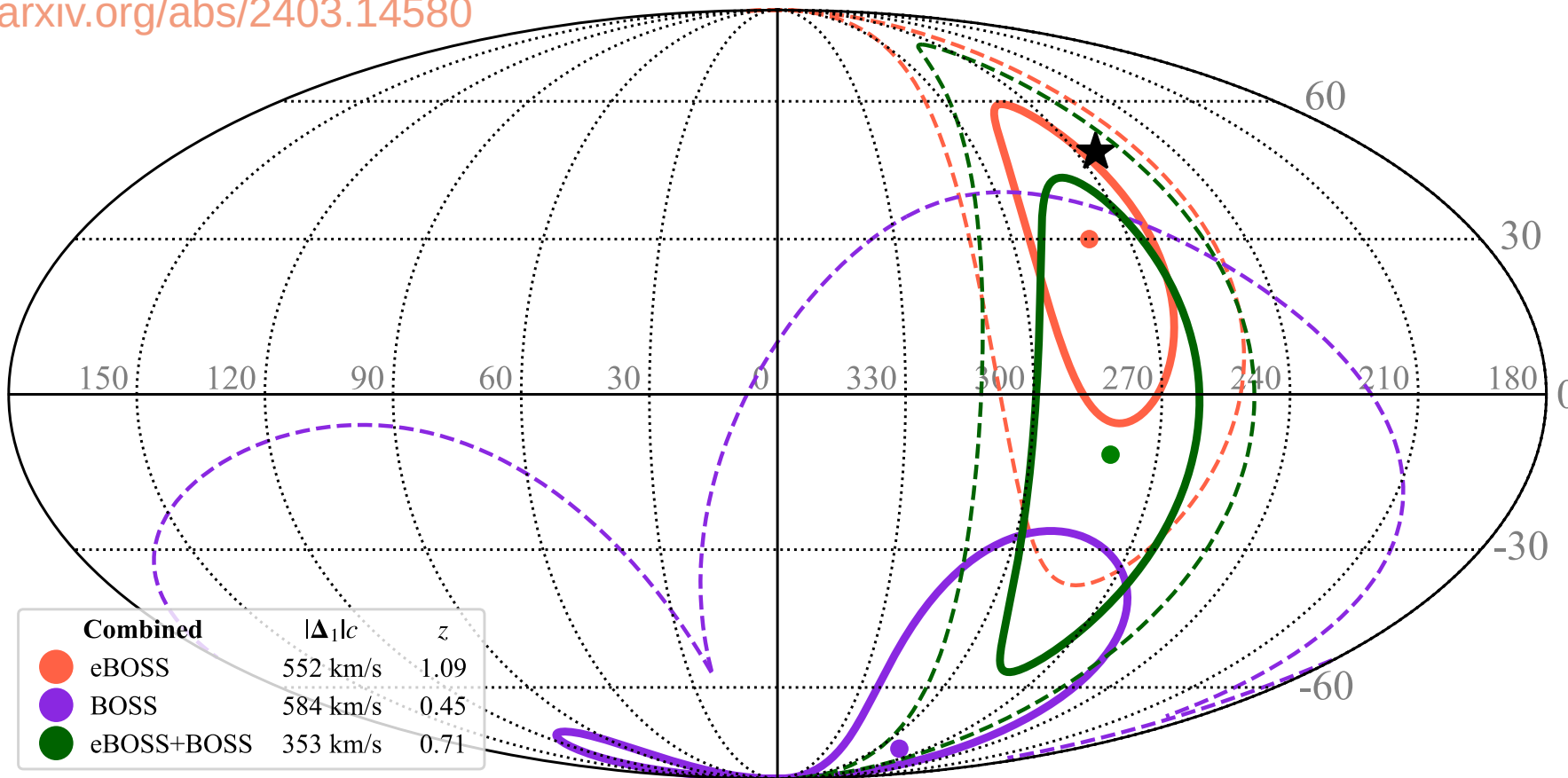


Tomographic redshift dipole: Testing the cosmological principle

Pedro da Silveira Ferreira and Valerio Marra

<https://arxiv.org/abs/2403.14580>



A challenge to the cosmological principle

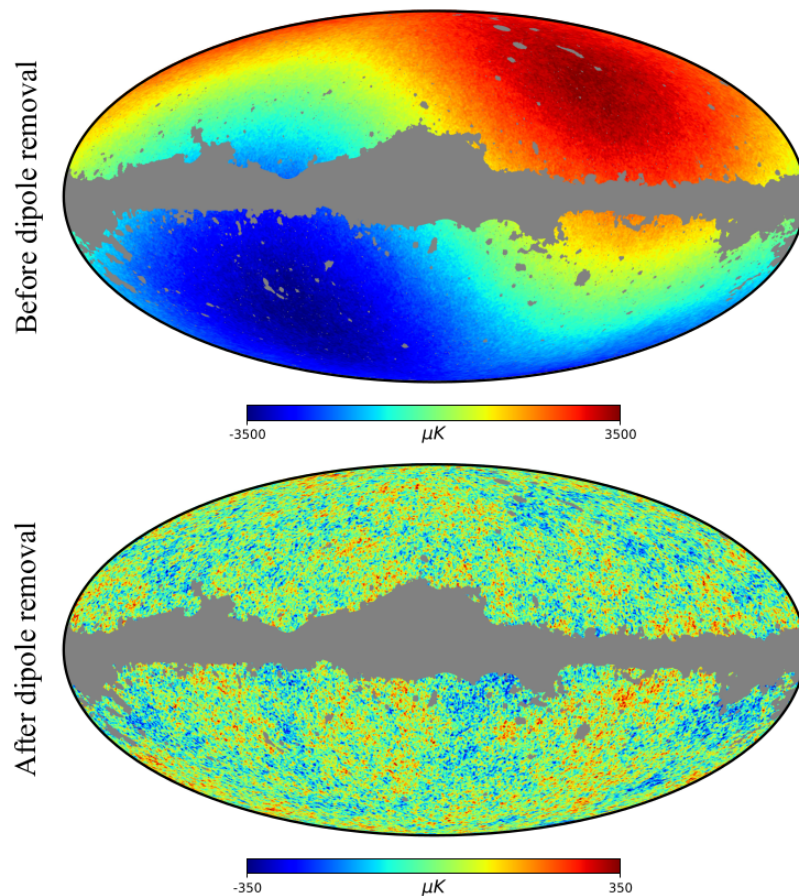
Cosmology's standard model (Λ CDM), is founded on the cosmological principle, which asserts that **the universe is statistically homogeneous and isotropic on scales larger than approximately 100 Mpc.**

Consequently, the primary source of the dipole observed in distant objects should be attributed to our peculiar velocity.

This implies that velocity estimates derived from different sources, such as x-ray, radio galaxies (**RG**), quasars (**QSO**), supernovae Ia (**SNe**), and even gravitational waves, should agree.

However, over the past 25 years, several studies utilizing different RG and QSO catalogs have consistently found that, though the peculiar velocity is generally consistent in direction with the CMB dipole, its amplitude is in tension. This quarter-century-long puzzle poses a significant challenge to the standard model, with **the tension regarding the CMB dipole now reaching a 5σ level.**

Planck 2018 (SMICA Temperature map)



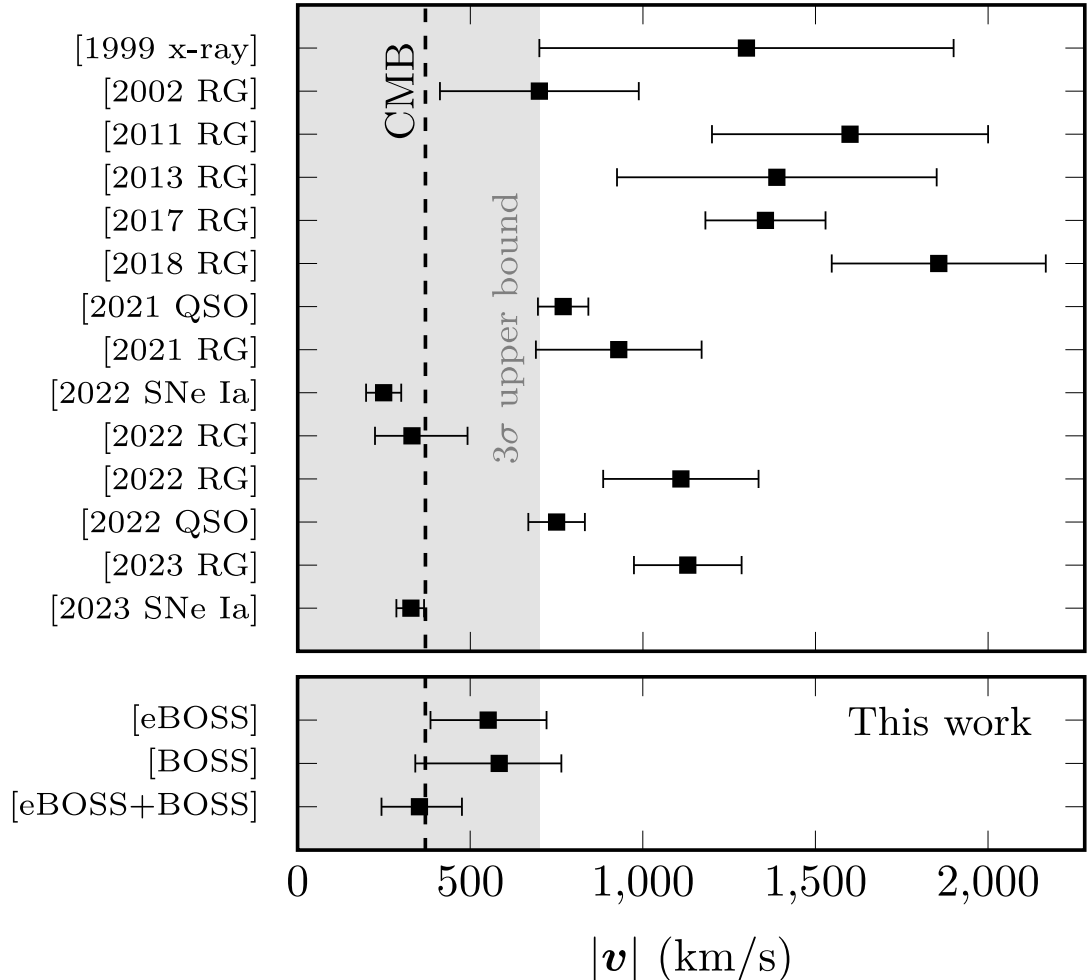
A challenge to the cosmological principle

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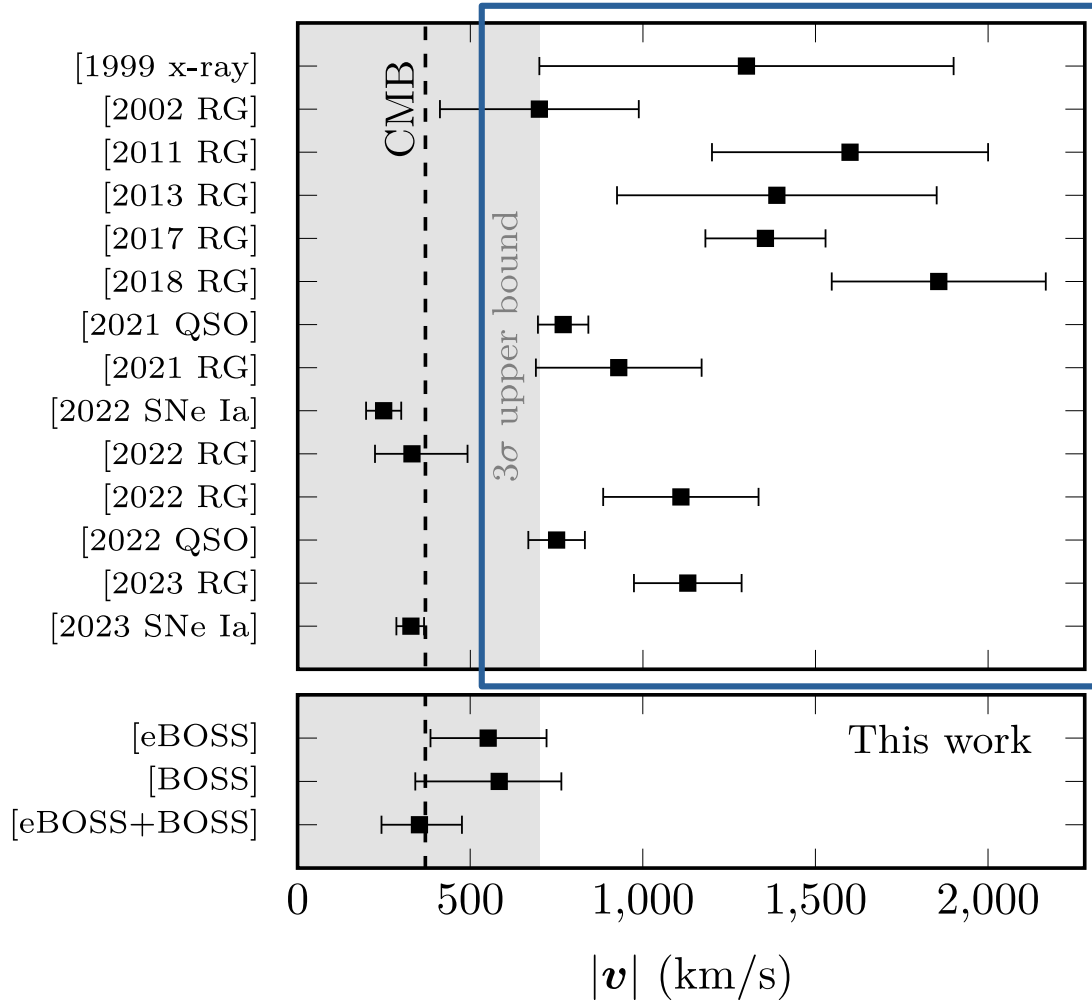
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A challenge to the cosmological principle



A challenge to the cosmological principle

PHYSICAL REVIEW LETTERS

Accepted Paper

First constraints on the intrinsic CMB dipole and our velocity with Doppler and aberration

Phys. Rev. Lett.

Pedro da Silveira Ferreira and Miguel Quartin

Accepted 21 July 2021

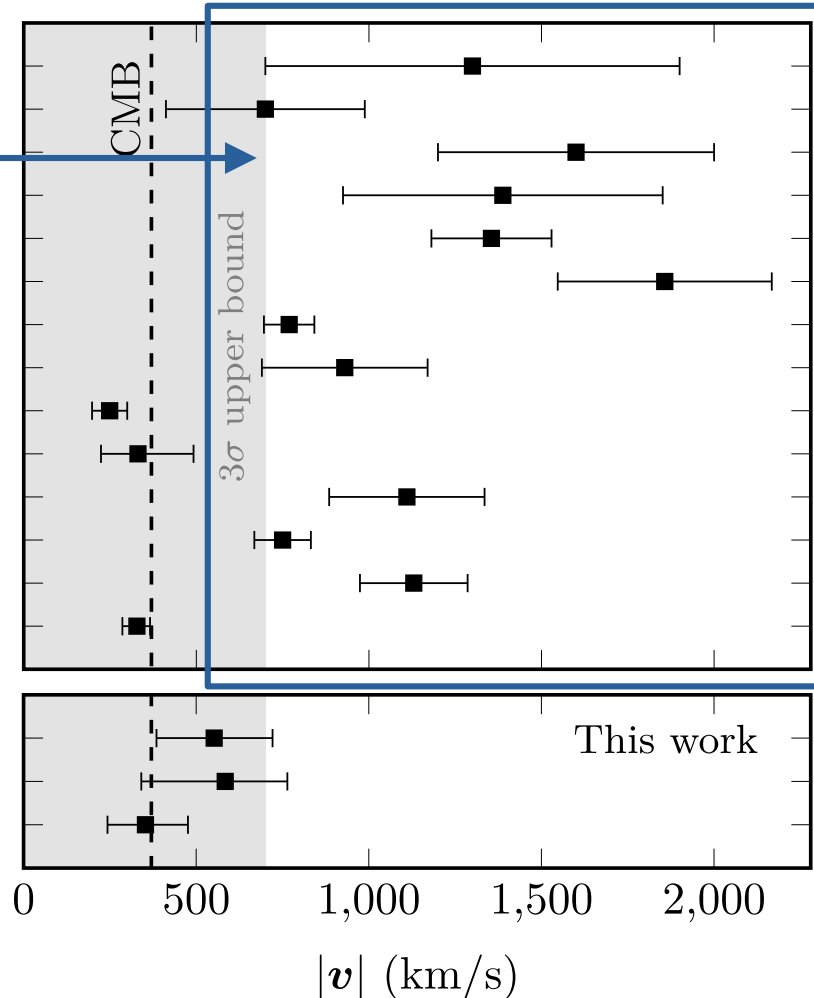
<https://arxiv.org/abs/2011.08385v2>

Nevertheless there exists the possibility that part of the dipolar effect could be due to primordial fluctuations in the surface of last-scattering (SLS). Concrete alternatives to the kinematic scenario were discussed as far back as 30 years ago by [2], which showed that a large local void could also explain the dipole. This particular scenario was further investigated by e.g. [3] and [4]. A “tilted universe scenario” composed of a superhorizon isocurvature perturbation was proposed in [5]. An inflationary model which produces similar results was proposed by [6]. This scenario can be tested as it leads to

$$\Delta_{1,int} \quad \leftarrow \quad \underbrace{\quad \rightarrow}_{\Delta_1} \quad \beta$$

- [1999 x-ray]
- [2002 RG]
- [2011 RG]
- [2013 RG]
- [2017 RG]
- [2018 RG]
- [2021 QSO]
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- [2022 RG]
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- [eBOSS]
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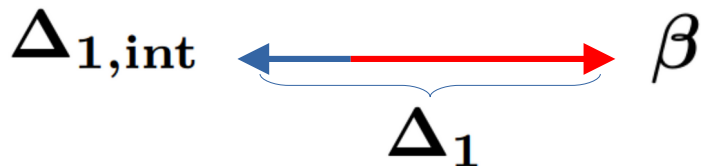
Pedro da Silveira Ferreira and Miguel Quartin

Accepted 21 July 2021

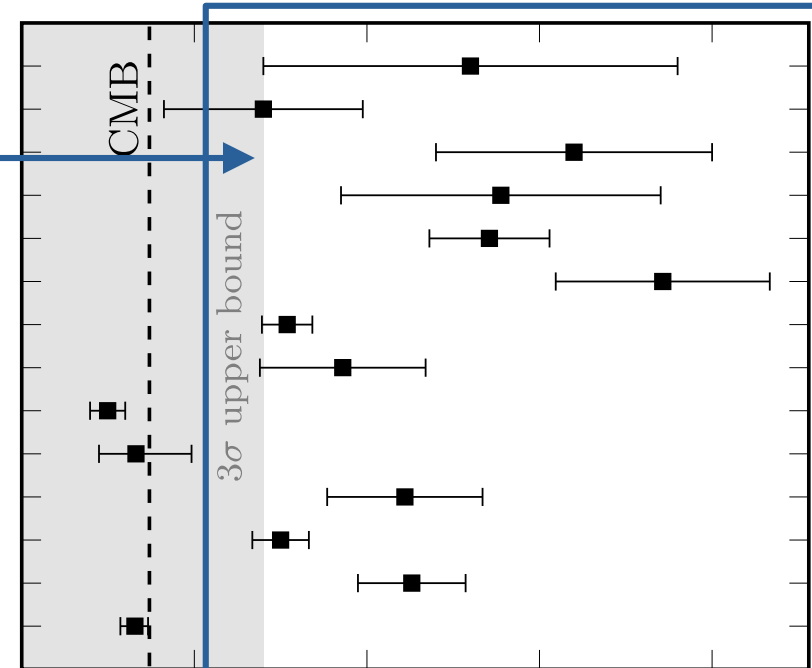
<https://arxiv.org/abs/2011.08385v2>

Interpreting the CMB aberration and Doppler measurements: boost or intrinsic dipole?

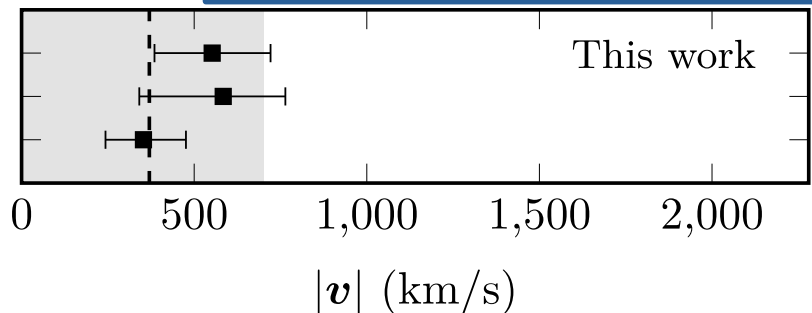
Omar Roldan,^a Alessio Notari^b and Miguel Quartin^a



- [1999 x-ray]
- [2002 RG]
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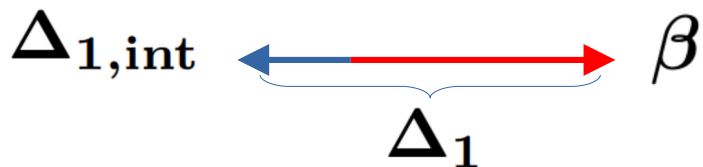
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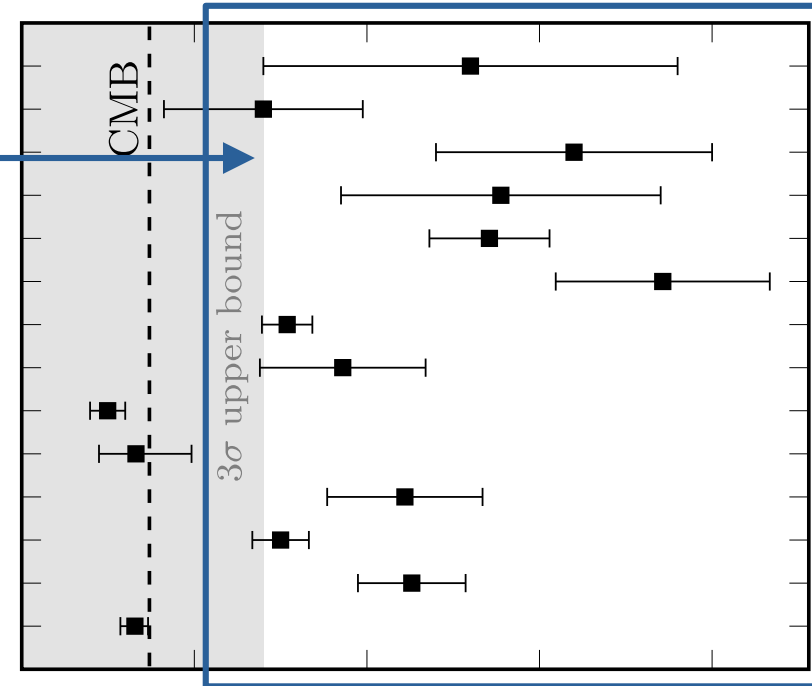
$$\Delta_1 = \beta + \Delta_{1,\text{int}},$$

$$\beta^{\text{D}} = \beta + (1 + \alpha^{\text{NG}}) \Delta_{1,\text{int}},$$

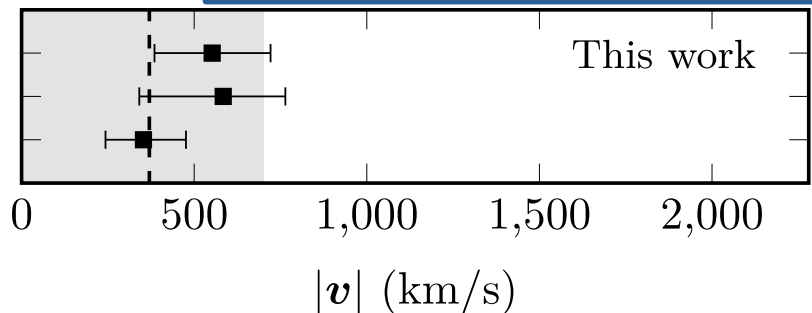
$$\beta^{\text{A}} = \beta + \mathbf{L}_d,$$



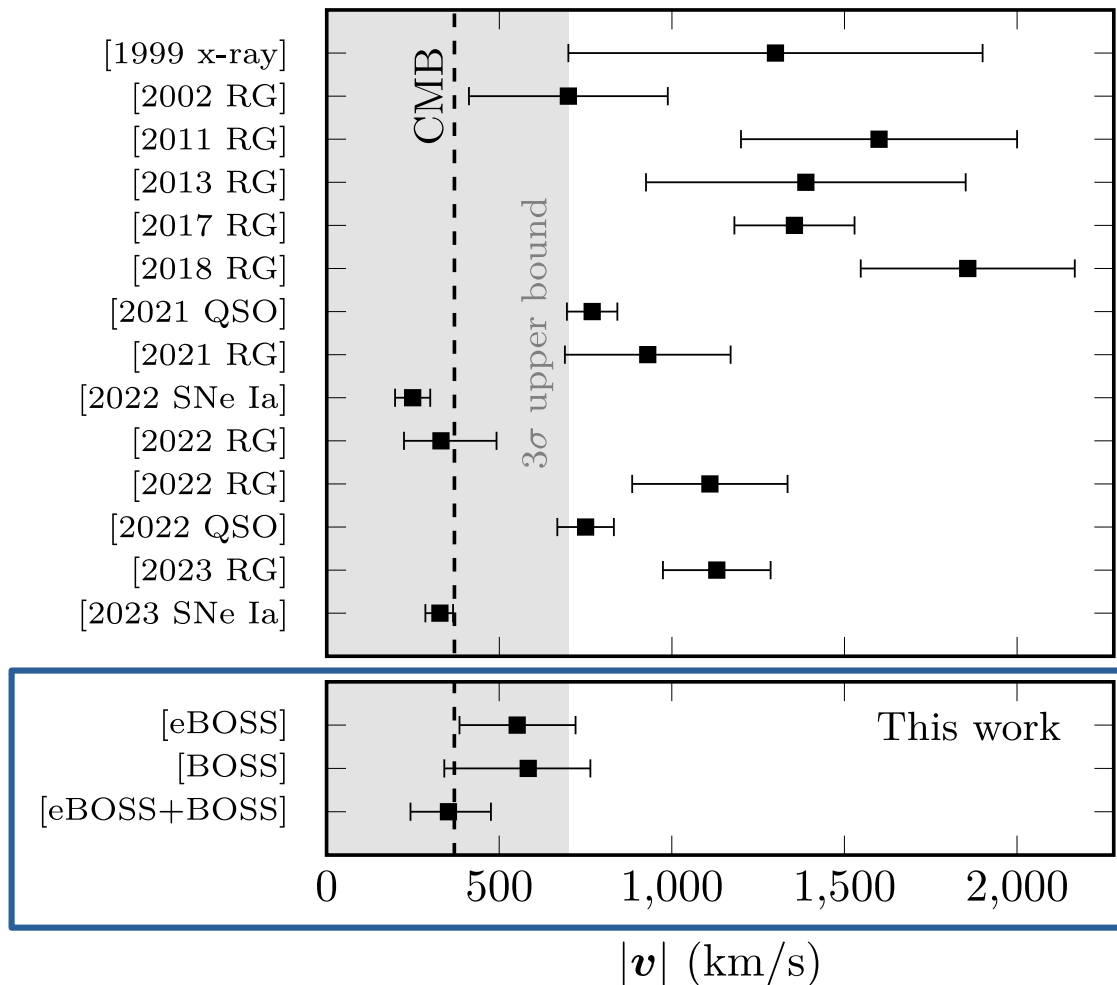
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- [2022 RG]
- [2022 RG]
- [2022 QSO]
- [2023 RG]
- [2023 SNe Ia]



- [eBOSS]
- [BOSS]
- [eBOSS+BOSS]



A challenge to the cosmological principle



The redshift dipole

Doppler modulation

$$1 + z'(\hat{n}') = (1 + z(\hat{n}))\delta(\beta, \hat{n}')$$

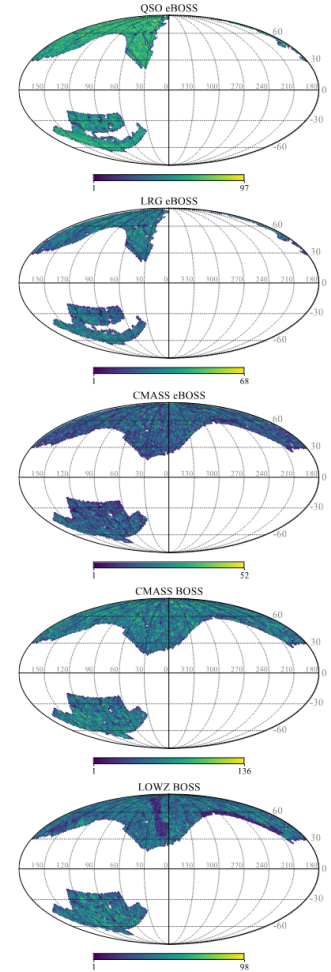
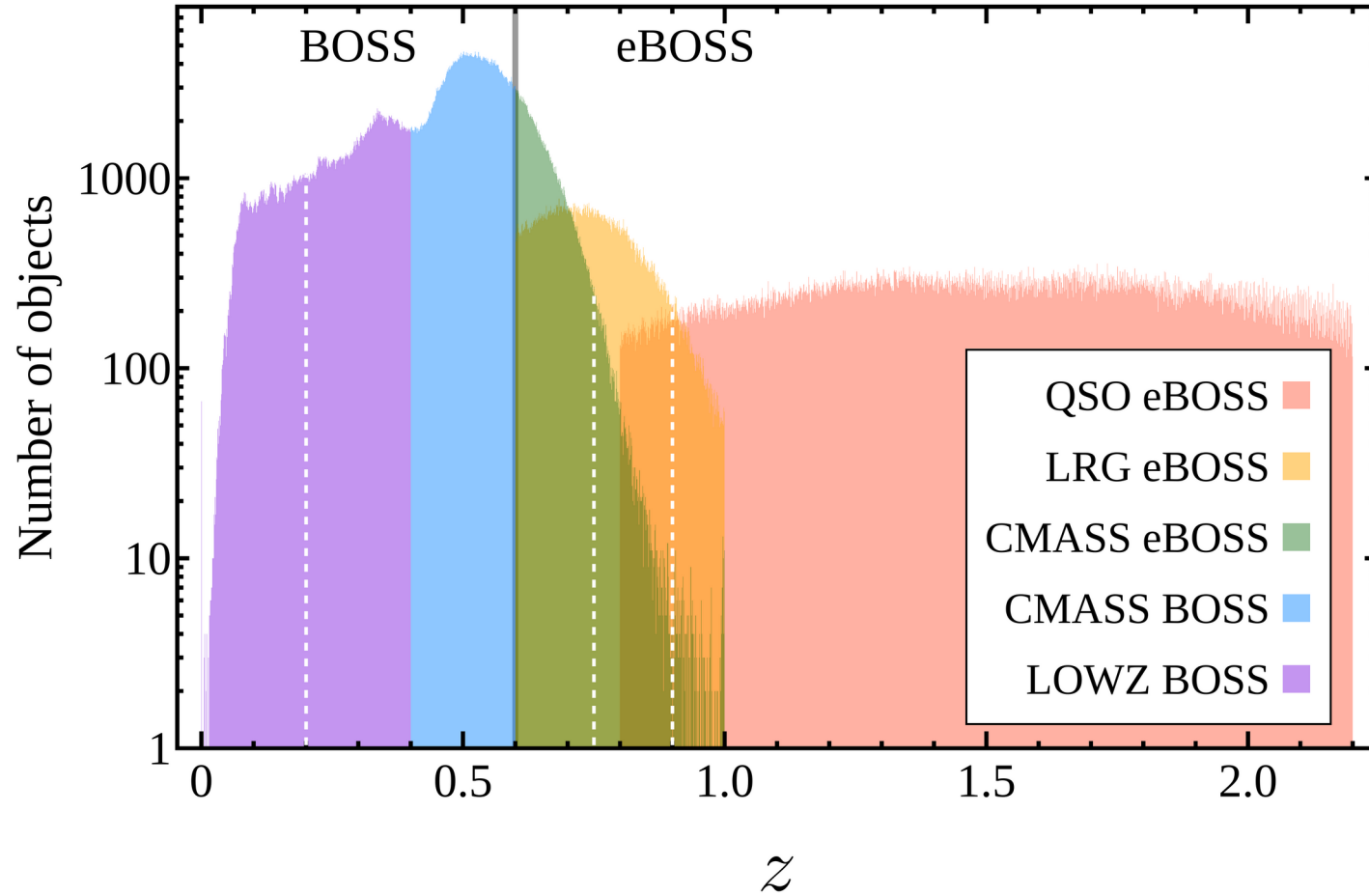
$$\delta(\beta, \hat{n}') = \frac{\sqrt{1 - \beta^2}}{(1 + \beta \cdot \hat{n}')}$$

Relation between the dipole and the velocity

$$\Delta_1 = -\beta + \Delta_{1,\text{int}} + \mathcal{O}(\beta^2) \quad \left. \vphantom{\Delta_1} \right\} \Delta_1 = -\beta$$

↑
<2% (0.2 < z < 2.2)

Data



Measuring the dipolar modulation

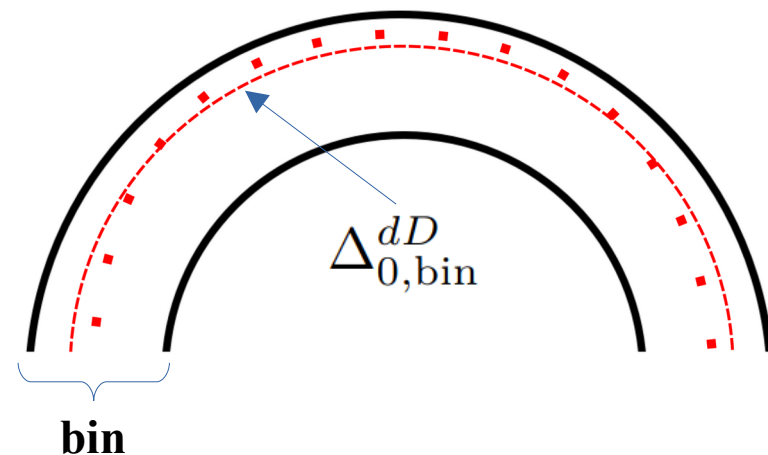
$$\chi_{\text{bin}}^2(\Delta_1) = \frac{\sum_i^N w_i^2 [1 + z_i - \Delta_{0,\text{bin}}^{dD} \delta(-\Delta_1, \hat{\mathbf{n}}'_i)]^2}{\sum_i^N w_i^2}$$

$$w_{i,\text{eBOSS}} = w_{i,\text{sys}} \cdot w_{i,\text{noz}} \cdot w_{i,\text{fc}},$$

$$w_{i,\text{BOSS}} = w_{i,\text{sys}} \cdot (w_{i,\text{noz}} + w_{i,\text{fc}} - 1)$$

$$\Delta_{0,\text{bin}}^{dD} = \frac{\sum_i^N w_i (1 + z_i) \delta(-\Delta_1, \hat{\mathbf{n}}'_i)^{-1}}{\sum_i^N w_i}$$

$$\chi^2(\Delta_1) = \sum_{\text{bin}} \chi_{\text{bin,NGC}}^2(\Delta_1) + \sum_{\text{bin}} \chi_{\text{bin,SGC}}^2(\Delta_1)$$



Measuring the dipolar modulation

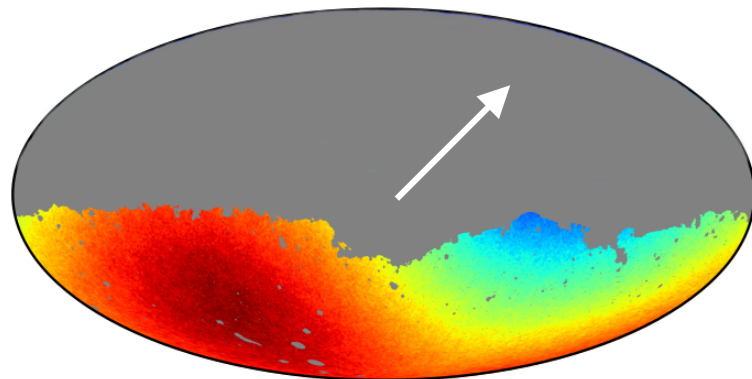
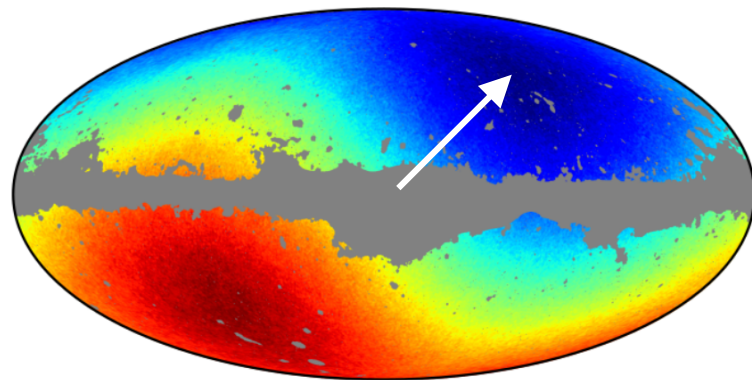
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Measuring the dipolar modulation

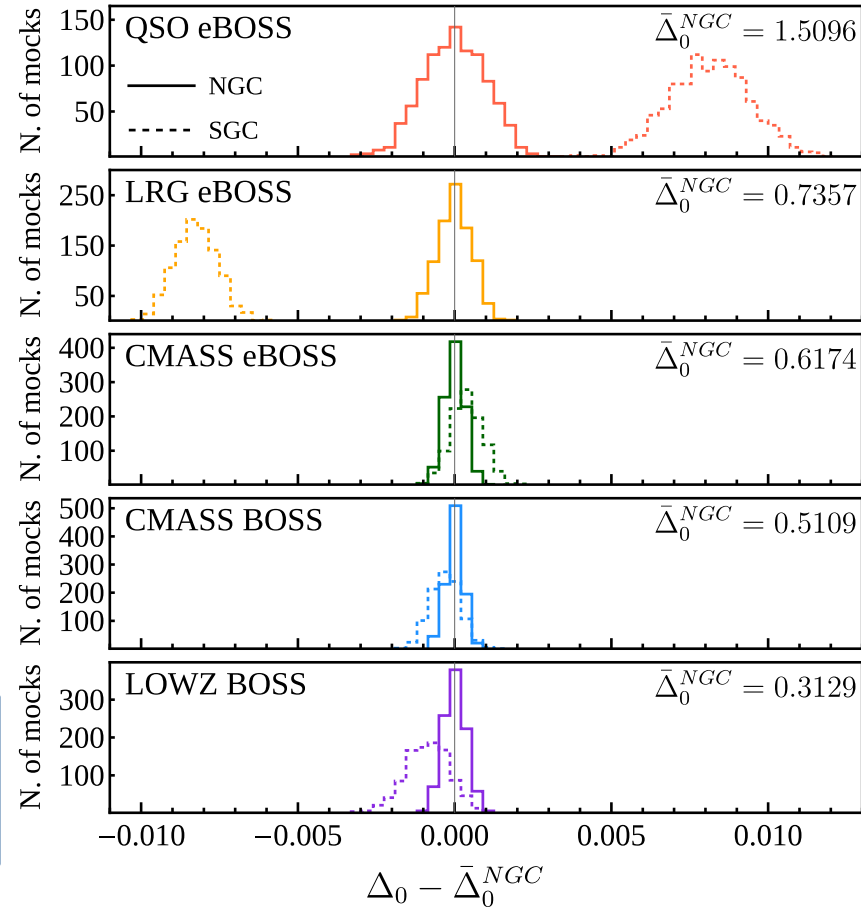
$$\chi_{\text{bin}}^2(\Delta_1) = \frac{\sum_i^N w_i^2 [1 + z_i - \Delta_{0,\text{bin}}^{dD} \delta(-\Delta_1, \hat{\mathbf{n}}'_i)]^2}{\sum_i^N w_i^2}$$

$$w_{i,\text{eBOSS}} = w_{i,\text{sys}} \cdot w_{i,\text{noz}} \cdot w_{i,\text{fc}},$$

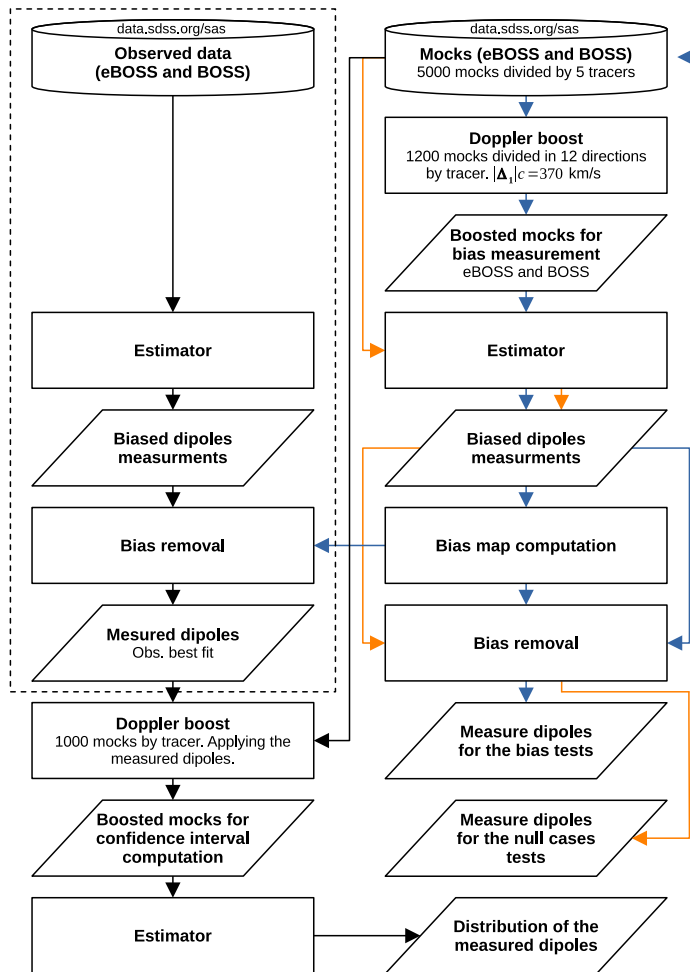
$$w_{i,\text{BOSS}} = w_{i,\text{sys}} \cdot (w_{i,\text{noz}} + w_{i,\text{fc}} - 1)$$

$$\Delta_{0,\text{bin}}^{dD} = \frac{\sum_i^N w_i (1 + z_i) \delta(-\Delta_1, \hat{\mathbf{n}}'_i)^{-1}}{\sum_i^N w_i}$$

$$\chi^2(\Delta_1) = \sum_{\text{bin}} \chi_{\text{bin,NGC}}^2(\Delta_1) + \sum_{\text{bin}} \chi_{\text{bin,SGC}}^2(\Delta_1)$$



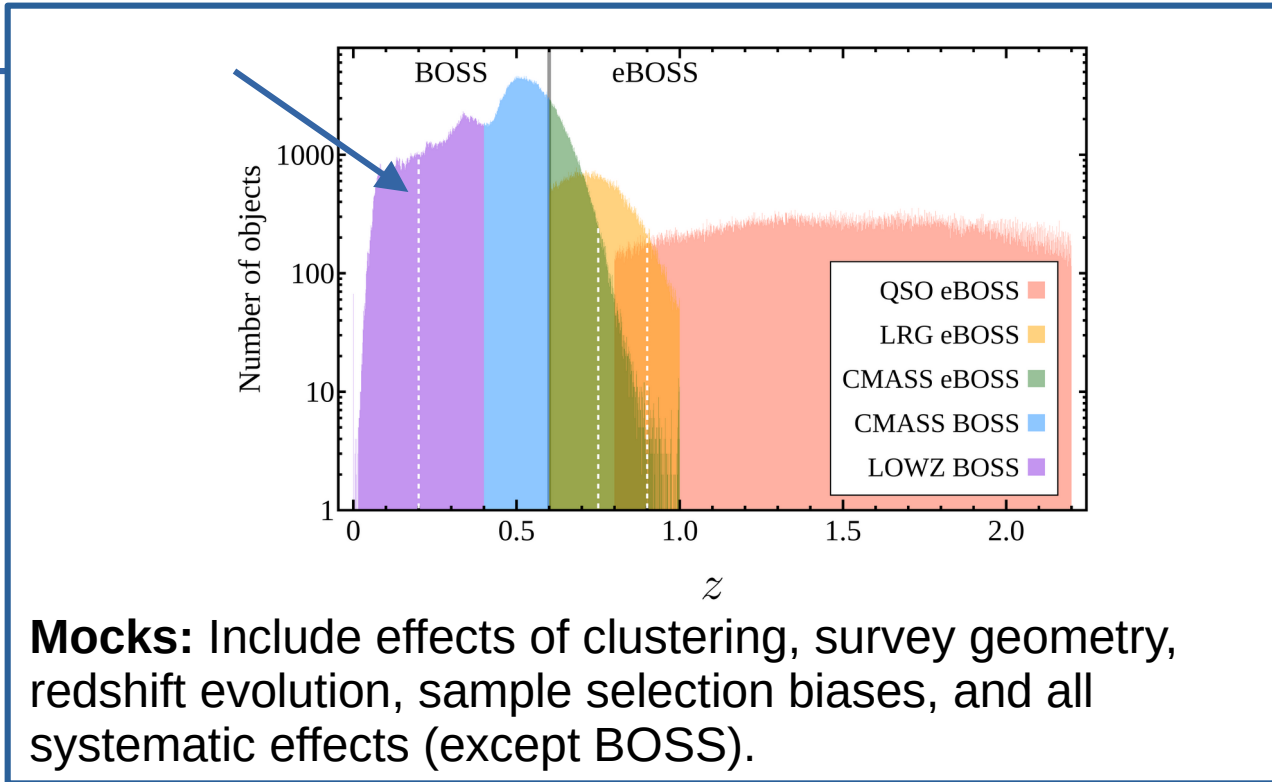
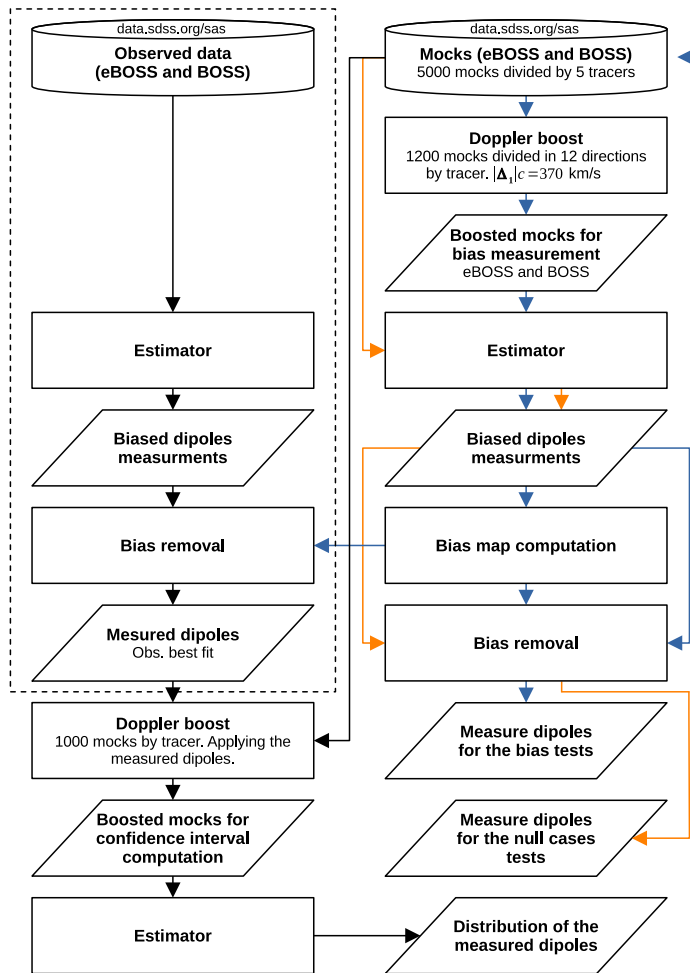
Measuring the dipolar modulation



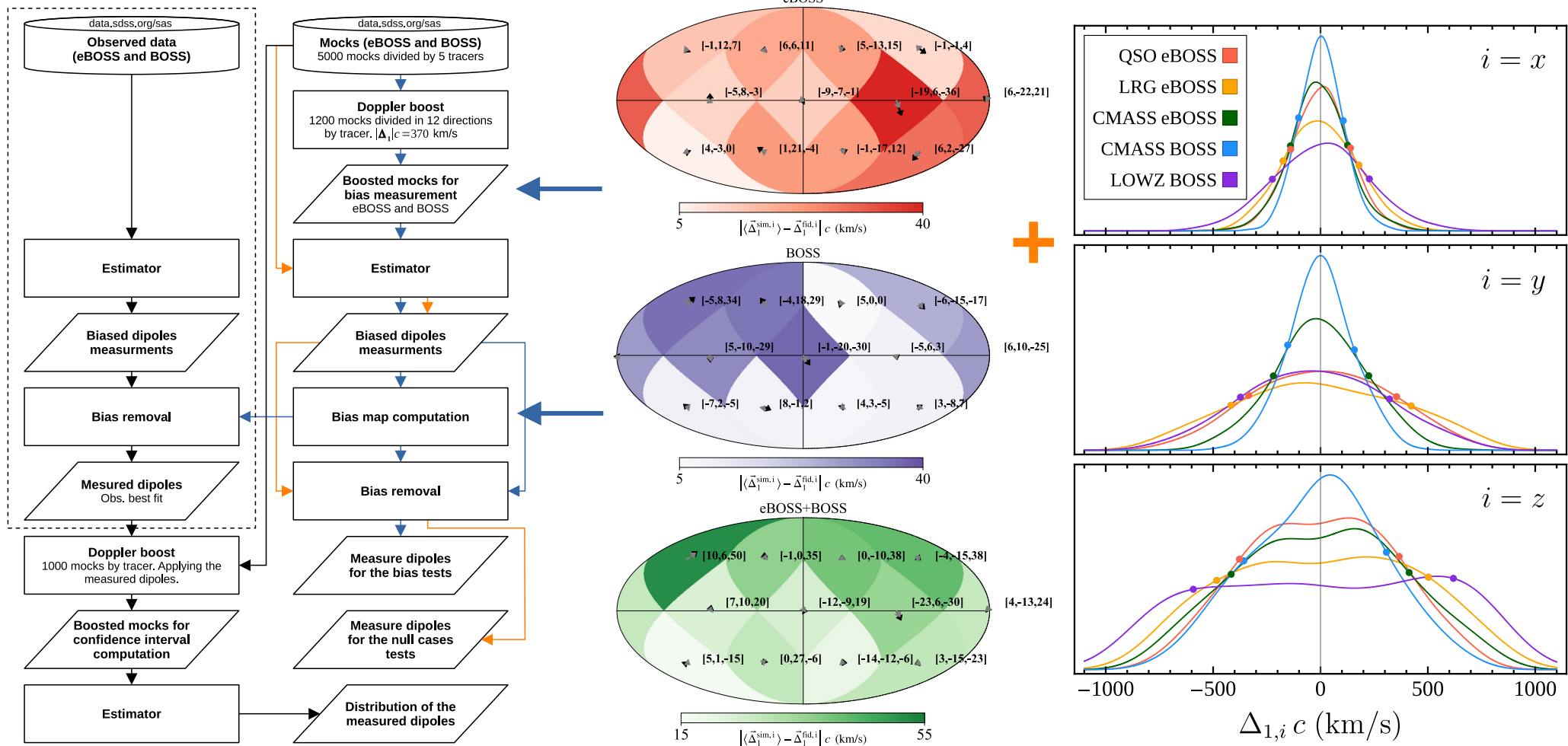
Realistic error bars: Survey systematics, including observational strategies, footprint inhomogeneities, and variations in sky and telescope conditions, will affect the errors and could introduce measurement bias. To assess and then adjust for this bias, we developed a series of mock catalogs from **eBOSS's EZmock** sample and **BOSS's MultiDark-Patchy mocks**. Notably, we utilized the realistic version of EZmock, which incorporates observational systematics, unlike the MultiDark-Patchy mocks that lack this aspect.

Mocks: Include effects of clustering, survey geometry, redshift evolution, sample selection biases, and all systematic effects (except BOSS).

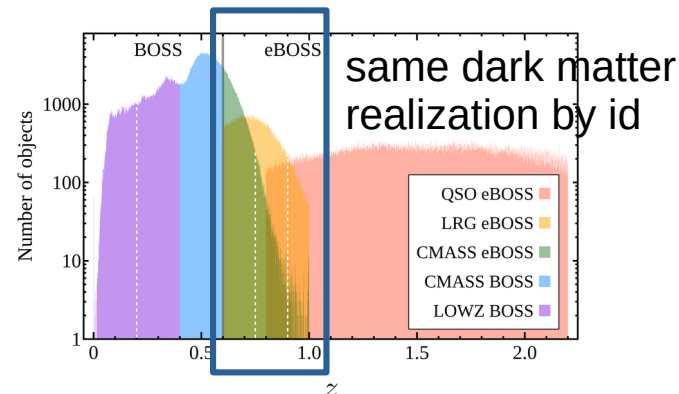
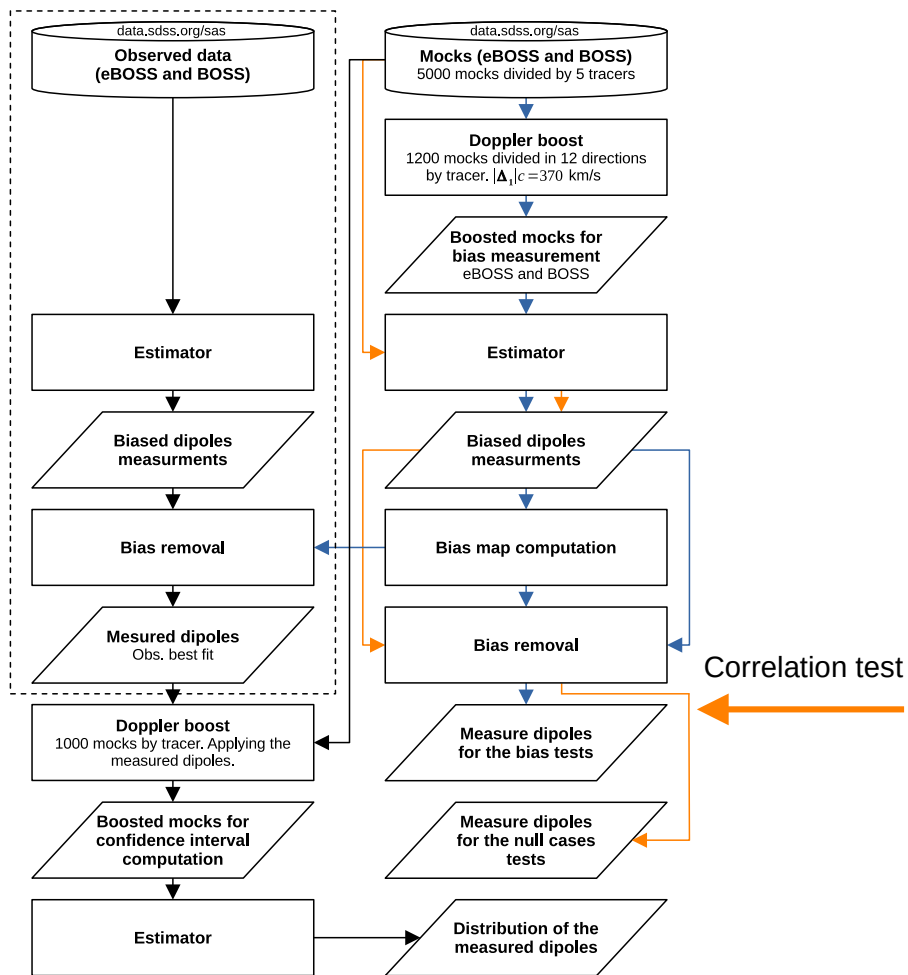
Measuring the dipolar modulation



Measuring the dipolar modulation

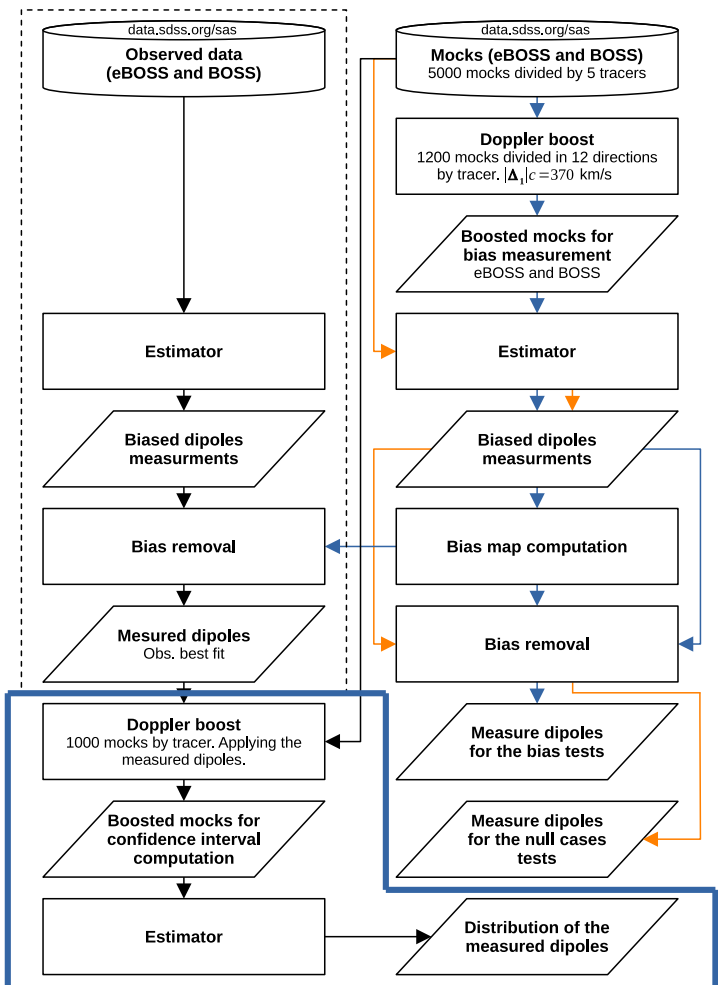


Measuring the dipolar modulation



$$\Delta_1 = -\beta + \Delta_{1,int} + \mathcal{O}(\beta^2)$$

Measuring the dipolar modulation

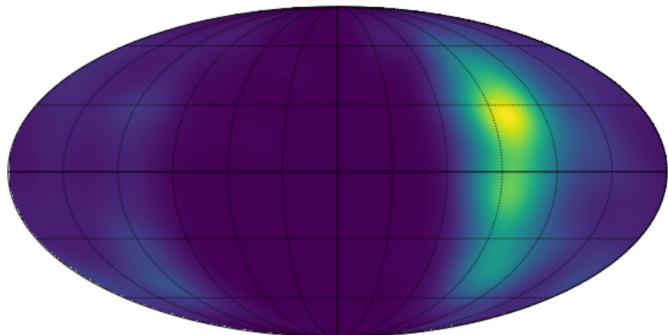


Obtaining the distribution of measured dipoles

Measuring the dipolar modulation

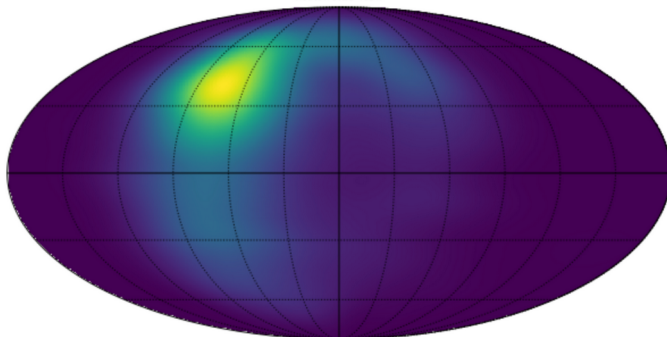
QSO

Mollweide view



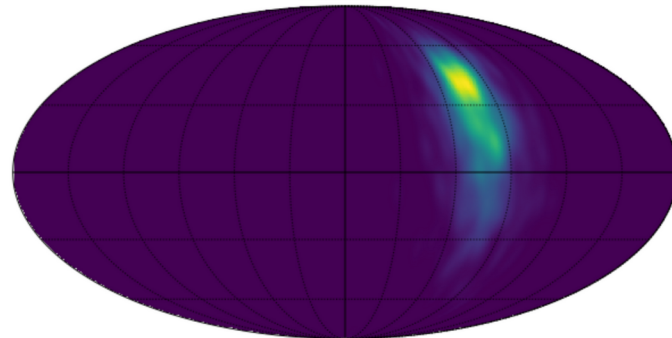
LRG

Mollweide view



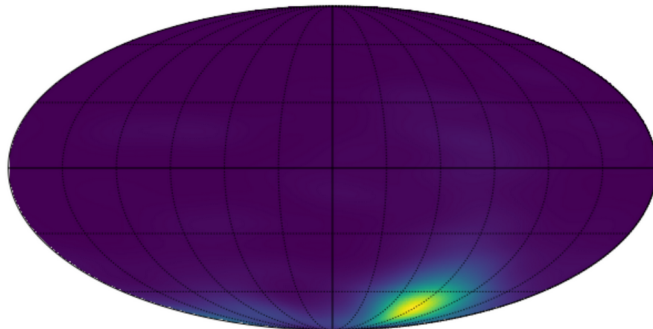
CMASS

Mollweide view



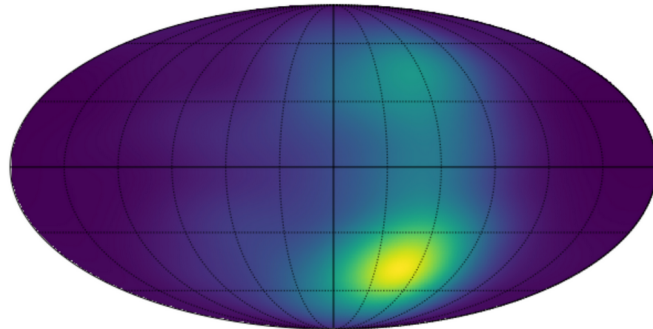
CMASS BOSS

Mollweide view



LOWZ BOSS

Mollweide view

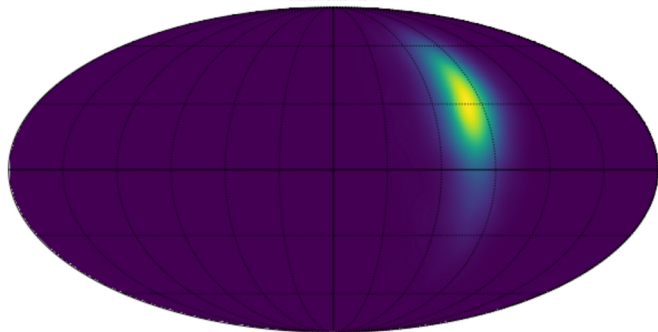


<https://lscsoft.docs.ligo.org/ligo.skymap/>

Measuring the dipolar modulation

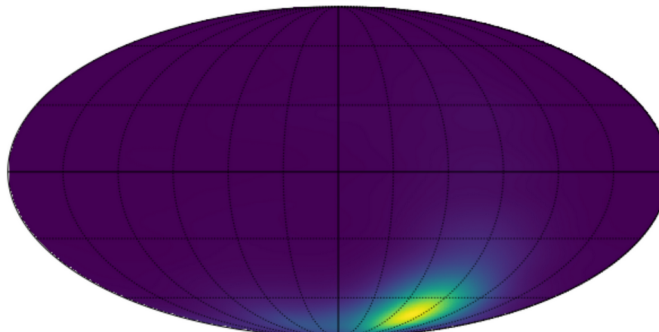
eBOSS

Mollweide view



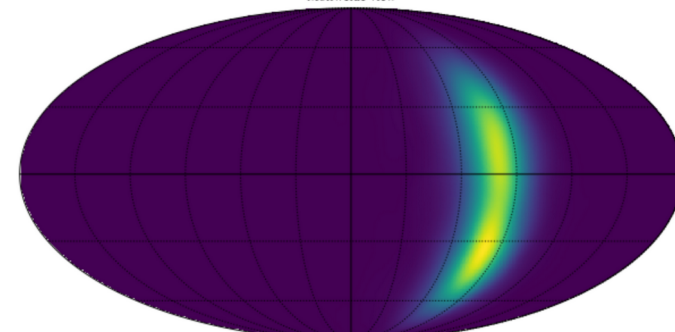
BOSS

Mollweide view



eBOSS+BOSS

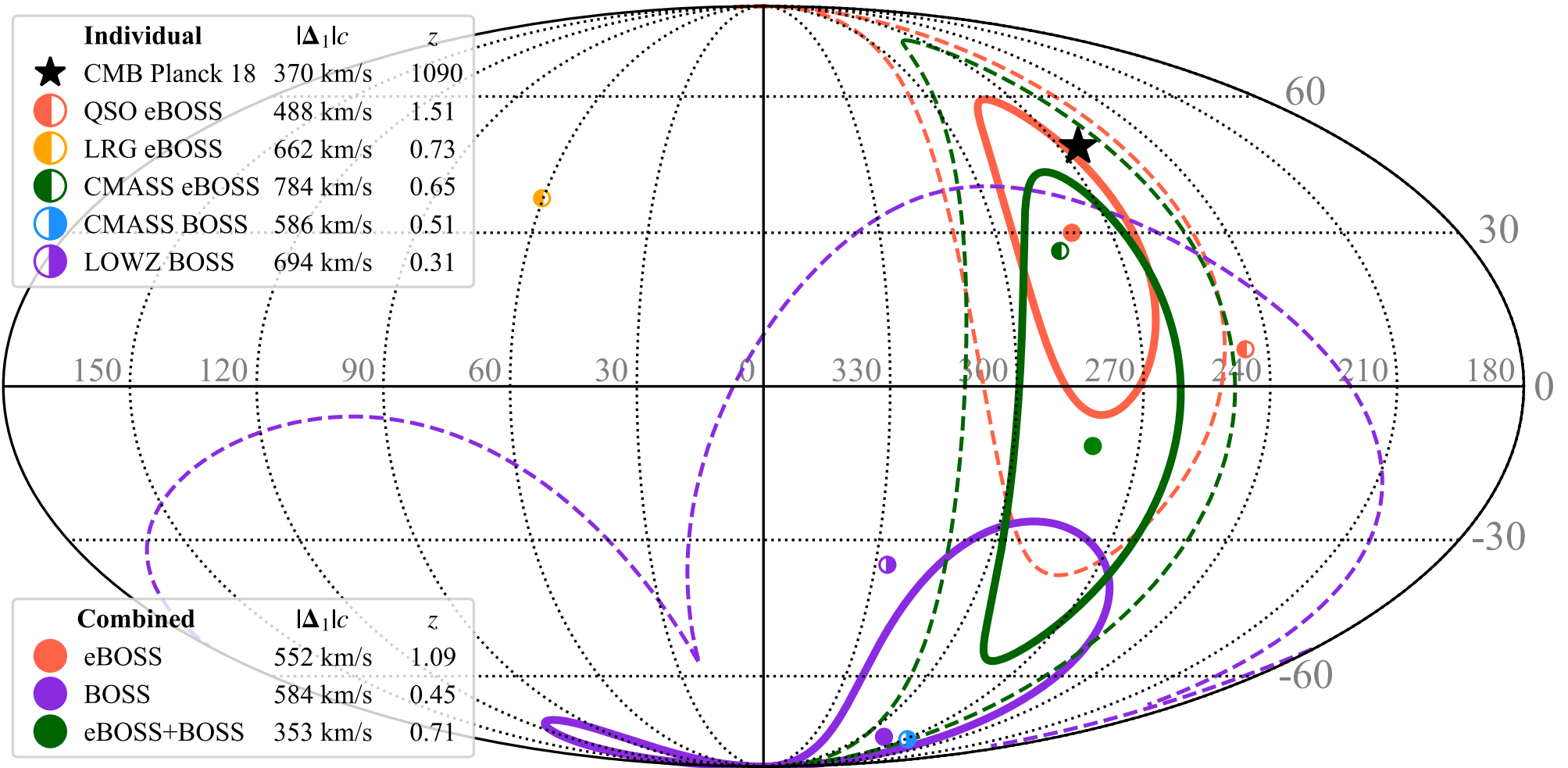
Mollweide view



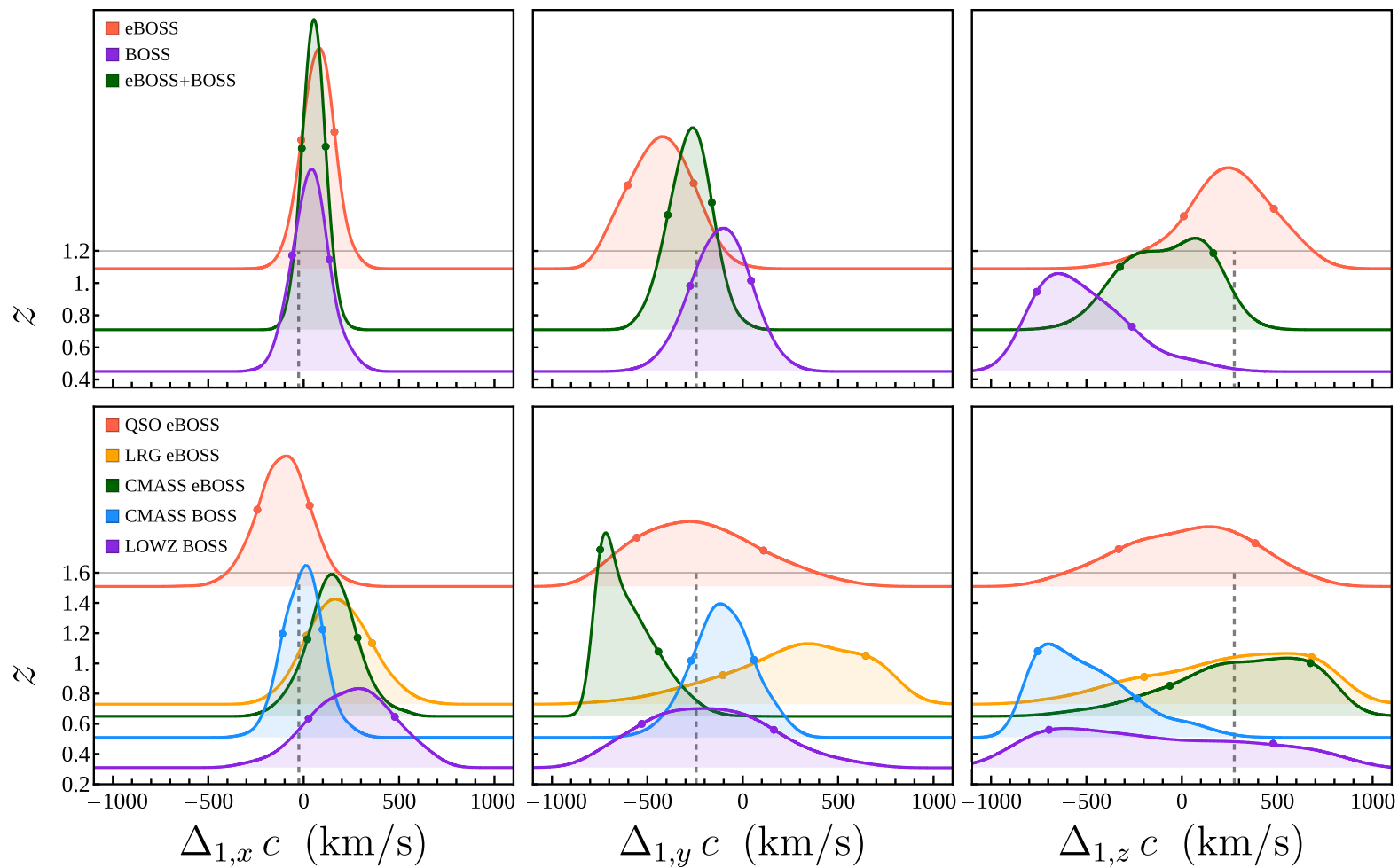
$$\begin{aligned} P_x^{\text{BOSS}} &= P_x^{\text{CMASS BOSS}} \times P_x^{\text{LOWZ BOSS}} \\ P_x^{\text{eBOSS}} &= P_x^{\text{QSO eBOSS}} \times P_x^{\text{LRG eBOSS}} \times P_x^{\text{CMASS eBOSS}} \\ P_x^{\text{eBOSS+BOSS}} &= P_x^{\text{eBOSS}} \times P_x^{\text{BOSS}}, \end{aligned} \quad (11)$$

<https://lscsoft.docs.ligo.org/ligo.skymap/>

Results



Results



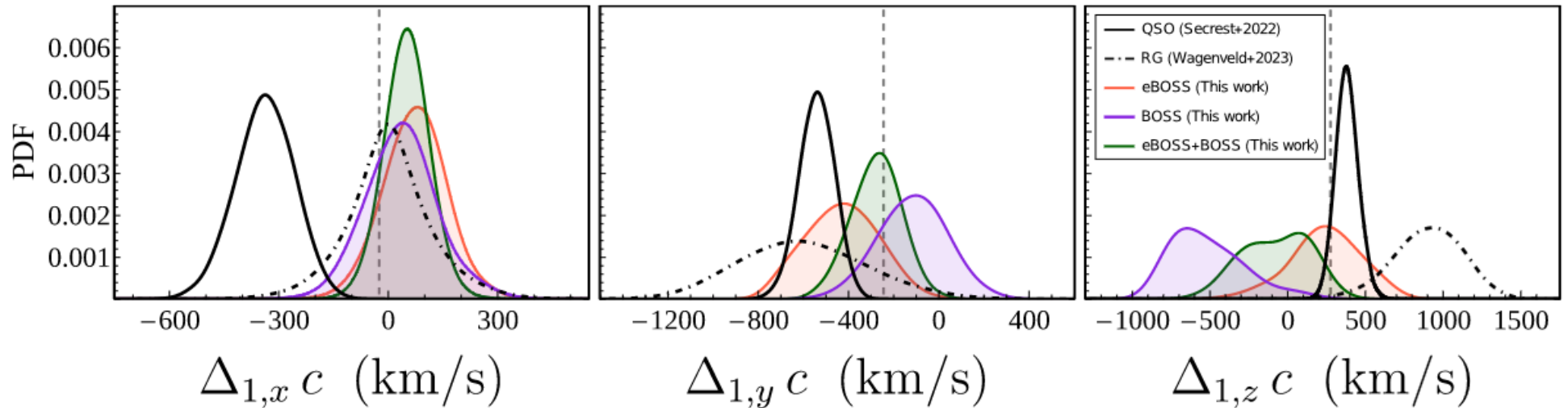
Results

Table 1 | Dipole measurements with 1σ uncertainties and significance of tension against the CMB dipole.

Case	z	Dipole Δ_1			Significance of tension	
		$ \mathbf{v} $ (km/s)	$l(^{\circ})$	$b(^{\circ})$	KDE	Distfit
CMB	1090	$369.8^{+0.1}_{-0.1}$	$264.02^{+0.01}_{-0.01}$	$48.253^{+0.005}_{-0.005}$	–	–
Combined	eBOSS	552^{+169}_{-167}	280^{+12}_{-12}	30^{+15}_{-27}	0.8σ	0.8σ
	BOSS	584^{+180}_{-243}	286^{+25}_{-146}	-77^{+52}_{-4}	2.1σ	1.9σ
	eBOSS+BOSS	353^{+123}_{-111}	281^{+14}_{-14}	-11^{+39}_{-30}	1.4σ	1.3σ
Individual	QSO eBOSS	488^{+207}_{-187}	245^{+30}_{-89}	7^{+33}_{-44}	0.2σ	0.2σ
	LRG eBOSS	662^{+200}_{-240}	60^{+232}_{-22}	37^{+14}_{-58}	1.0σ	1.0σ
	CMASS eBOSS	784^{+150}_{-160}	285^{+10}_{-13}	26^{+18}_{-33}	1.6σ	1.2σ
	CMASS BOSS	586^{+196}_{-251}	269^{+34}_{-143}	-78^{+62}_{-4}	2.1σ	1.6σ
	LOWZ BOSS	694^{+198}_{-247}	327^{+6}_{-284}	-35^{+73}_{-16}	0.6σ	0.6σ

To evaluate the two-tailed significance, we compare the dipoles to the CMB value in Cartesian coordinates using two methods: a non-parametric Kernel Density Estimation (KDE) with a Gaussian kernel and a parametric best-fit distribution analysis conducted using the `Distfit` Python module³⁹. The table additionally lists the effective redshift for each scenario. For BOSS and eBOSS data, this corresponds to the weighted average redshift, which is equivalent to the monopole.

Comparing



Extended Data Fig. 6 | Comparison of dipole measurements in Cartesian coordinates with previous estimates. The distributions for eBOSS, BOSS, eBOSS+BOSS analyses correspond to those presented in Fig. 5.

Conclusions

Our redshift dipole measurements show agreement with the CMB dipole, exhibiting a tension of 0.8σ for eBOSS data ($0.6 < z < 2.2$), 2.1σ for BOSS data ($0.2 < z < 0.6$), and 1.4σ for combined eBOSS+BOSS data ($0.2 < z < 2.2$). The most notable, albeit moderate, tension with the anticipated dipole arises from BOSS data within the redshift range $0.2 < z < 0.6$, where our findings suggest a deviation towards the southern hemisphere, despite the dipole's magnitude closely matching expectations.

These results reveals that our motion with respect to distant galaxies and quasars is in close agreement with that suggested by the CMB dipole, as illustrated in Fig. 3 in both Galactic and Cartesian coordinates. This concordance implies that matter at cosmological distances of 1–5 Gpc shares the same rest frame as the CMB, located approximately 14 Gpc away, offering substantial support to the cosmological principle, which advocates for large-scale homogeneity and isotropy. Moreover, our results suggest that previous assertions of discrepancies with the CMB dipoles might stem from overlooked systematic influences, such as the redshift evolution modeling of observables, biases in the estimators or the underestimation of uncertainties

Update: V3 coming (1~2 weeks) + Perspectives

- 3 typos in equations.
- Absolute values are a bit biased due to small inconsistency during analysis, they are smaller than presented in V2. Conclusions will remain the same. Still compatible with the CMB dipole and in tension with previous number count dipoles. It seems that LOWZ was only noise (estimator does not minimized).

Thanks for your attention!