

# Quark Gluon Plasma

*Rajiv V. Gavai*  
*T. I. F. R., Mumbai*

# Quark Gluon Plasma : From Lattice QCD

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Introduction

Basic Lattice QCD

FTQCD Results

Summary

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  - Even if Higgs is found,  $m_{u,d}$  can be understood only if  $g_{qqH} \sim 10^{-6}$  is experimentally established.
  - But QCD uniquely has very high interaction (binding) energies. E.g.,  $M_{Proton} \gg (2m_u + m_d)$ , by a factor of 100  $\rightarrow$  Understanding it is knowing where the Visible mass of Universe comes from.



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- Much richer structure : Quark Confinement, Dynamical Symmetry Breaking..
- Non-perturbative techniques needed for real precision tests of QCD.

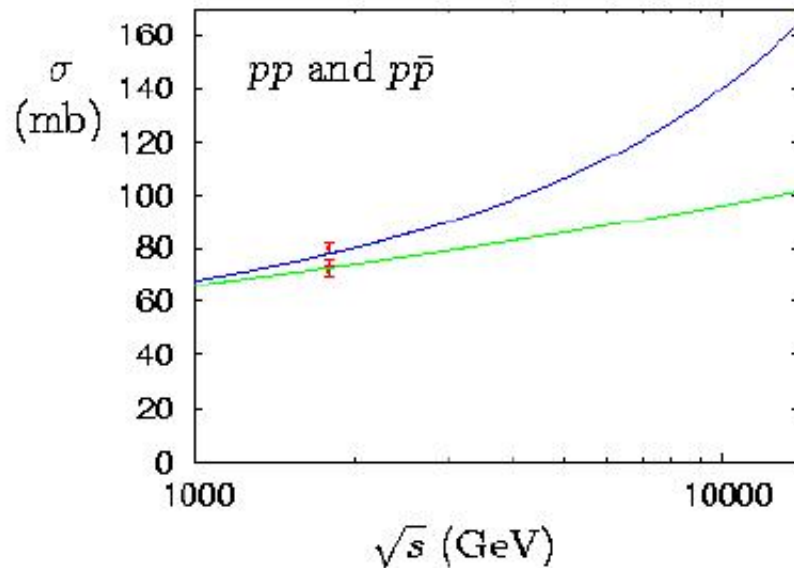
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- Much richer structure : Quark Confinement, Dynamical Symmetry Breaking..
- Non-perturbative techniques needed for real precision tests of QCD.
- QCD too complex  $\rightsquigarrow$  Simple models based on underlying symmetries are often employed, making them a weak link in precision tests : BSM physics may show up in non-perturbative QCD beyond these models.

# Total Cross Section at LHC

Predicted  $\sigma^{\text{tot}} = 125 \pm 25 \text{ mb}$  !

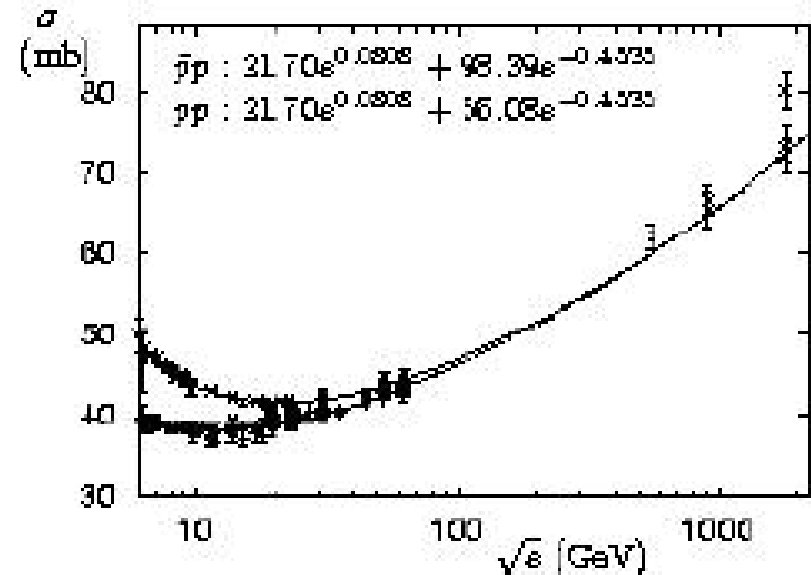
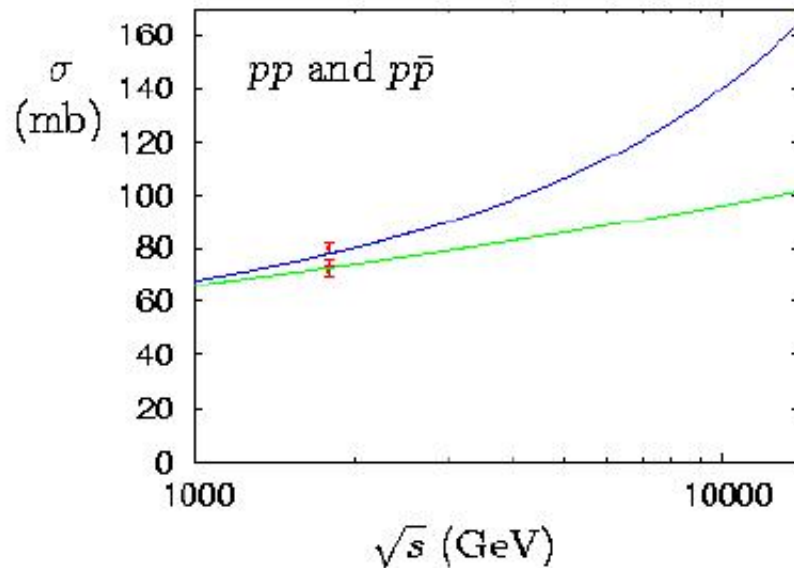
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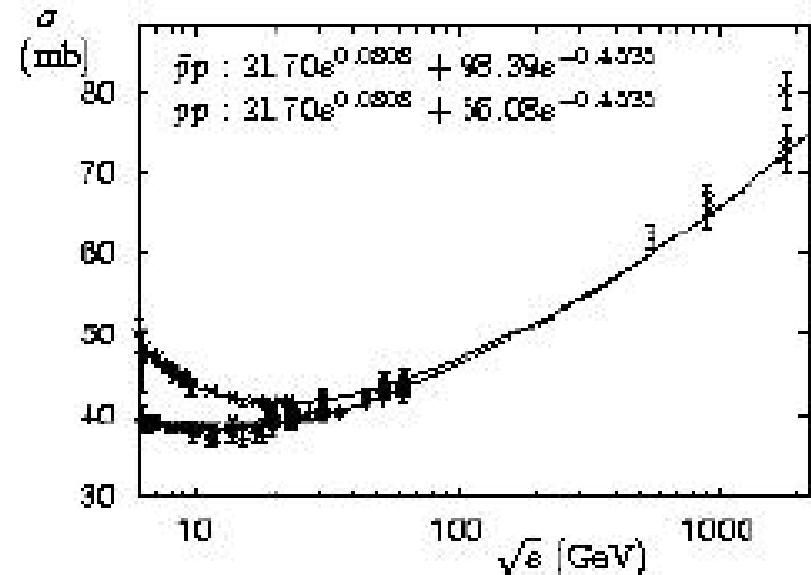
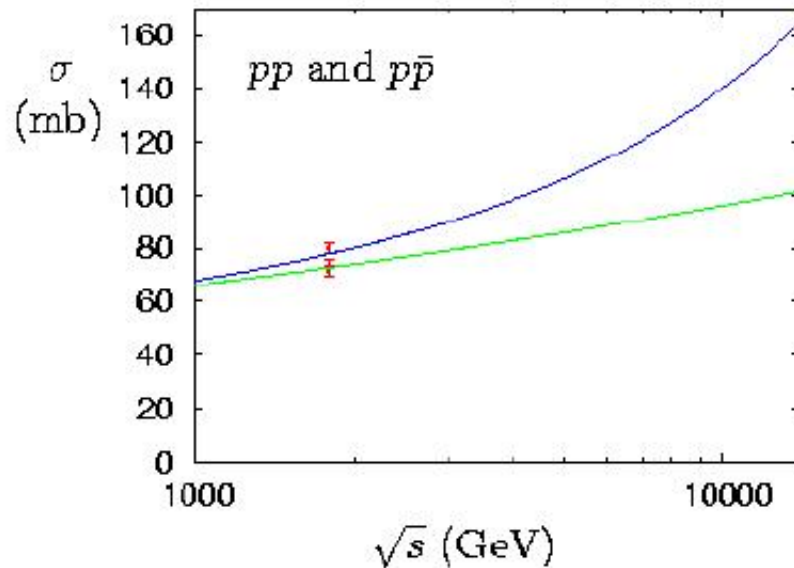
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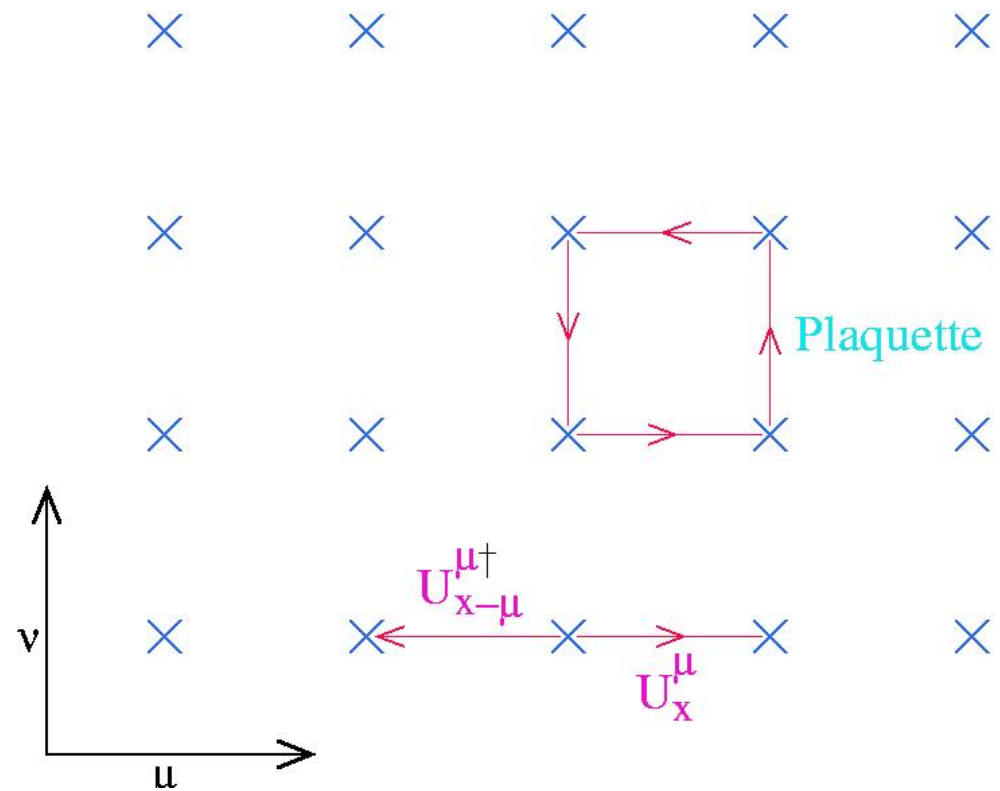


These Regge Models can explain the  $Q^2$ -variation of  $F_2$  as well.

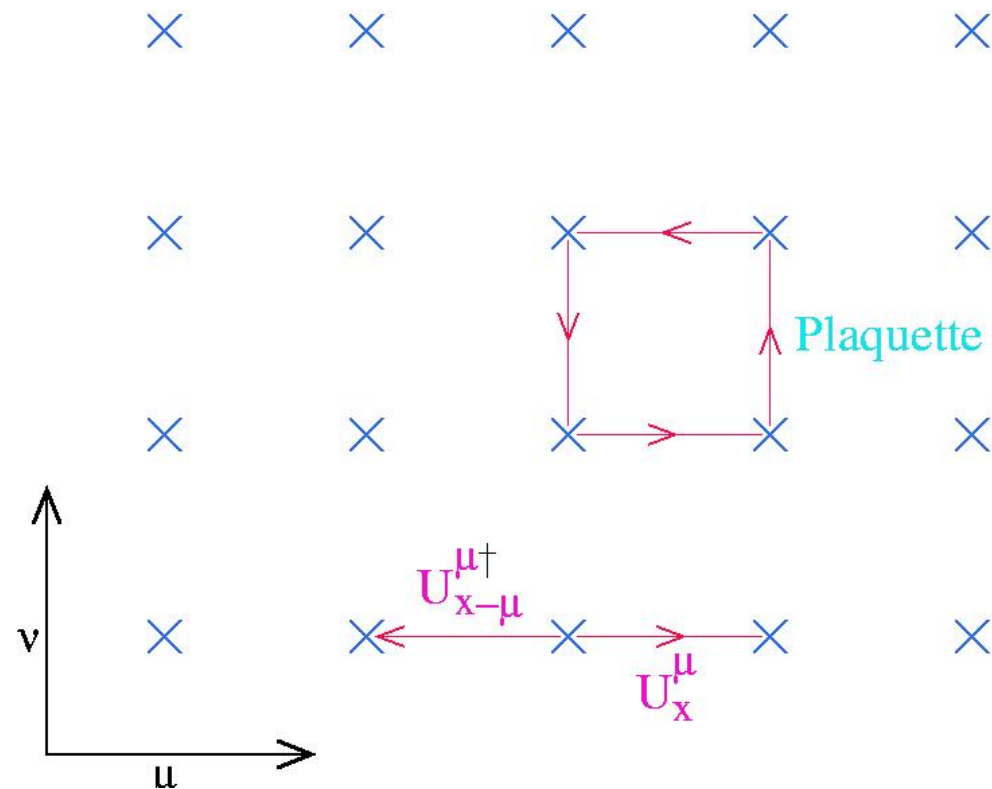
# Basic Lattice QCD



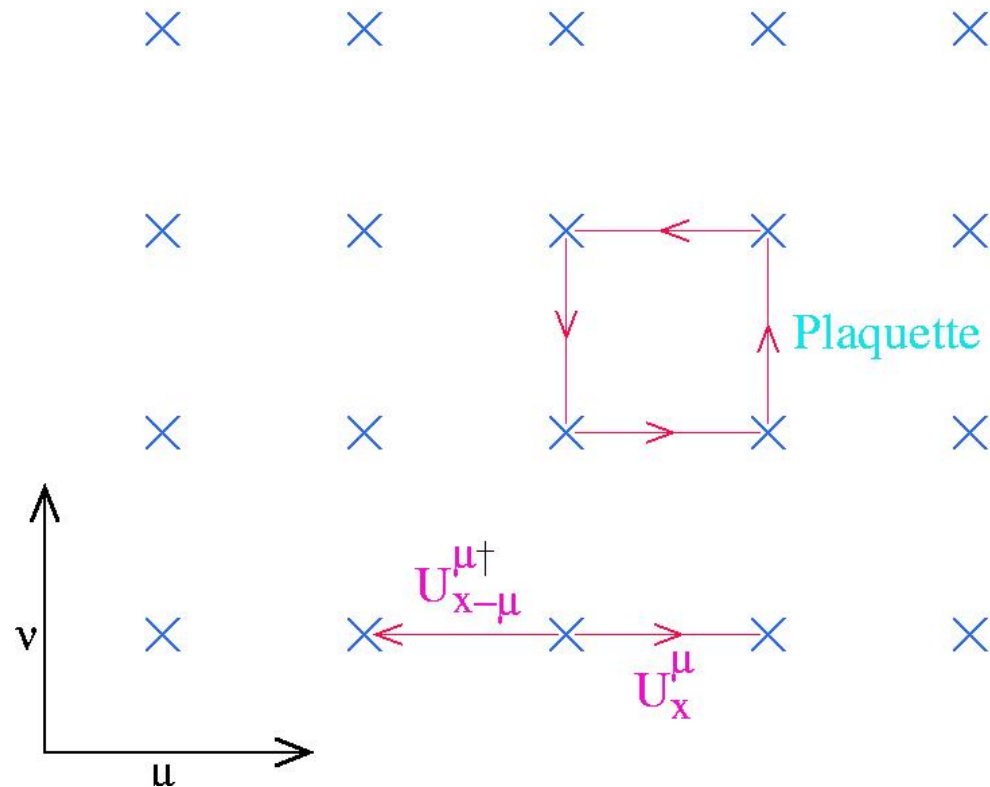
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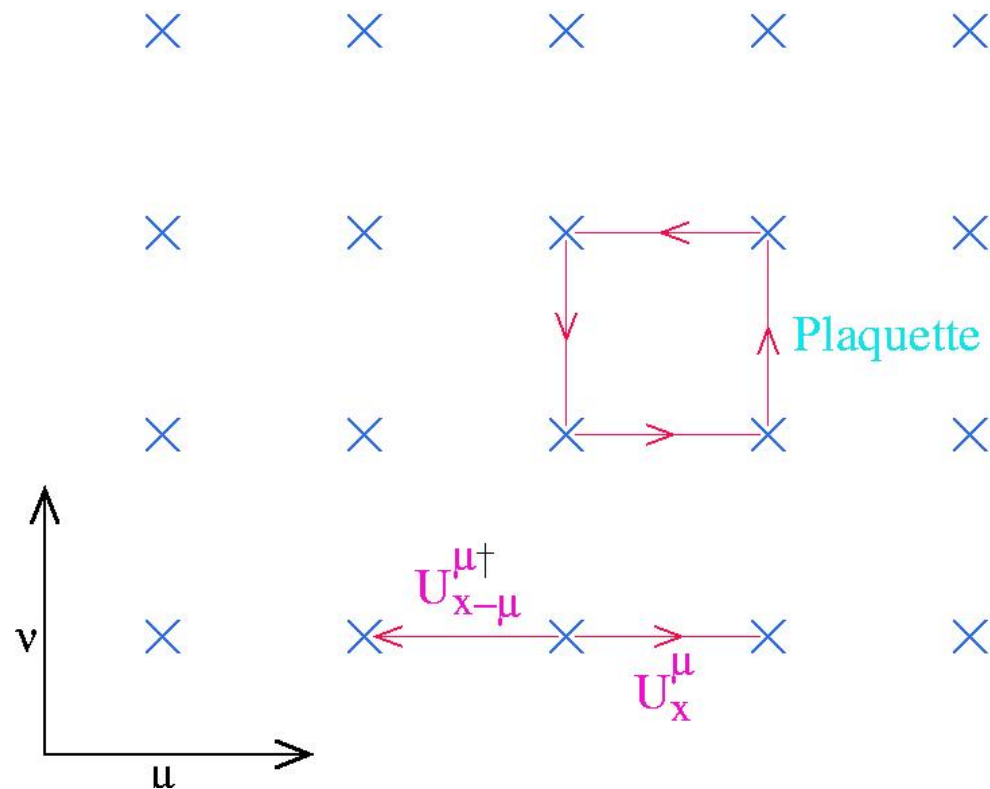
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- Fermion Actions : Staggered, Wilson, Overlap..

Typically, we need to evaluate

$$\langle \Theta(m_v) \rangle = \frac{\int DU \exp(-S_G) \Theta(m_v) \text{Det } M(m_s)}{\int DU \exp(-S_G) \text{Det } M(m_s)}, \quad (1)$$

where  $M$  is the Dirac matrix in  $x$ , colour, spin, flavour space for fermions of mass  $m_s$ ,  $S_G$  is the gluonic action, and the observable  $\Theta$  may contain fermion propagators of mass  $m_v$ .

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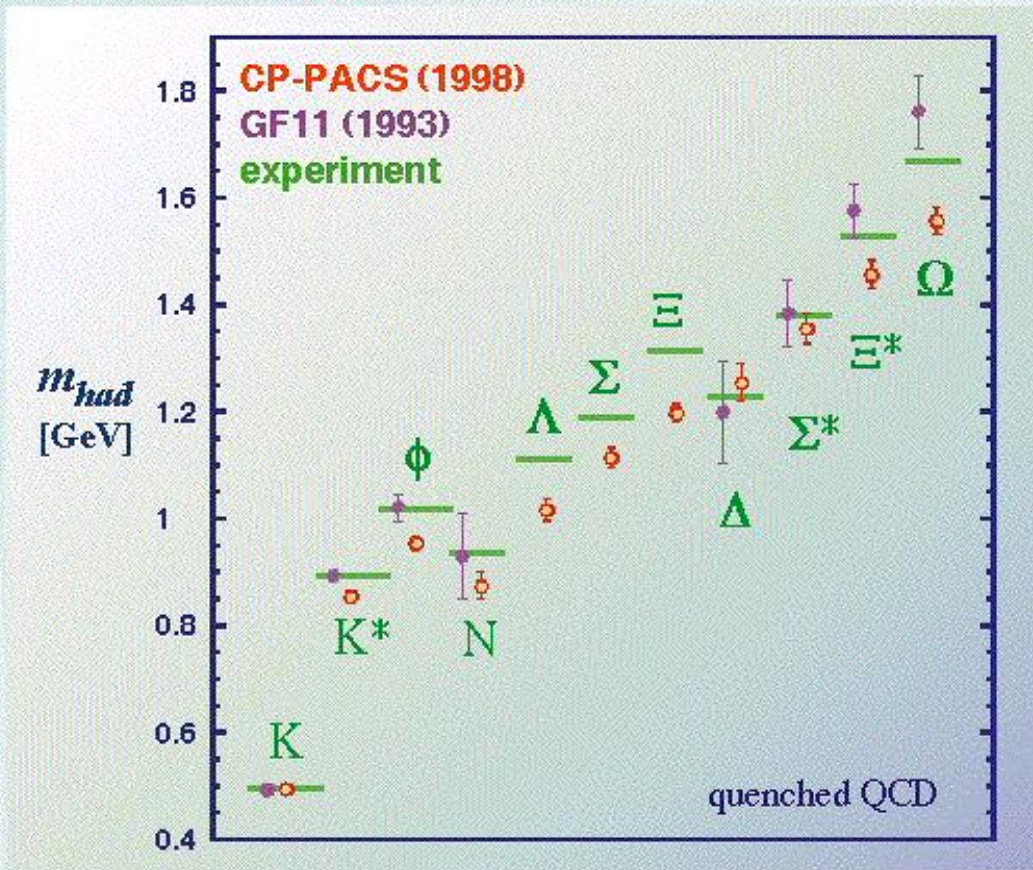
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Complexity of evaluation of  $\text{Det } M \implies$  approximations : Quenched (  $m_s = \infty$  limit) and Full ( low  $m_s = m_u = m_d$  ).

Q  $\rightarrow$  Full  $\rightsquigarrow$  Computer time  $\uparrow$  and Precision  $\downarrow$ .



# Hadron Mass Spectrum from Quarks and Gluons

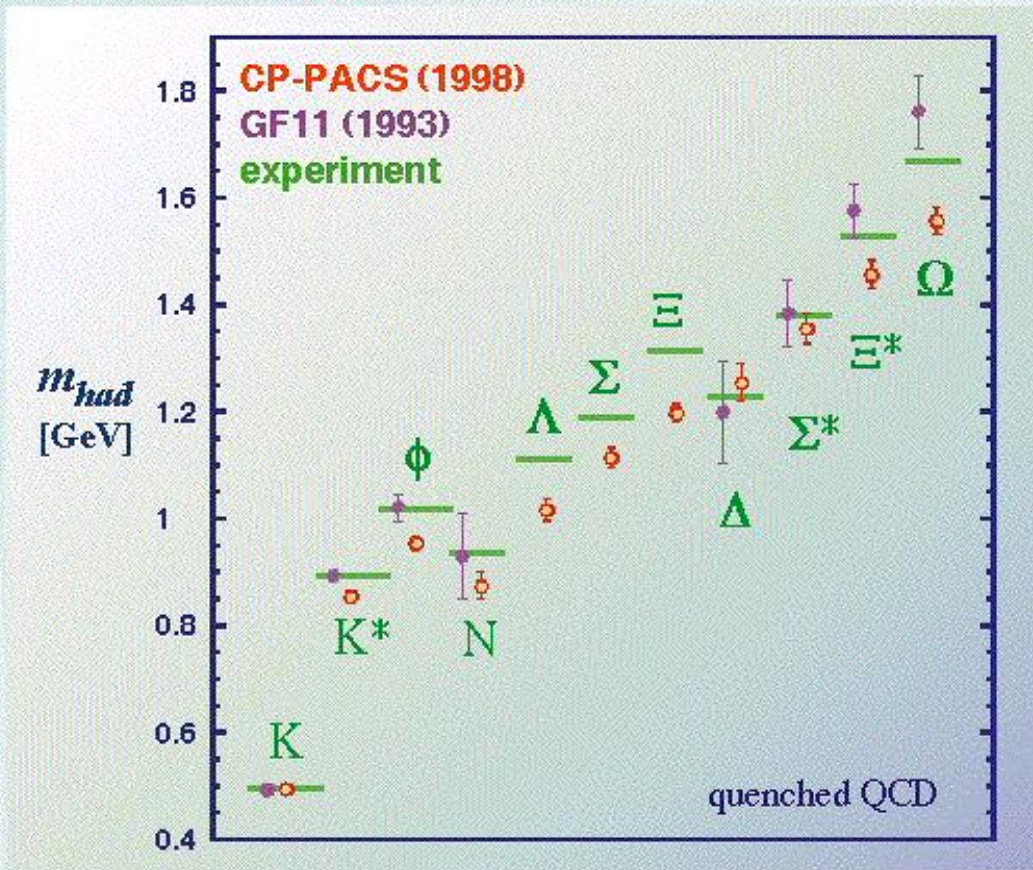


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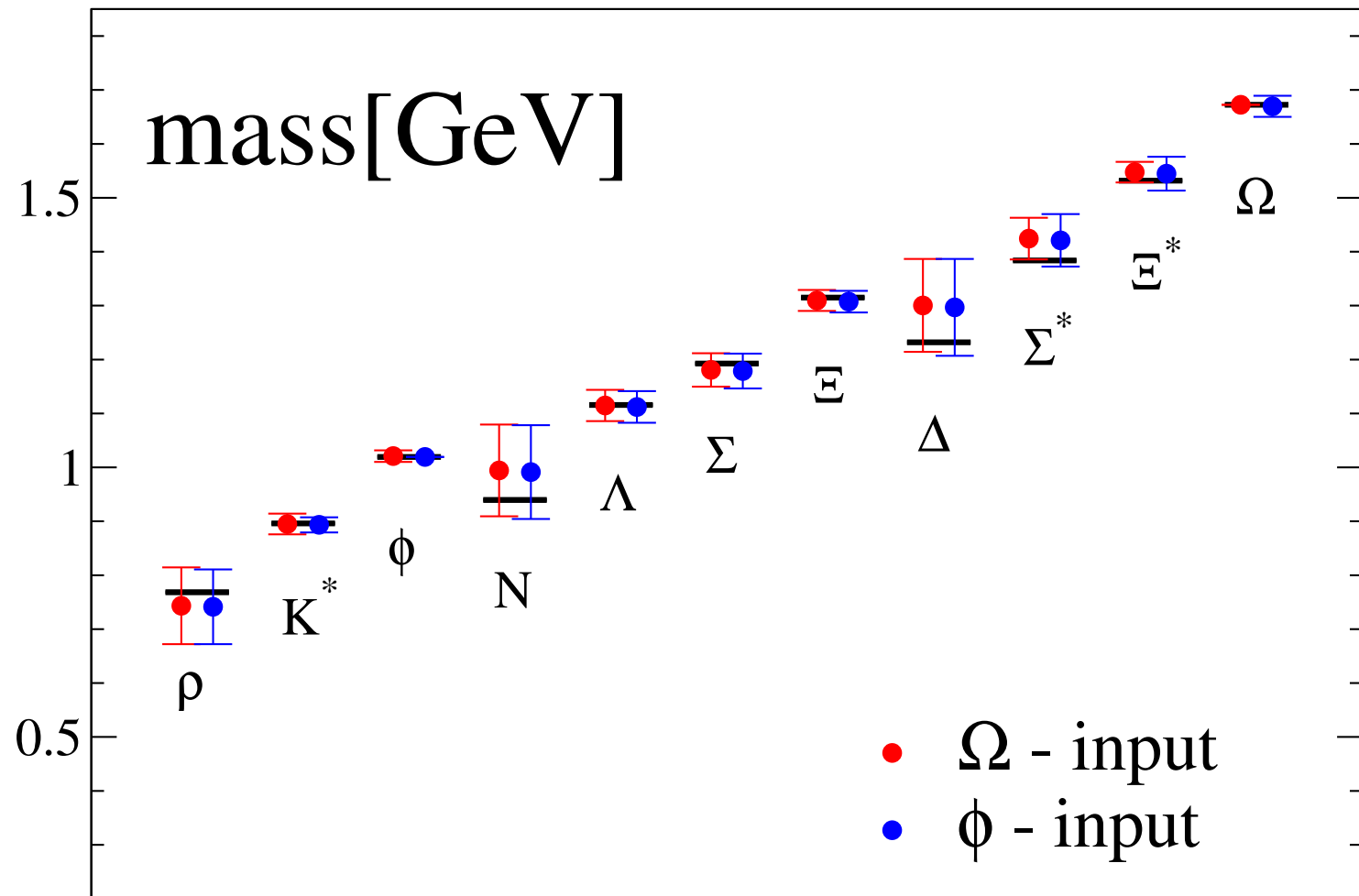
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♡ Massless quarks acquire mass dynamically : Vacuum breaks Chiral Symmetry, i.e,  $\langle \bar{\psi}\psi \rangle \neq 0$ .

♡ Goldstone nature of Pion established:

$$m_{\pi}^2 \propto m_q.$$



Dynamical 2+1 QCD : N. Ukita et al. [arXiv 0710.3462]

# Non-perturbative Test : QCD Phase Diagram

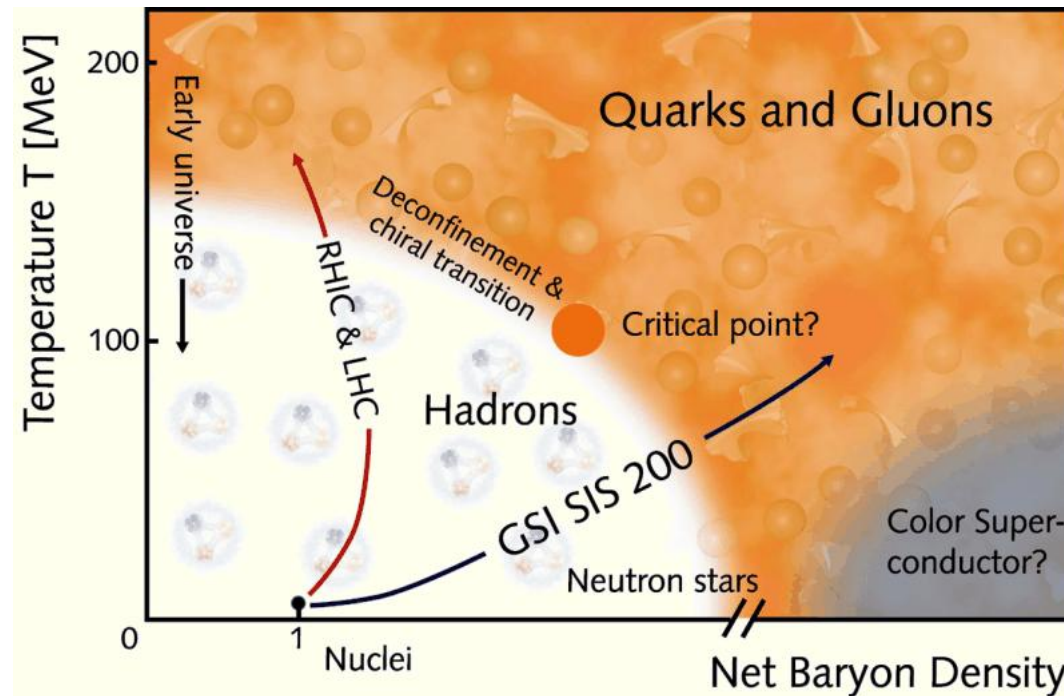
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- Lattice ideal tool to establish the phase diagram and properties of the phases.

# Lattice QCD : What it can do

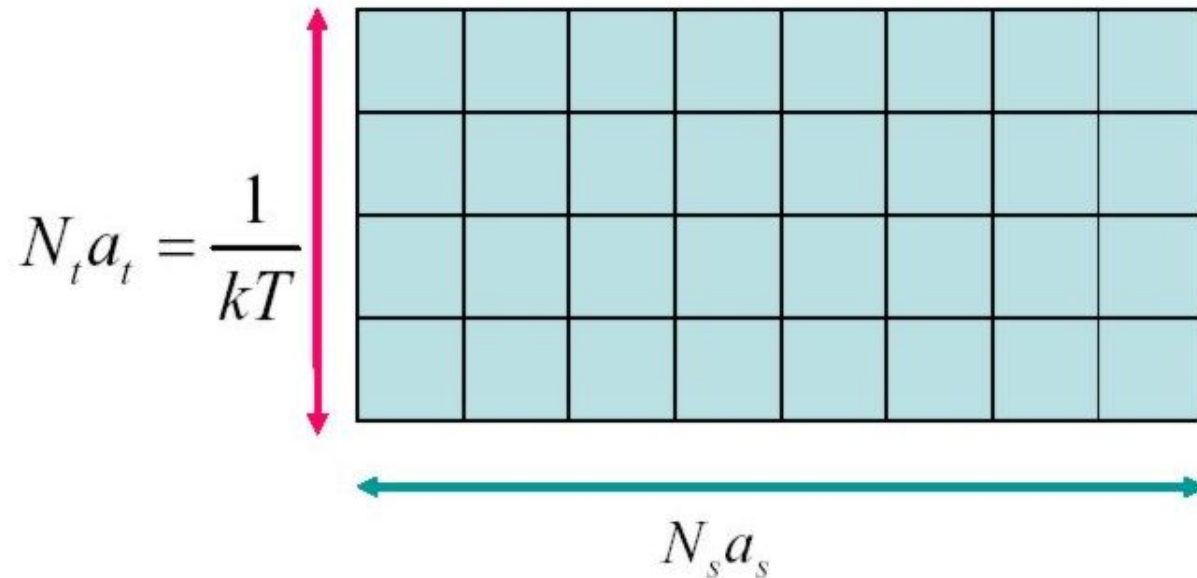
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Need  $N_s \gg N_t$  for thermodynamic limit and large  $N_t$  for continuum limit.

# Symmetries and Order Parameters

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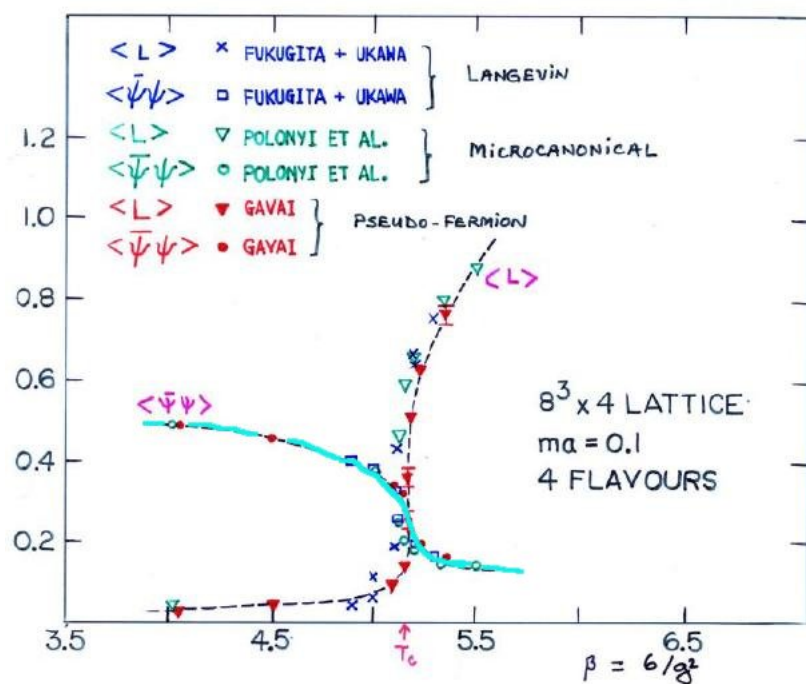
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- Real world with 2 light + 1 moderately heavy flavours. Both symmetries not exact but the order parameters may still act as beacons for transitions.

## Results for QCD at $T \neq 0$

- The Transition Temperature  $T_c \sim 185$  MeV, and Equation of State (EOS) have been predicted by lattice QCD.

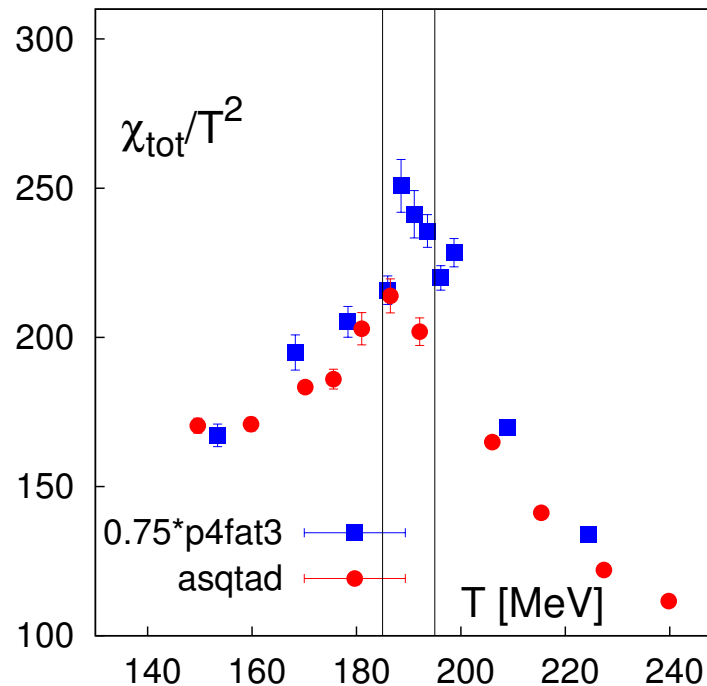
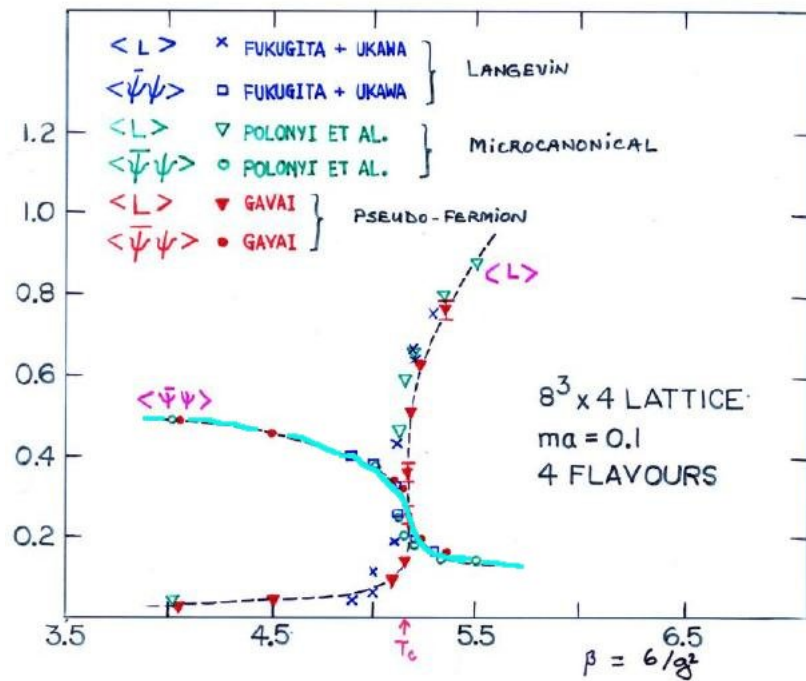
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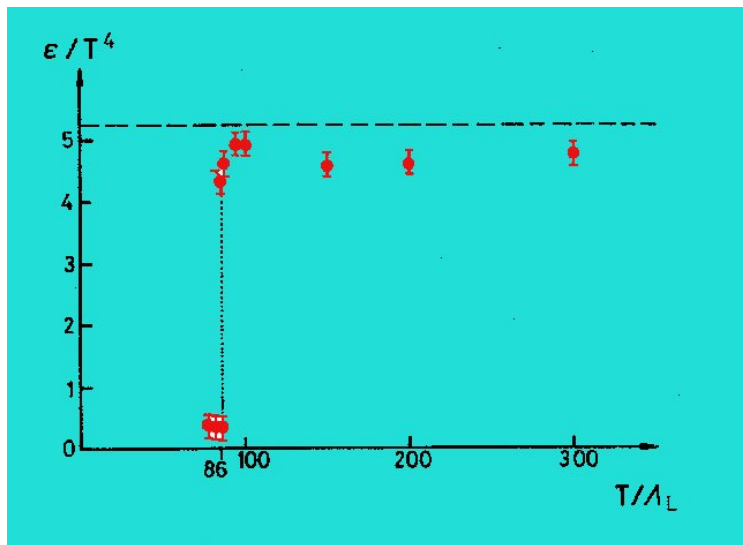
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F. Karsch, Lattice 2007, arxiv:0711.0661.

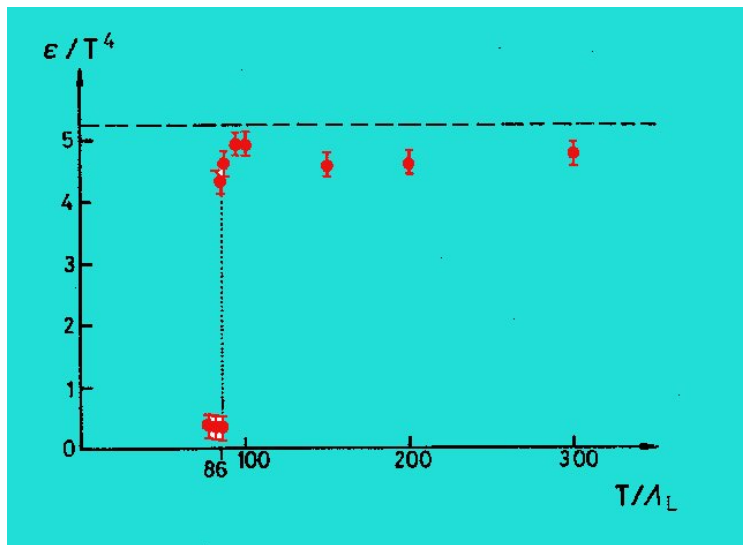
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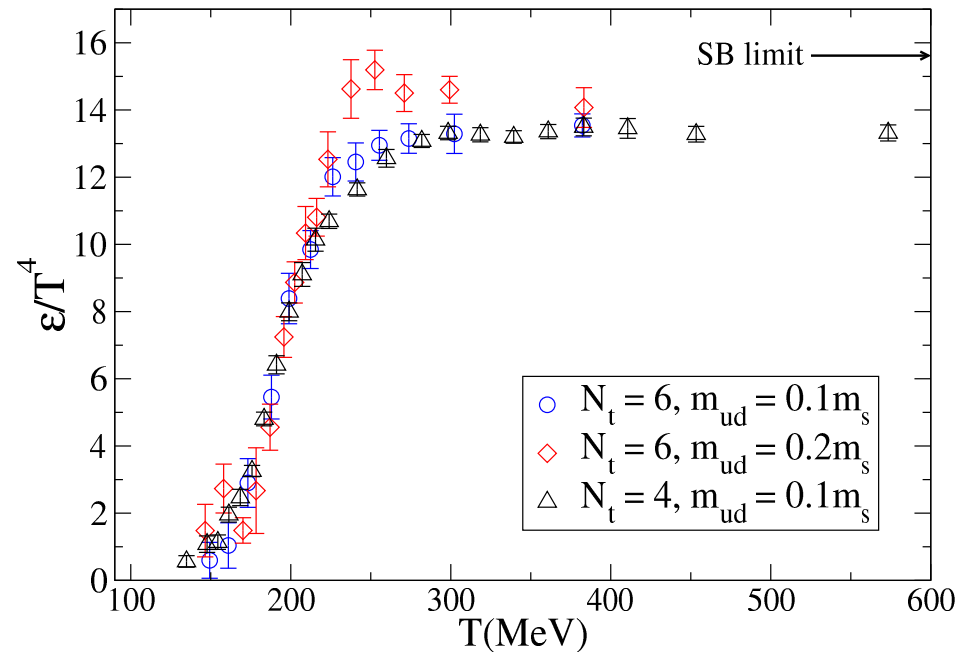


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Celik, Engels & Satz, PLB129, 323 1983

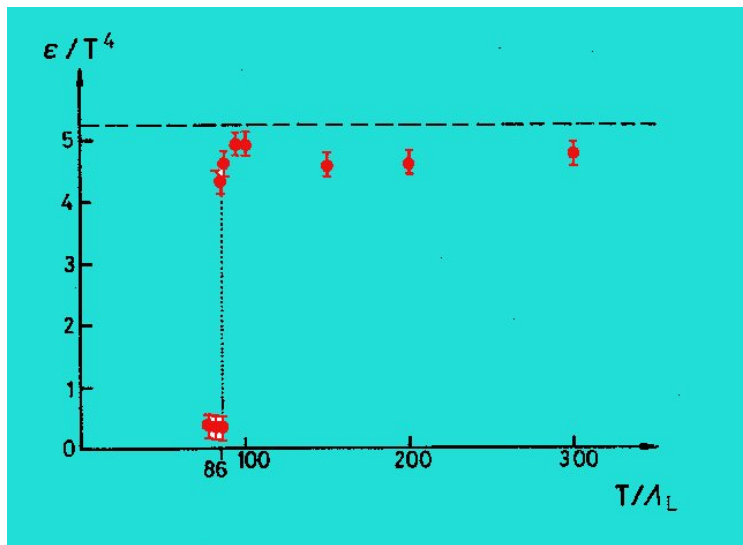


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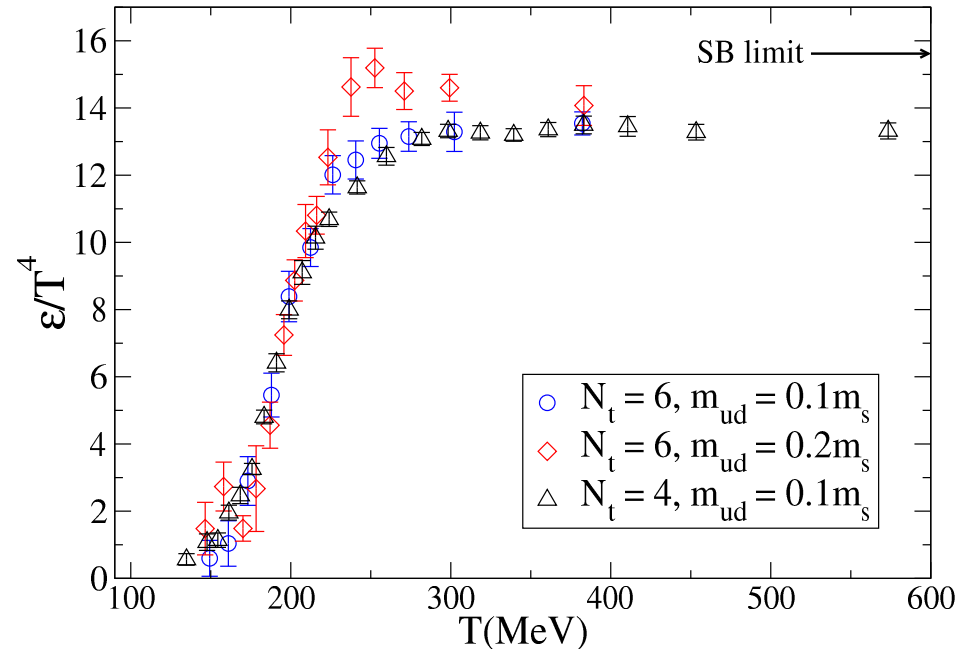
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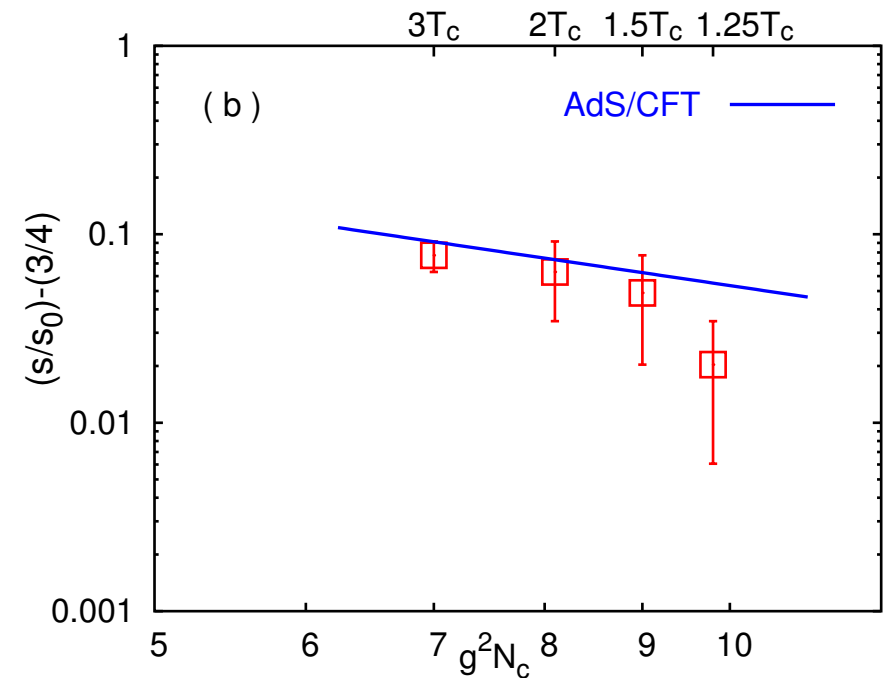
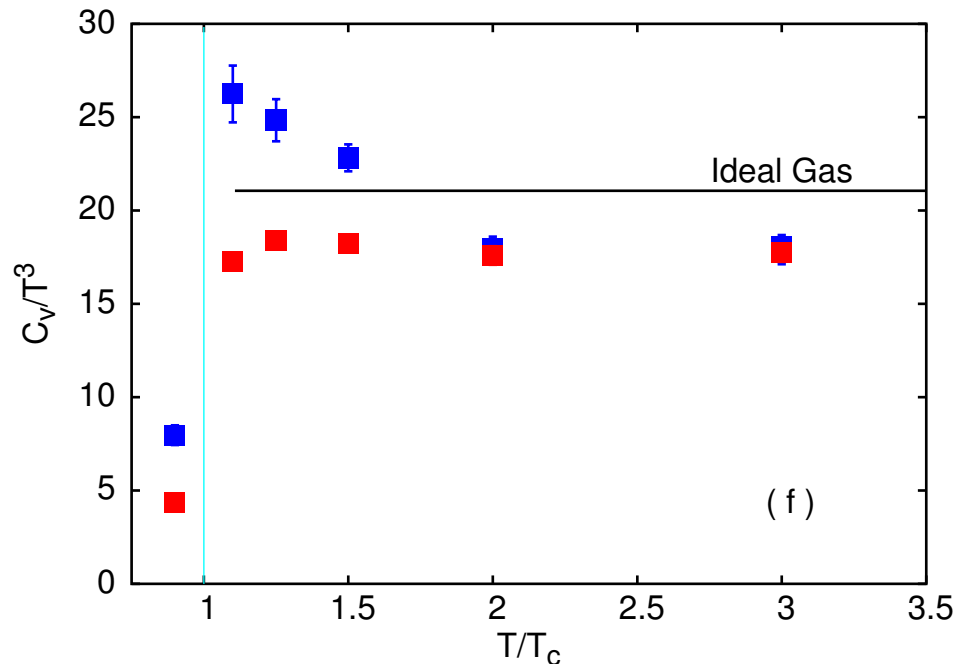


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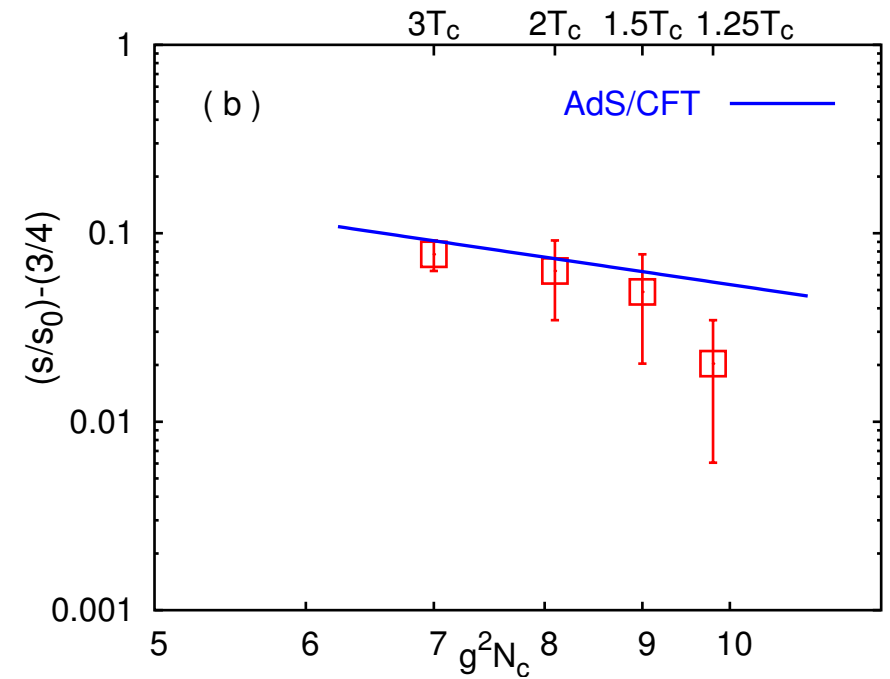
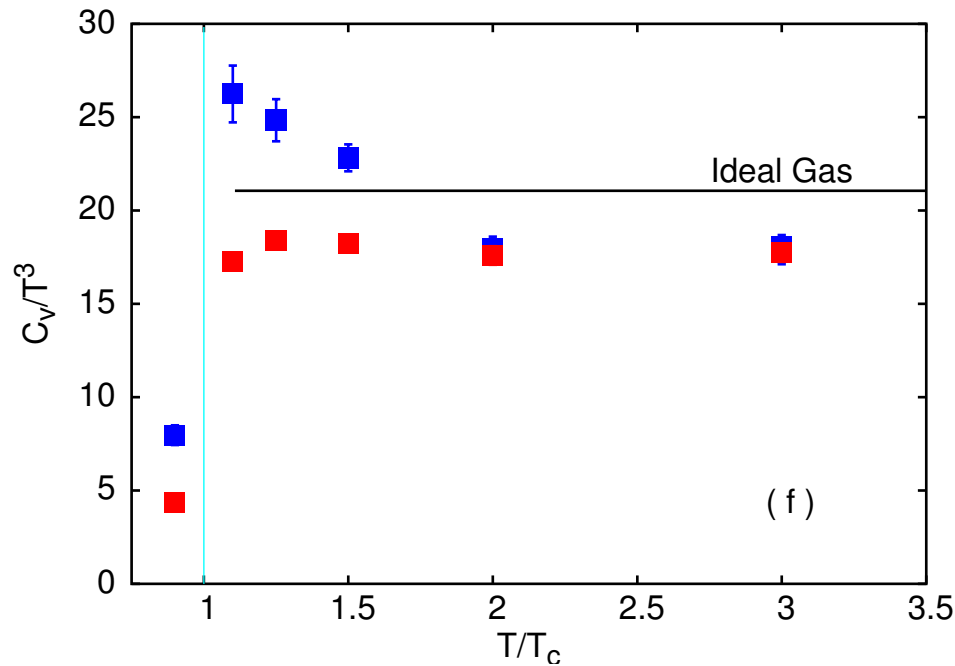
- Recent results for EoS :  $N_t=6$ , Smaller quark masses. Small differences for  $N_t = 4$  & 6;  $\epsilon(T_c) \sim 6T_c^4$  still. Too small volumes  $\longrightarrow$  Thermodynamic Limit ?



(RVG, S. Gupta and S. Mukherjee, hep-lat/0506015)

♠  $C_v \sim 4\epsilon$  for  $2T_c$  but No Ideal Gas limit.



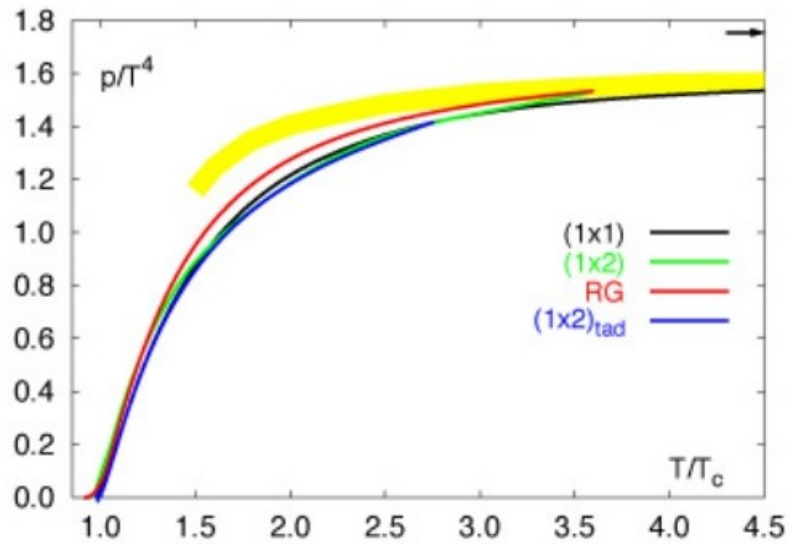


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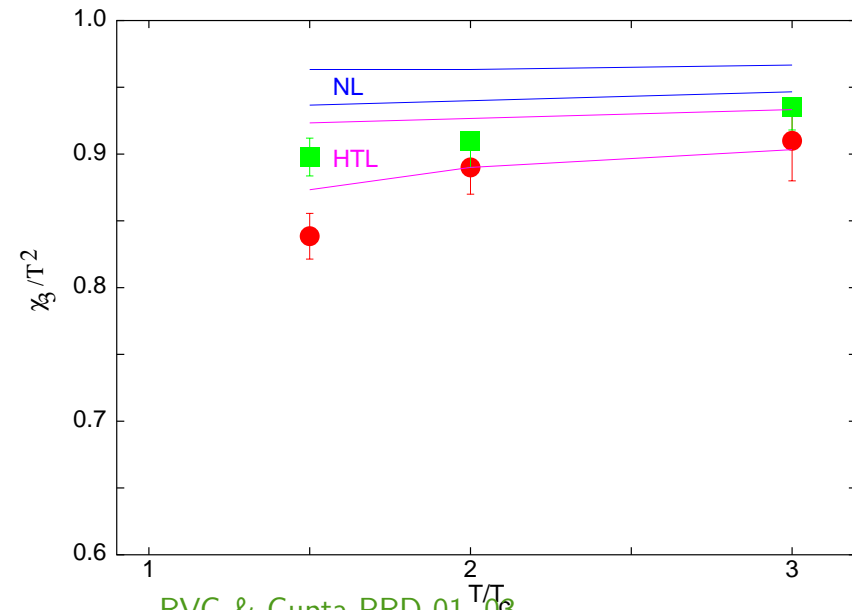
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♠ Entropy agrees with strong coupling SYM prediction (Gubser, Klebanov & Tseytlin, NPB '98, 202) for  $T = 1.5 - 3T_c$  but fails at lower  $T$ , as do various weak coupling schemes :  $\frac{s}{s_0} = f(g^2 N_c)$ , where  $f(x) = \frac{3}{4} + \frac{45}{32}\zeta(3)x^{-3/2} + \dots$  and  $s_0 = \frac{2}{3}\pi^2 N_c^2 T^3$ .

# Weak Coupling

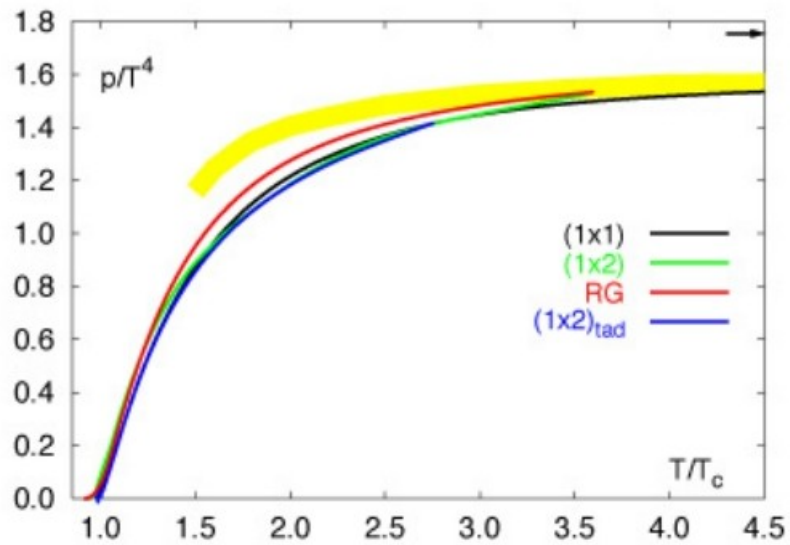


Blaizot, Iancu & Rebhan PRD 01, PLB 01

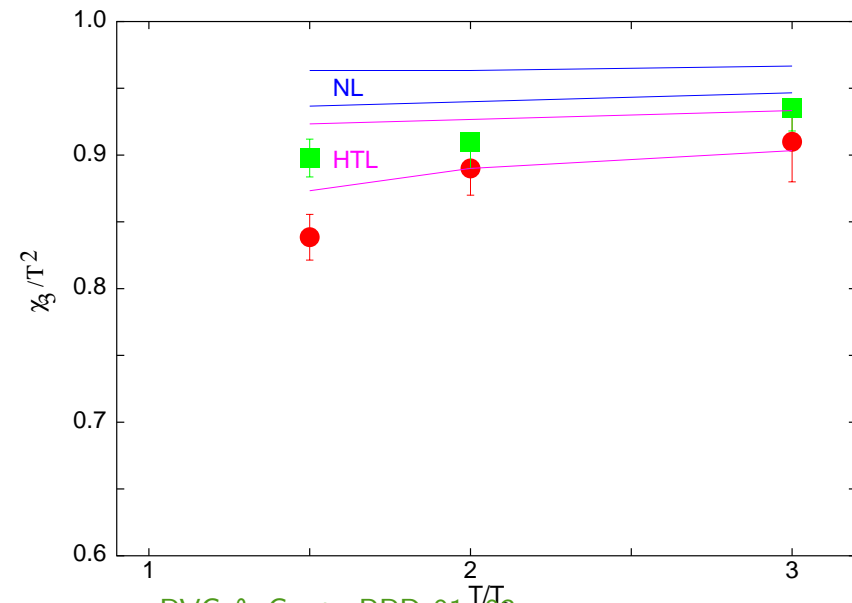


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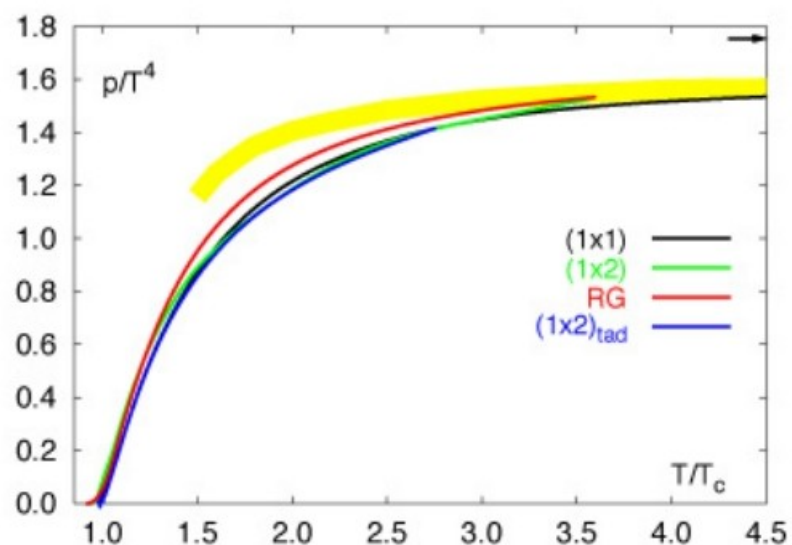
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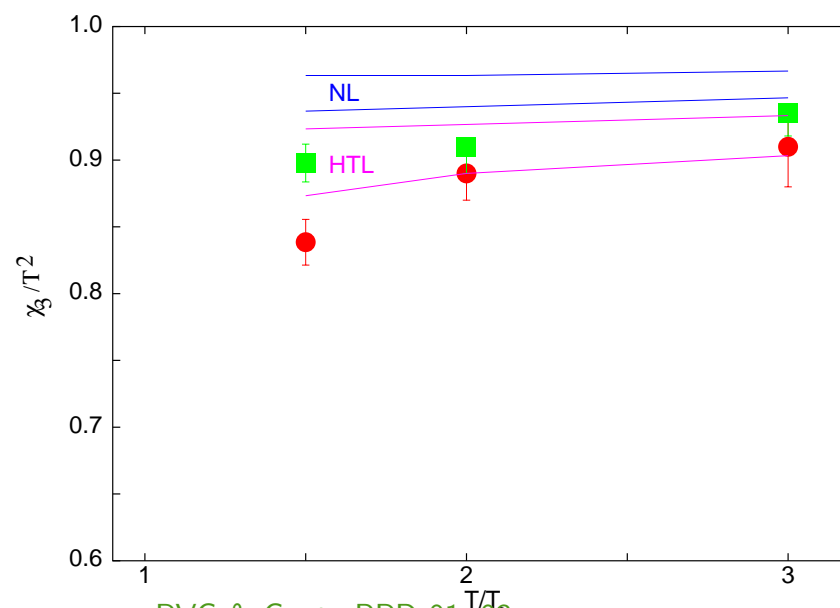
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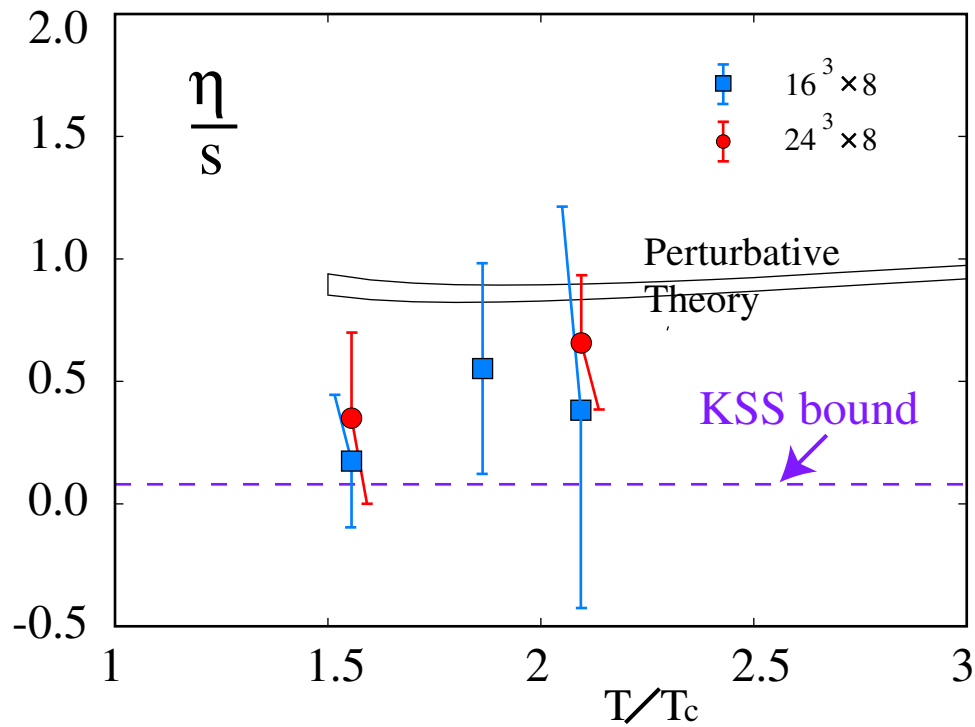
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♣ So does dimensional reduction (Kajantie et al, Vourinen)

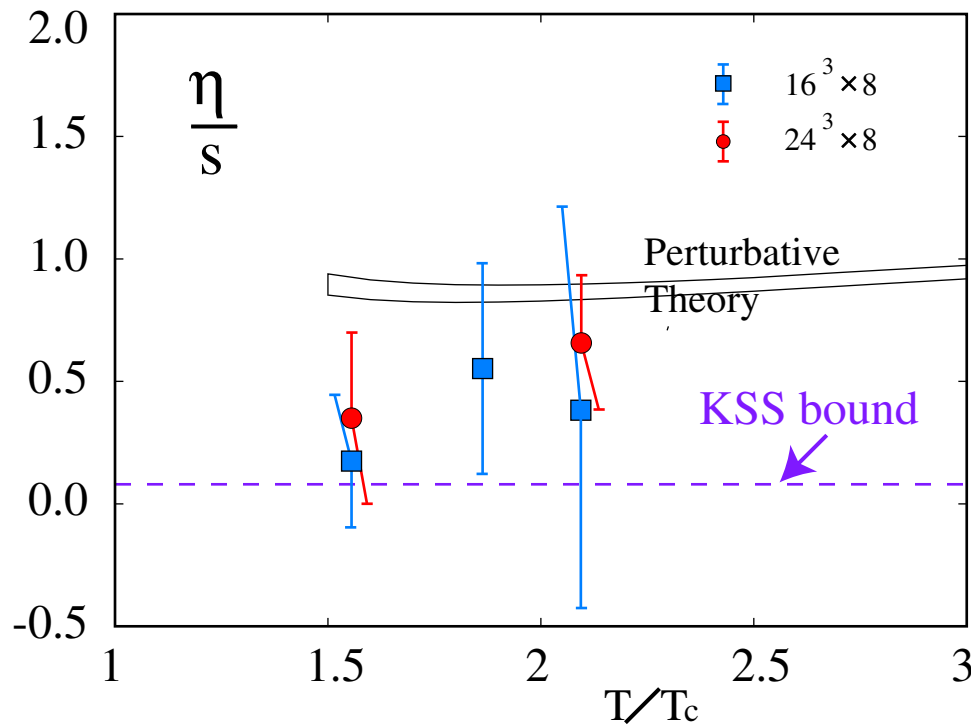
♣ Quasiparticle, PNJL models (Kampfer et al., Wiese et al.).

# Shear Viscosity



Nakamura and Sakai, PRL 94 (2005).

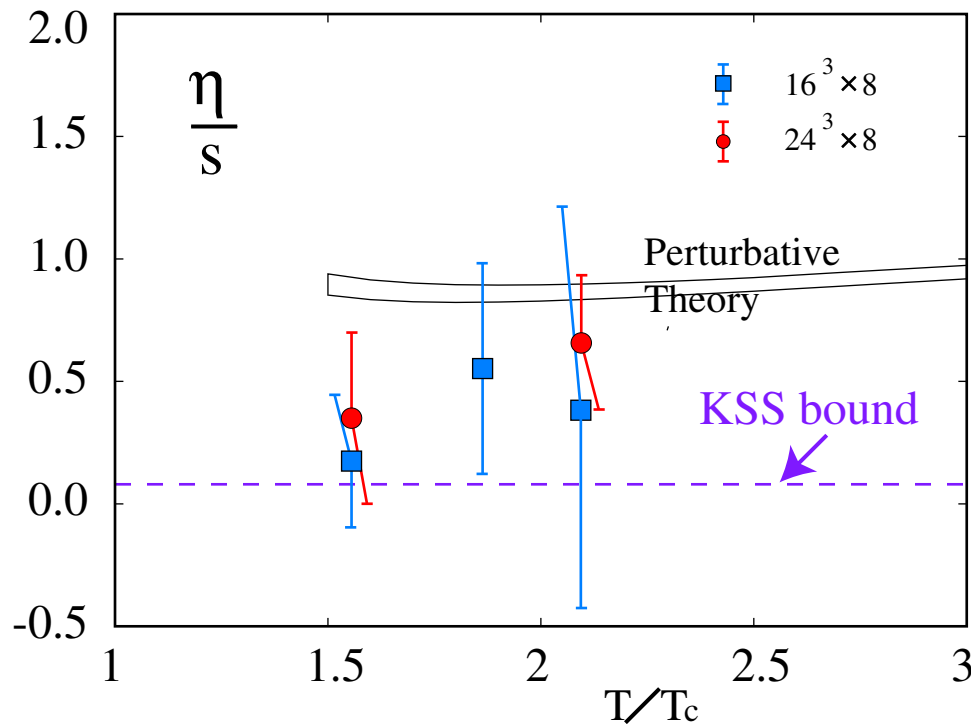
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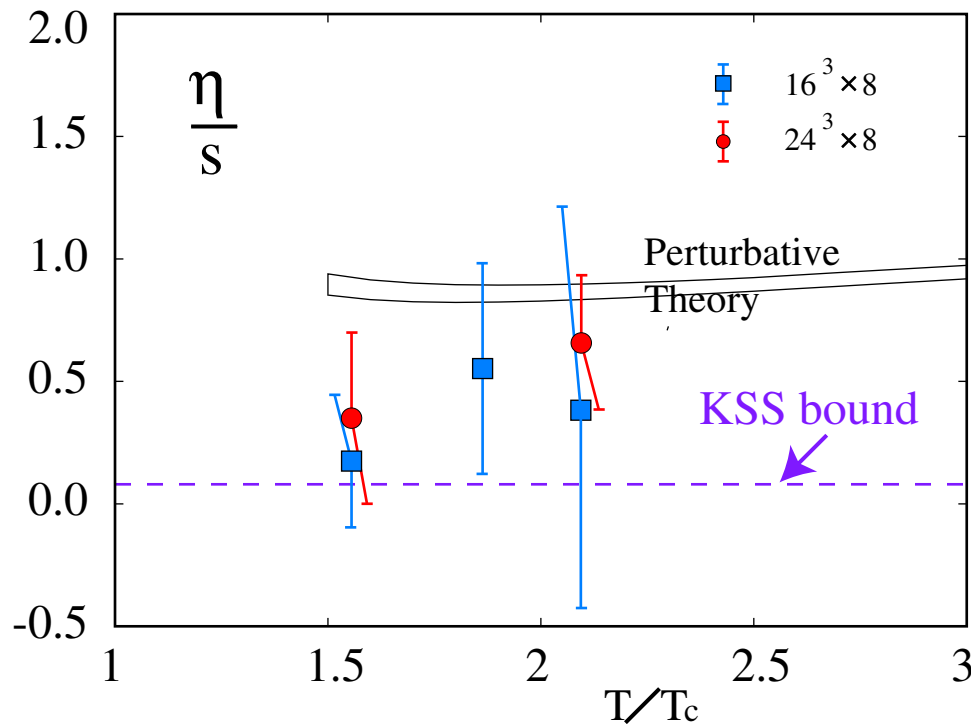
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- \* Continue them to get Retarded ones  $\rightsquigarrow$  Shear, Bulk Viscosities.
- \* Larger lattices and inclusion of dynamical quarks in future.



# Baryon-Strangeness Correlation

- ♣ Correlation between quantum numbers  $K$  and  $L$  can be studied through the ratio  $C_{(KL)/L} = \frac{\langle KL \rangle - \langle K \rangle \langle L \rangle}{\langle L^2 \rangle - \langle L \rangle^2}$ .
- ♣ These are robust : theoretically & experimentally.

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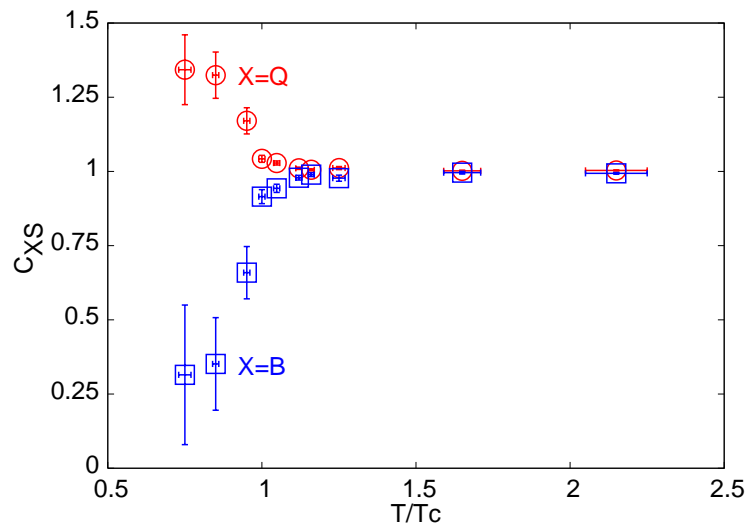
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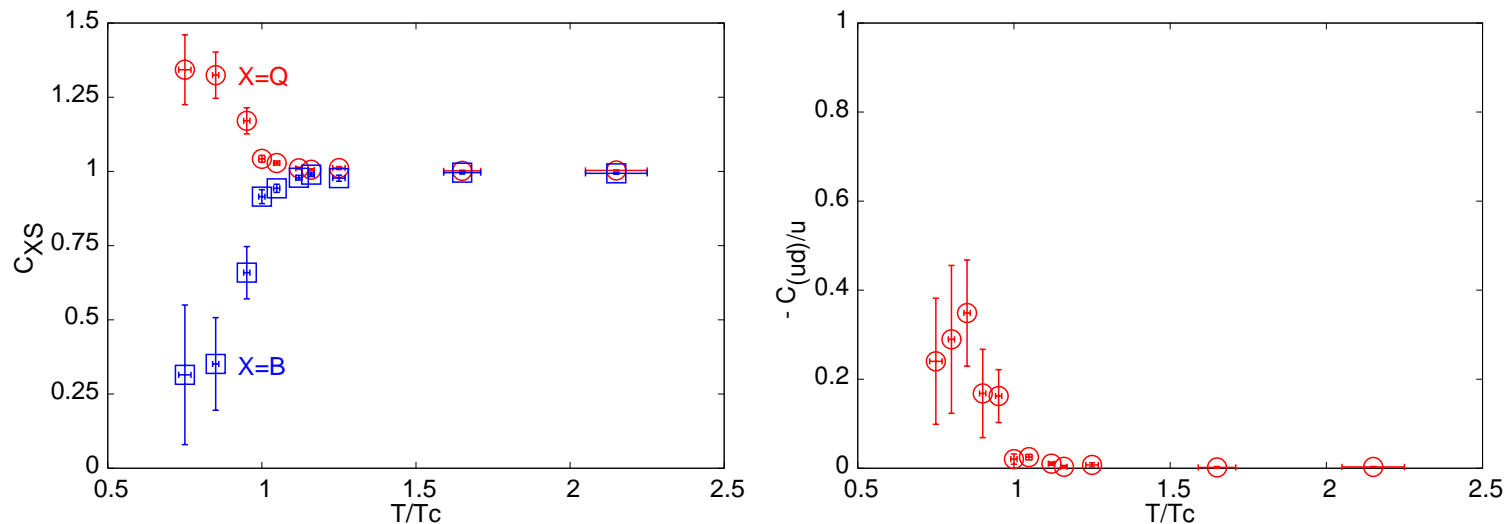


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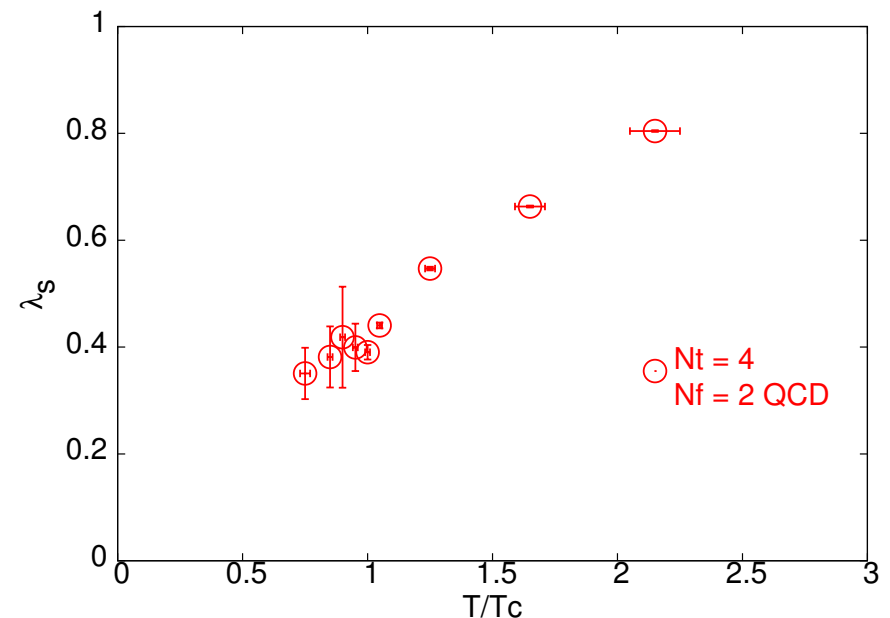
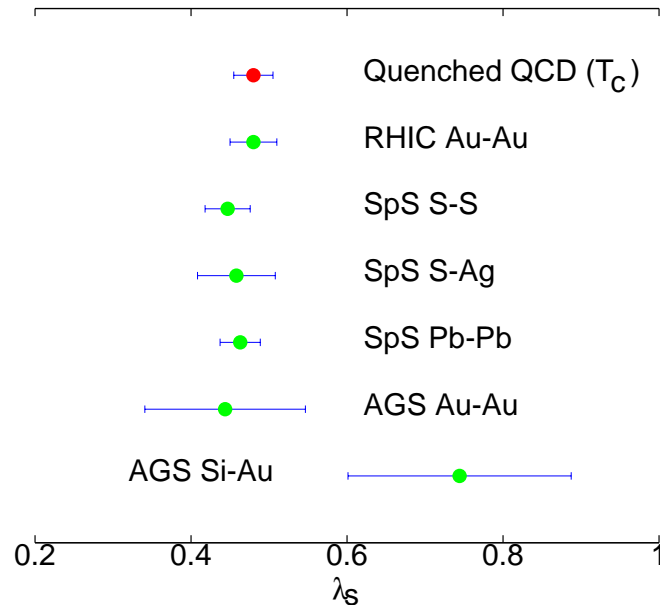
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Gavai and Gupta, Phys Rev D65, 2002 and Phys.Rev. D73, 2006.

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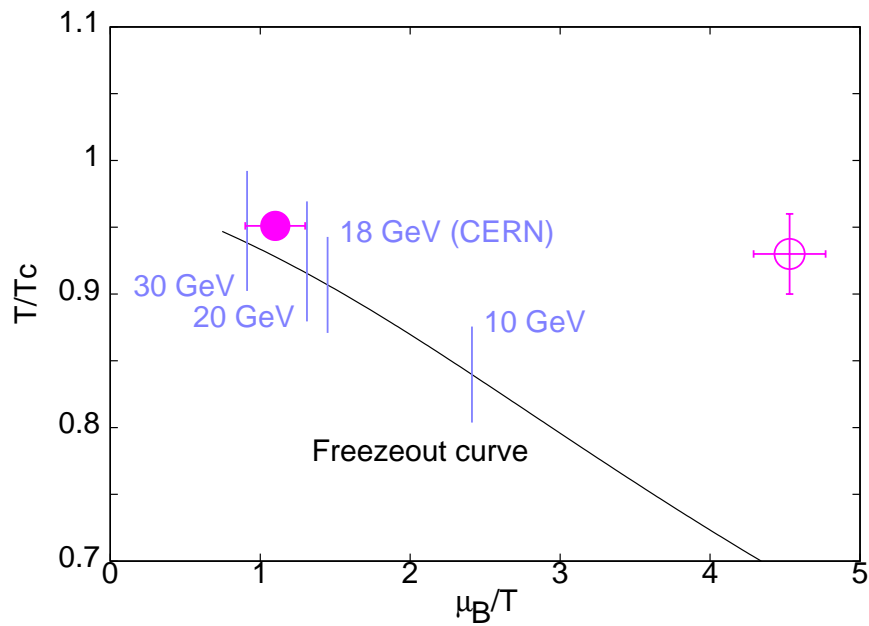
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# Our Workhorse



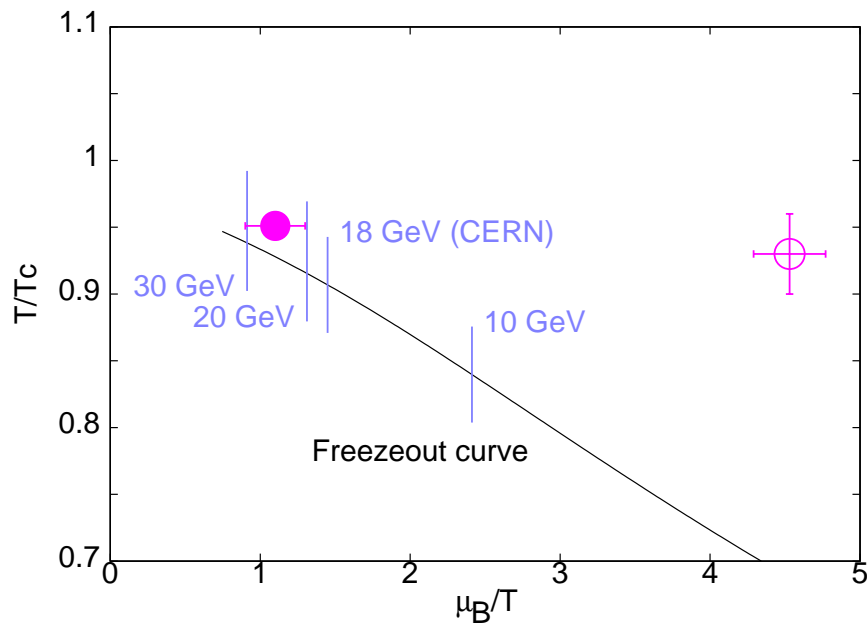
CRAY X1 of I L G T I , T I F R, Mumbai

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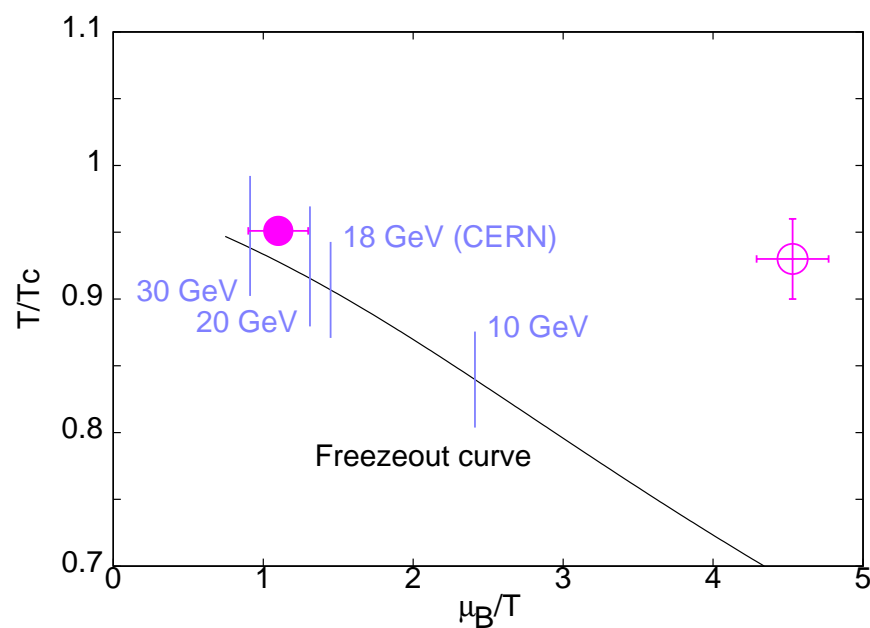


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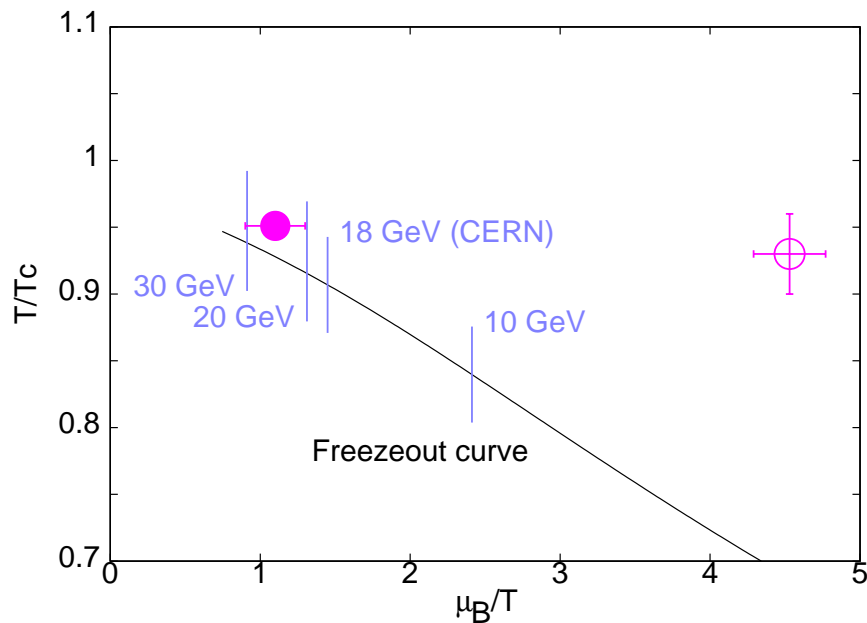


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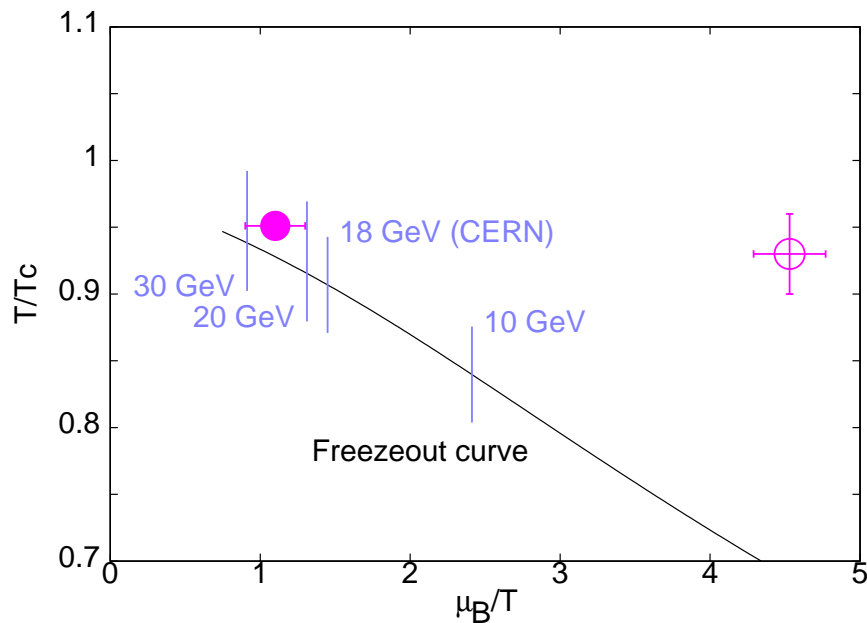
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- RHIC, if run at lower energy, can potentially discover it.



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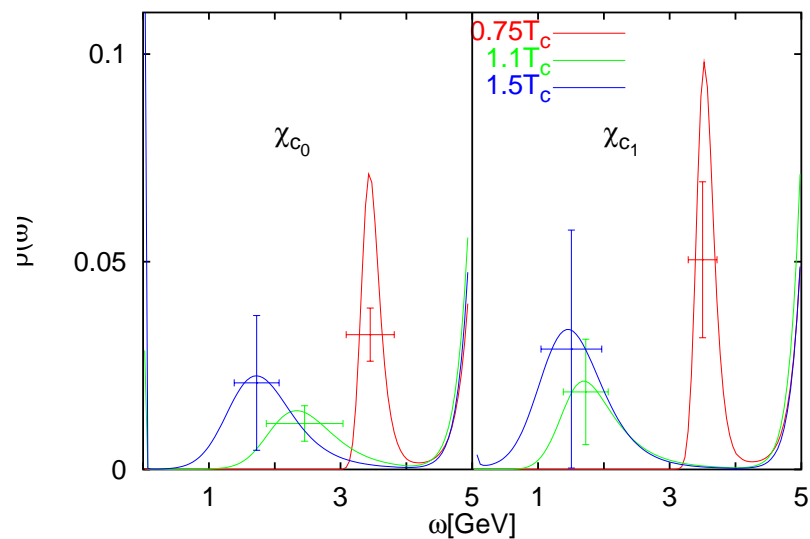
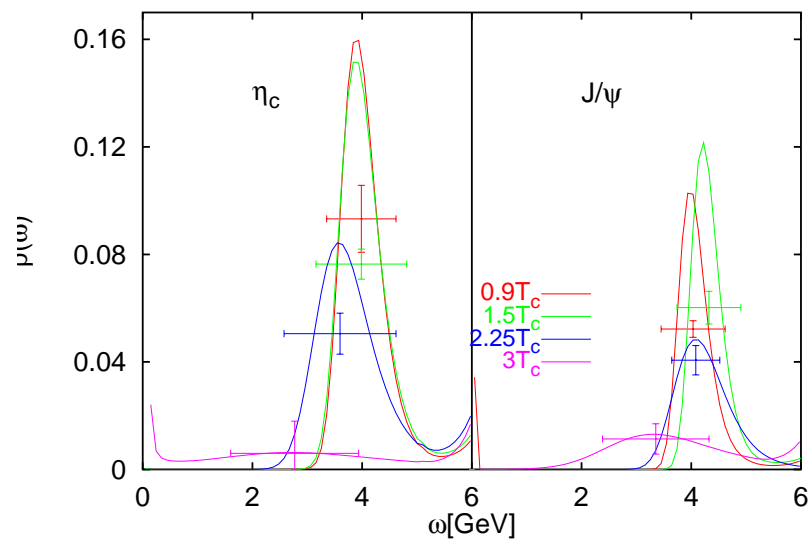
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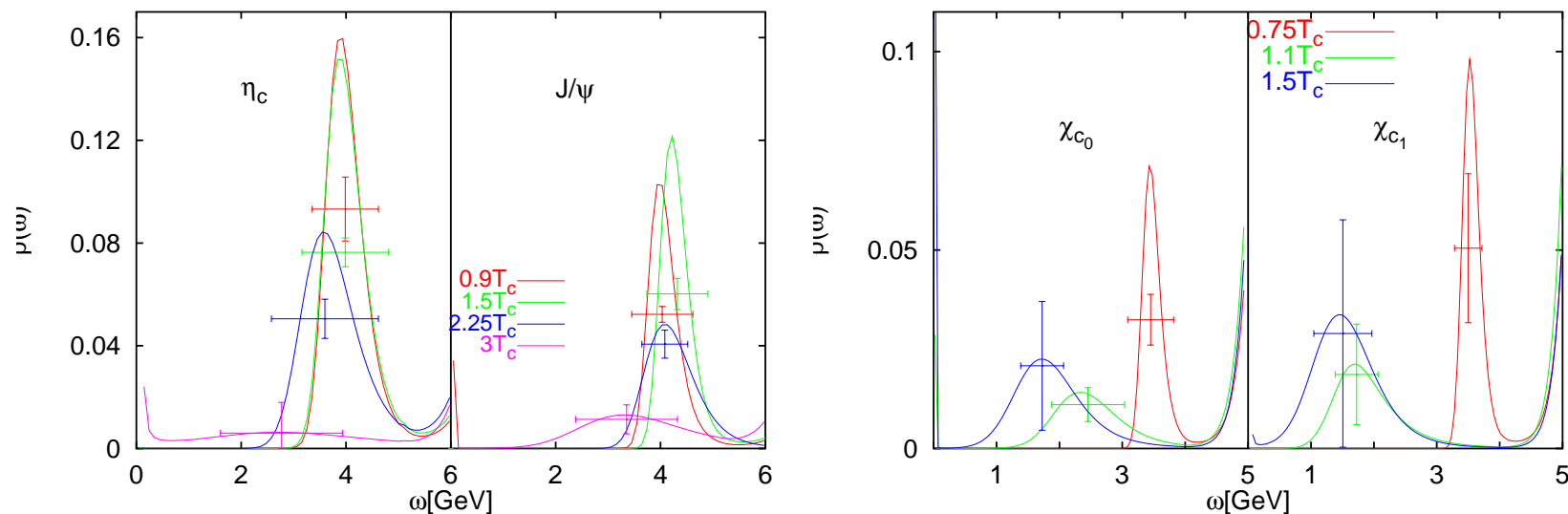
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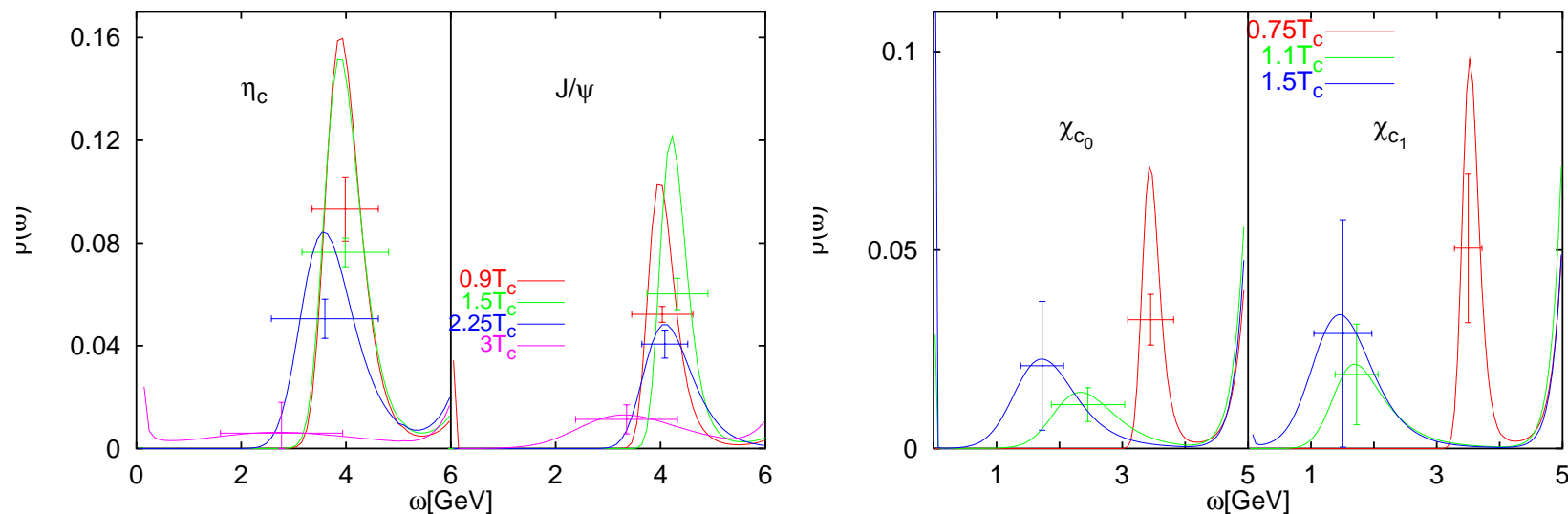


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♠ Effect of inclusion of dynamical fermions ?

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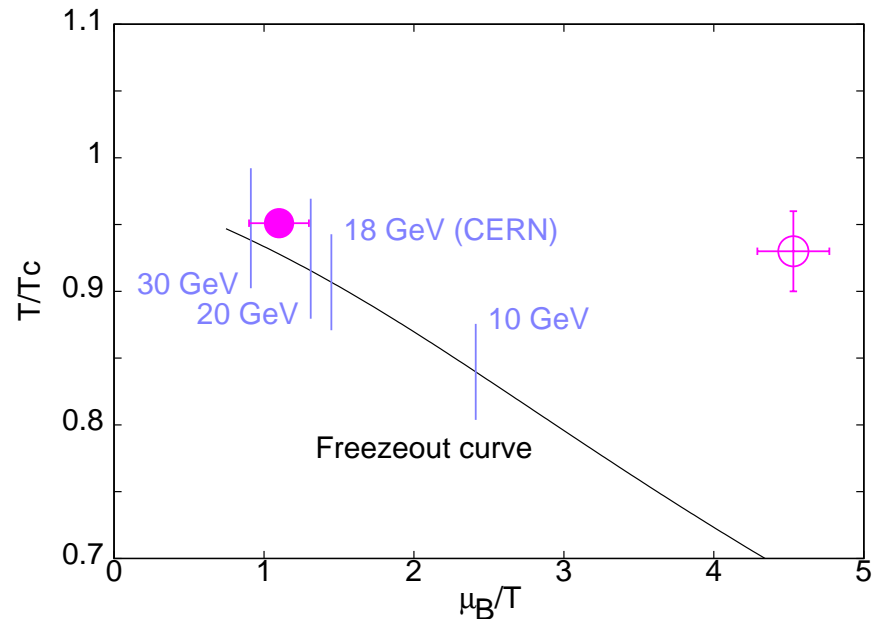


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♠ Phase diagram in  $T - \mu_B$  plane has begun to emerge: Our estimate for the critical point is  $\mu_B/T \sim 1 - 2$ .