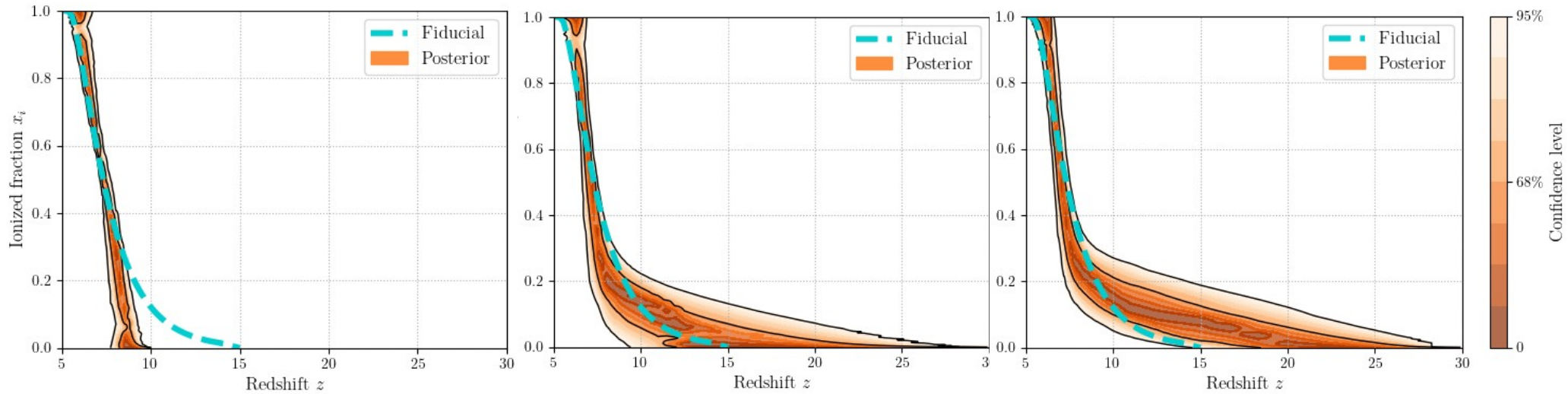
- “Free-form” parameterization, interpolate between “knots”
 - Use coordinates of knots as parameters
 - Interpolate function between knots
 - Obtain constraints on parameters



FlexKnot method CMB: Millea & Bouchet 2018, arXiv 1804.08476



FlexKnot: How many knots?



Only start + end knot:

too simple?

Add +2 more knots:

fits well?

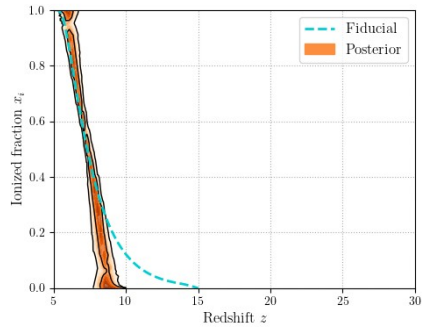
Add +9 additional knots:

too many params?

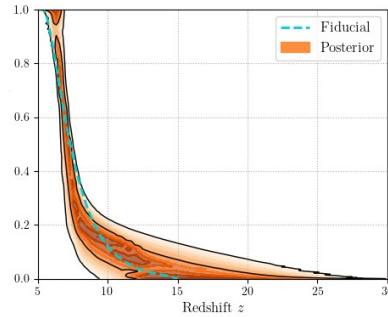
FlexKnot: How many knots?



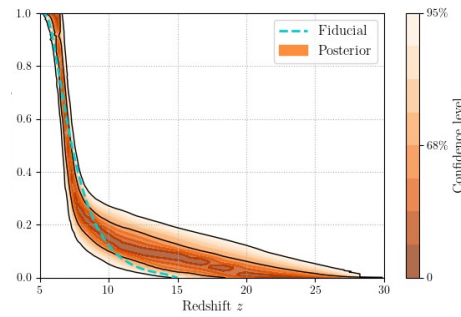
Marginalize over number of knots (\rightarrow Evidence)



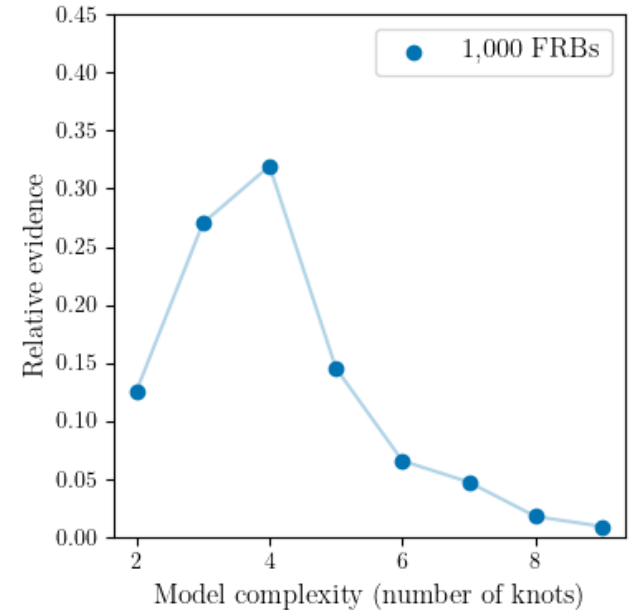
Only start + end knot:
too simple
Evidence $Z = 0.4$



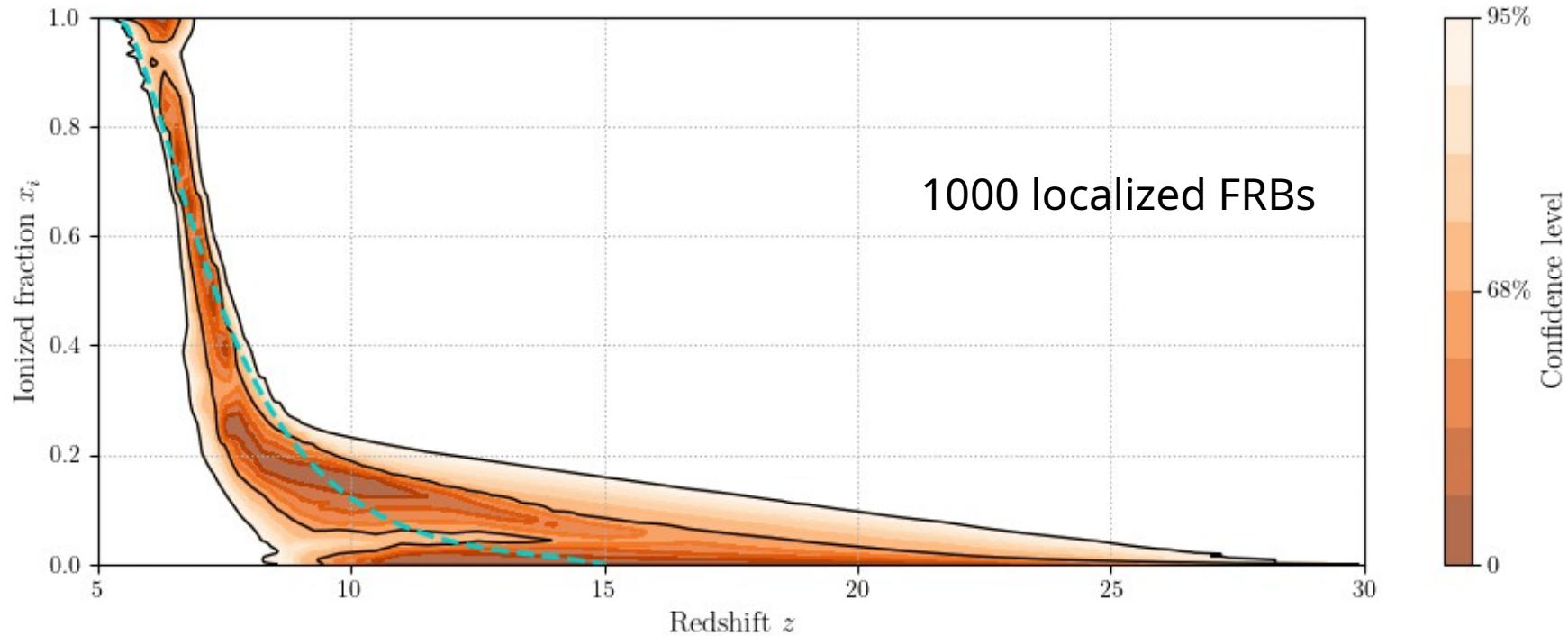
Add +2 more knots:
fits well
Evidence $Z = 1$



Add +9 additional knots:
too many params
Evidence $Z = 0.01$

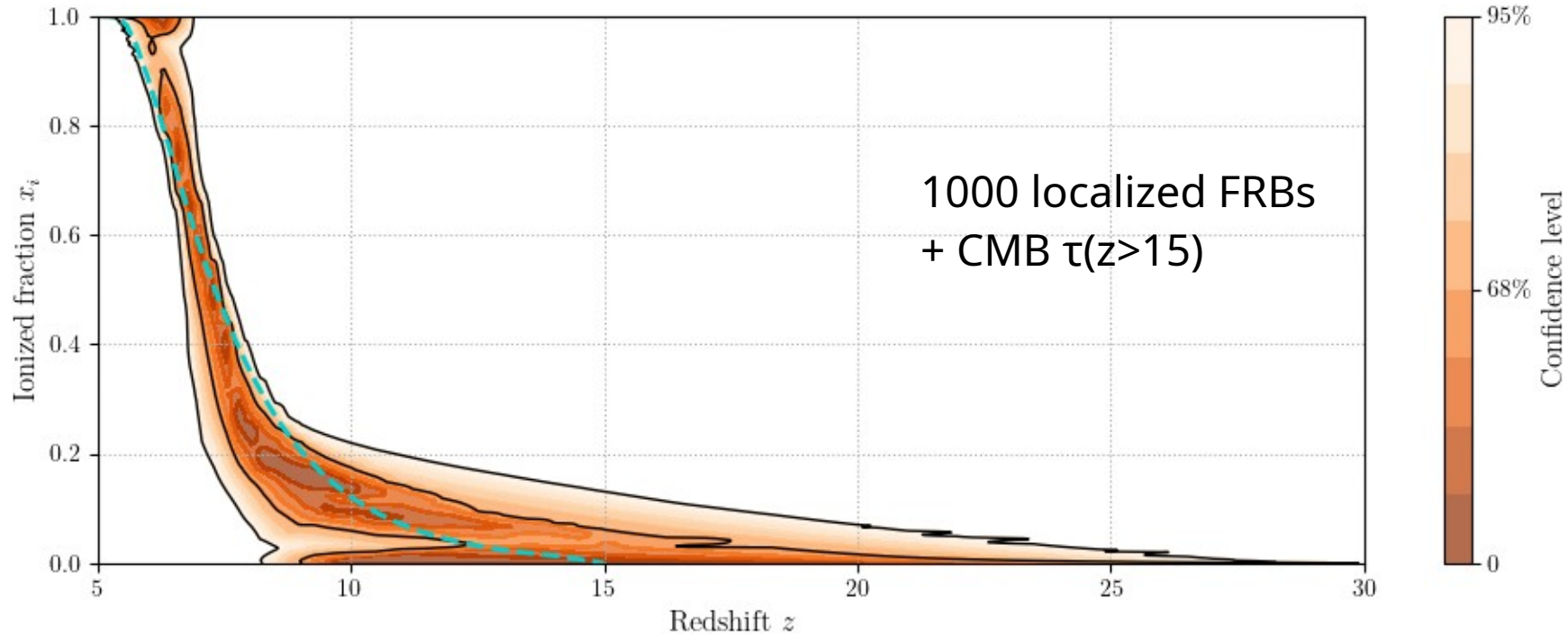


Reionization history constraints: FRBs only



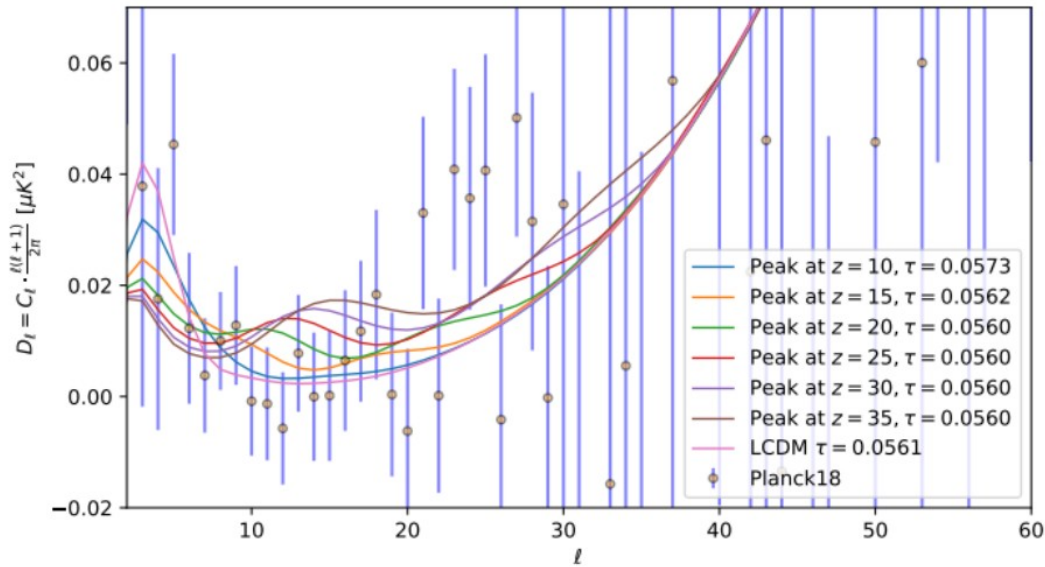
Reionization history constraints: Add $\tau(15,30)$

Advantages of having *function* $x_i(z)$: 1) Combine with integral constraint $\tau(15,30)$

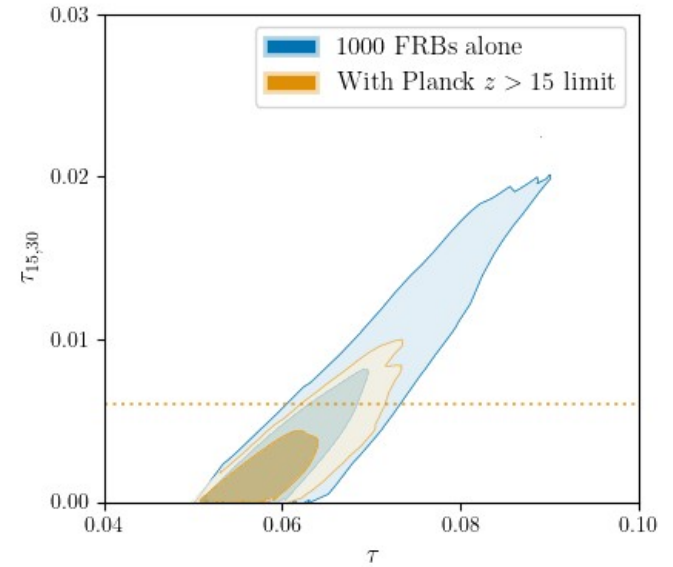


Synergy with Cosmic Microwave Background

CMB polarization power spectra observations limit early reionization, *Planck FlexKnot*: $\tau(15,30) < 0.006$

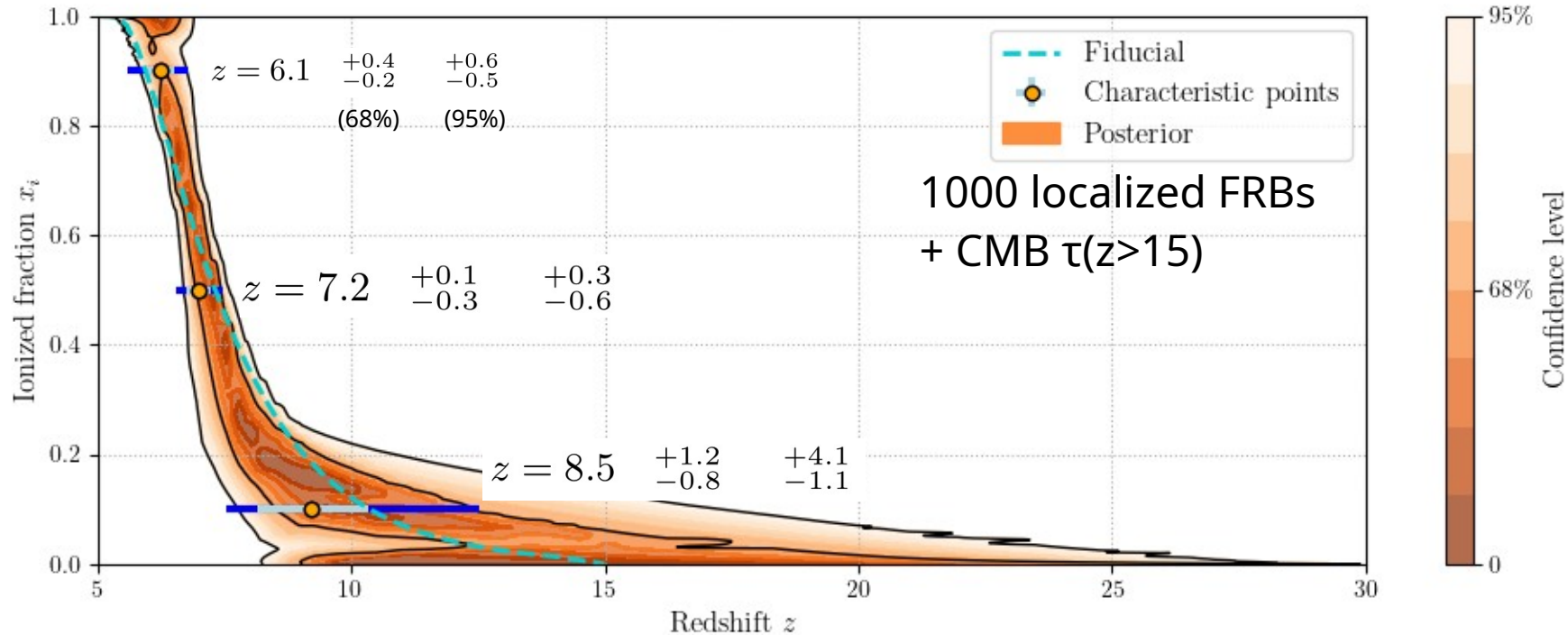


FRBs provide weak constraints for $z > 15$



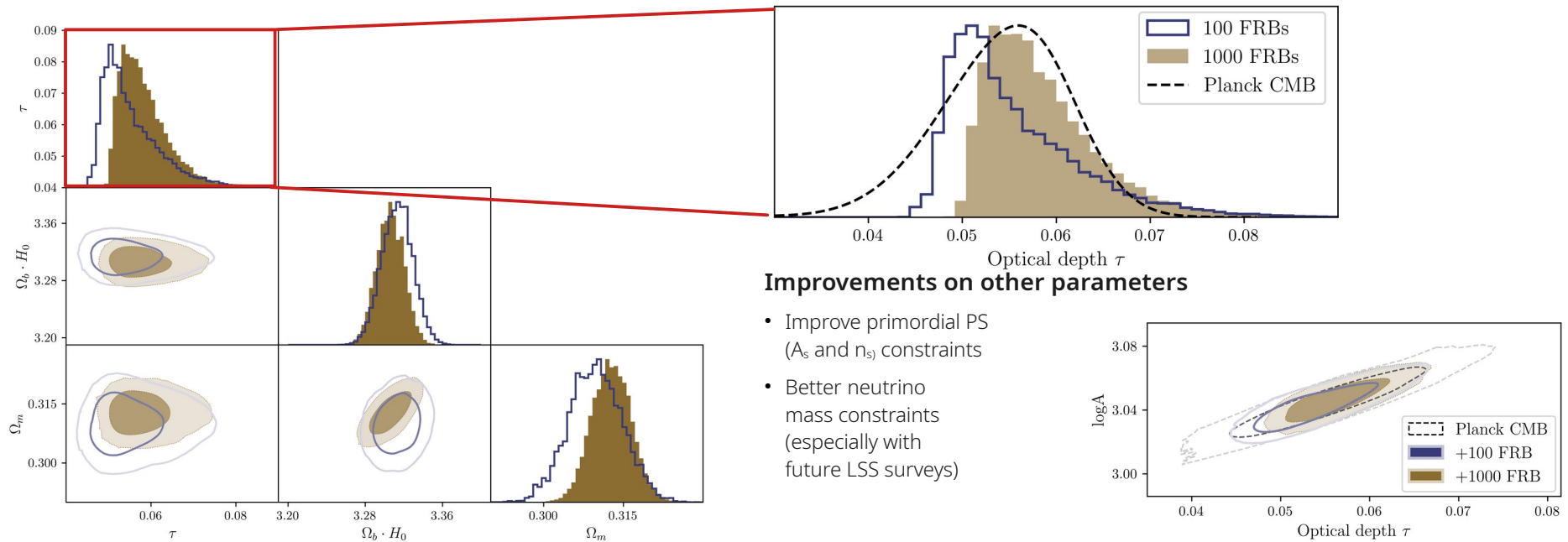
Reionization history constraints: Redshifts

Advantages of having *function* $x_i(z)$: 2) Derive additional constraints (e.g. midpoint)



Cosmology constraints

Key point: Reionization model-*marginalized* (“independent”), i.e. averaged over all reionization models.



Summary

- FRBs can probe Era of Reionization
 - Competitive constraints with 100 FRBs @ $z>5$
- Need to avoid biases in our methods
 - Model-independent reionization parameterization
 - Applicable to all kinds of function constraints

arXiv: [2107.14242](https://arxiv.org/abs/2107.14242)

Source code: github.com/Stefan-Heimersheim/FlexKnotFRB

- HERA 21cm power spectrum rules out first astrophysical models

→ Constrain X-ray heating & radio background / temperatures

arXiv: [2108.07282](https://arxiv.org/abs/2108.07282)

