

# Highlights of Research 2000-06

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Critical Point of QCD

Strangeness & Quasiquarks

EoS, Specific Heat..

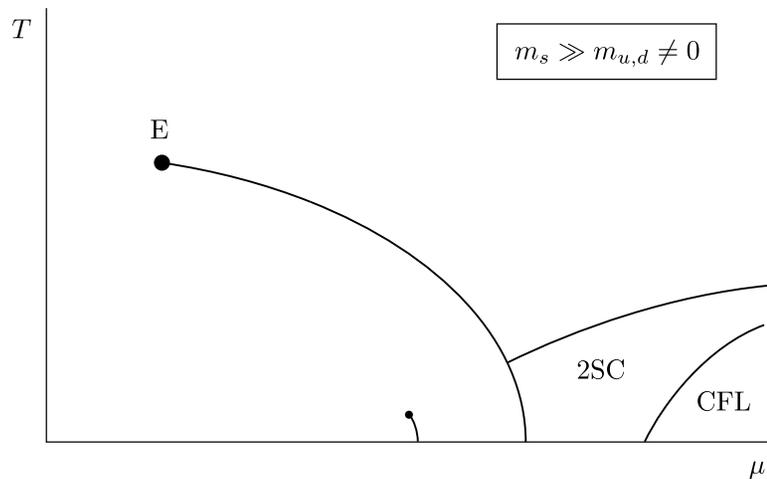
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♠ A Fundamental Aspect of  $T-\mu_B$  Phase Diagram – Critical Point

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## Expected QCD Phase Diagram

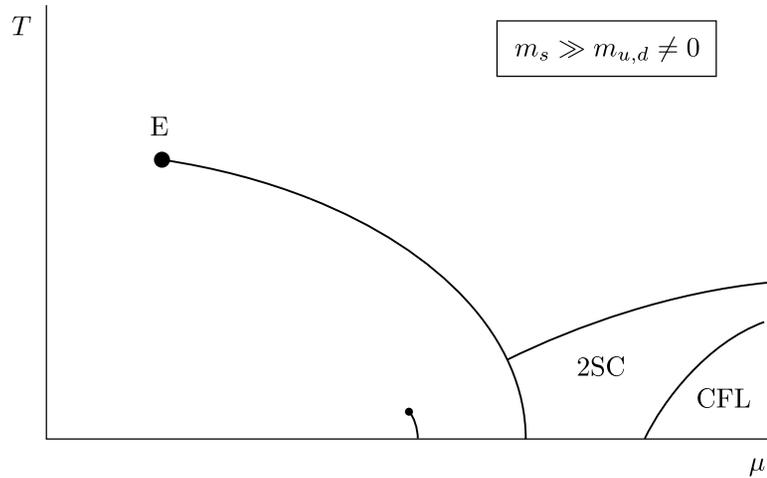


K. Rajagopal and F. Wilczek (2000)

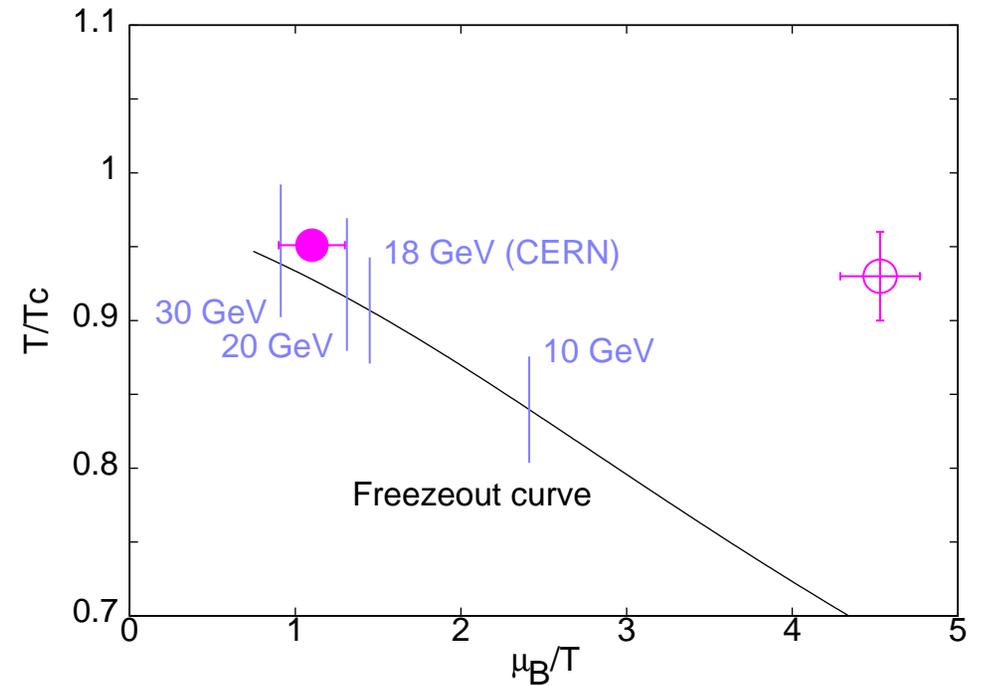
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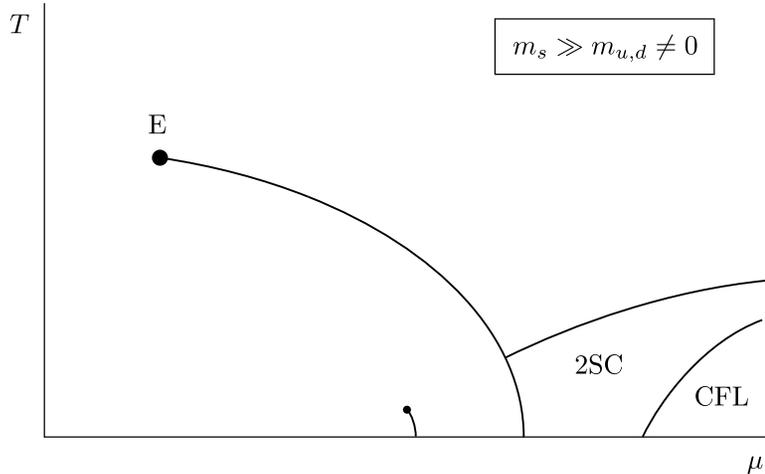


R.V. Gavai and S. Gupta, PR D71 (2005) 114014

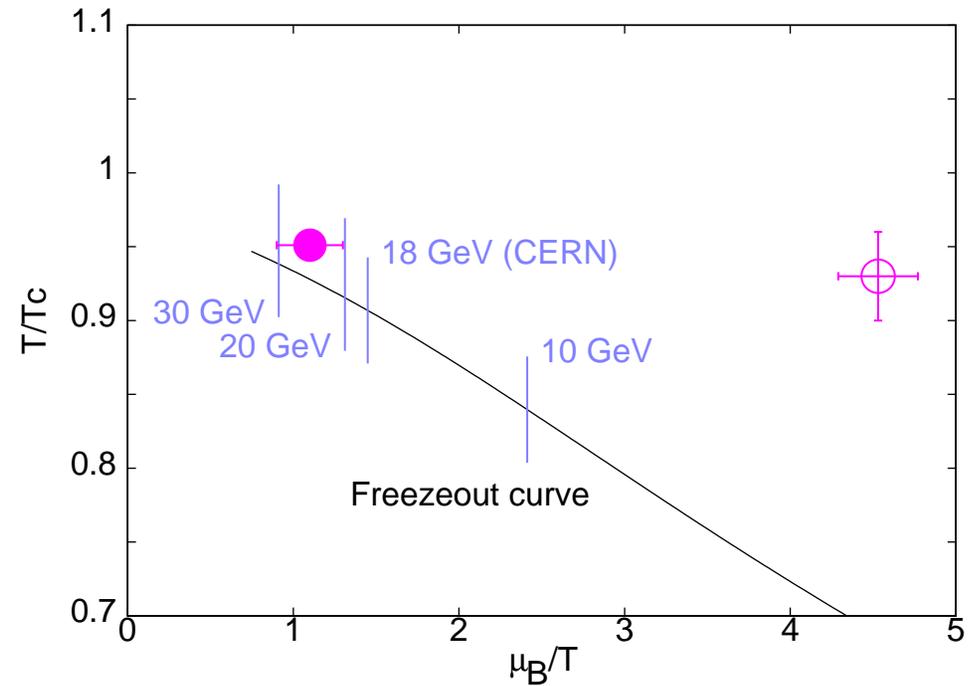
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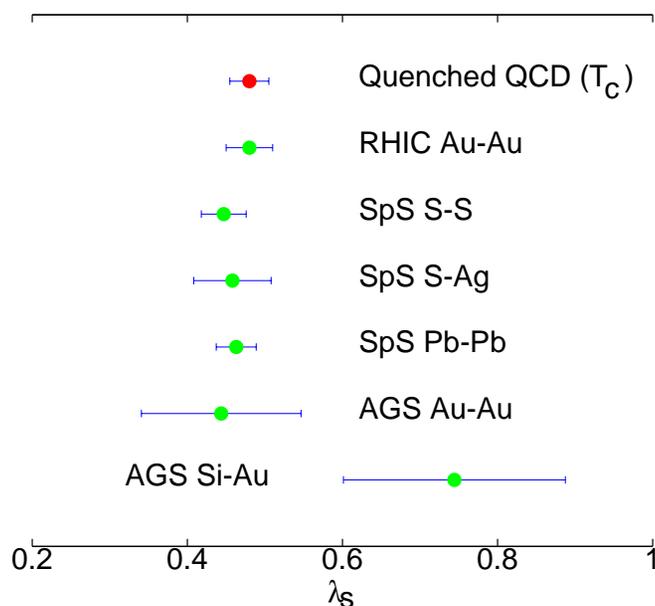
♣ Proposed *new* method, using Taylor Expansion (R.V. Gavai and S. Gupta, PR D68 (2003) 034506) and used it up to 8th order to get results.

# Strangeness & Quasiquarks

♠ Showed that Quark Number Susceptibilities,  $\chi_{ij} \sim \partial \ln Z / \partial \mu_i \partial \mu_j$ , can provide an estimate of “Wróblewski Parameter”, a measure of strangeness produced in Heavy Ion Collisions. (RVG & Sourendu Gupta, PRD 2002, PRD 2003 and PRD 2006)

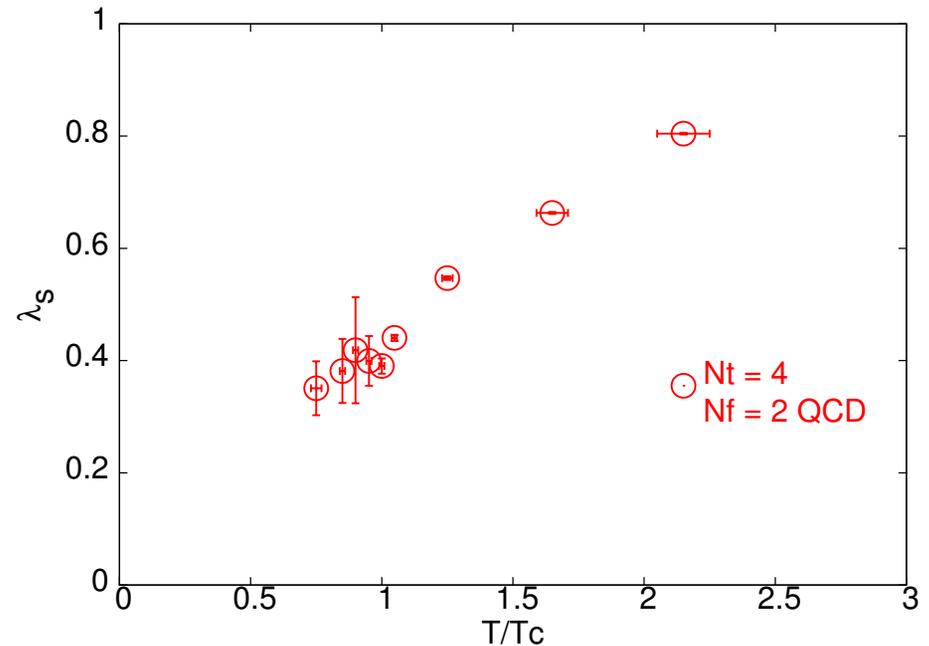
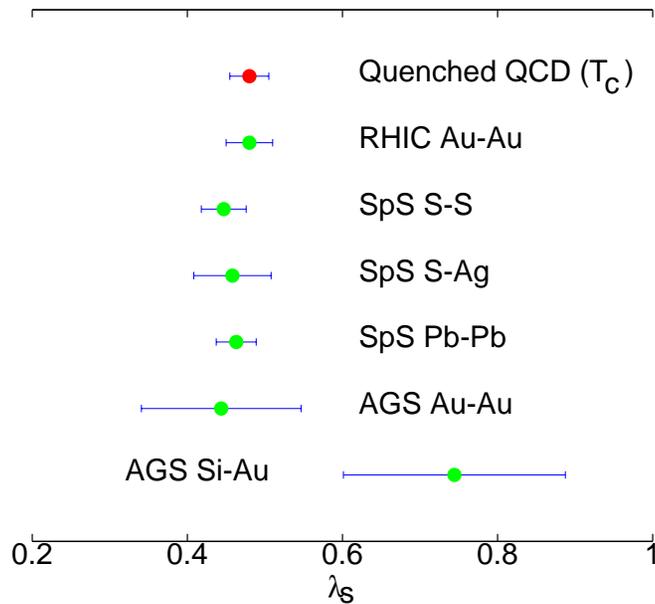
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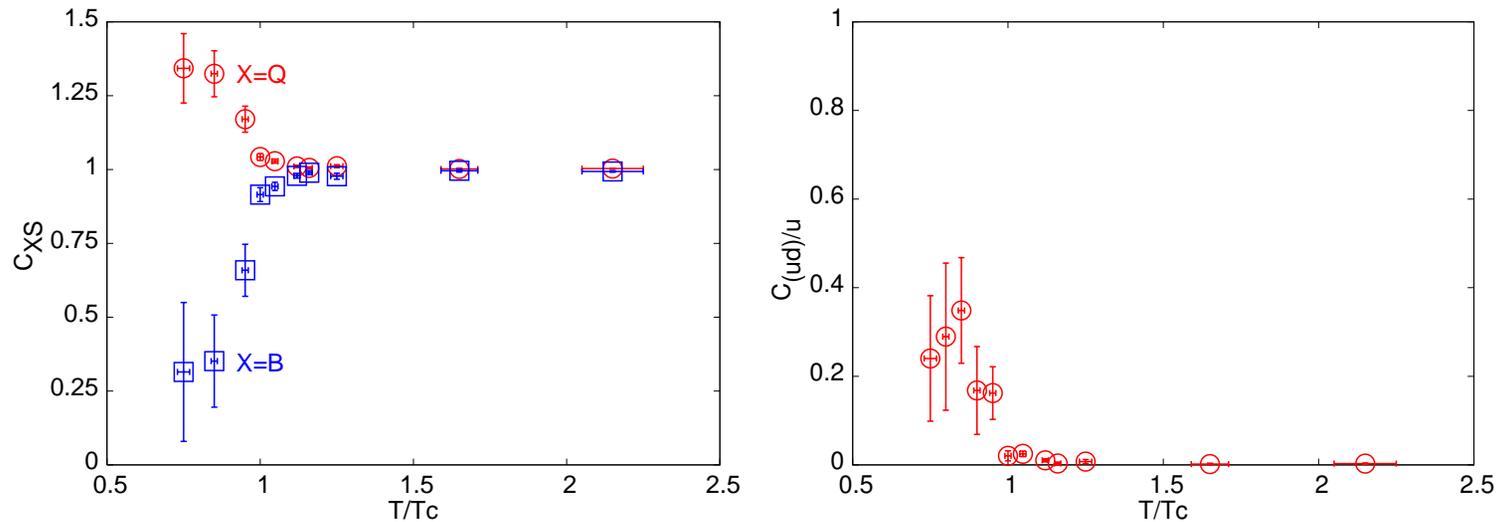


# Baryon-Strangeness Correlation

♣ Correlation between quantum numbers  $K$  and  $L$  can be studied through the ratio  $C_{(KL)/L} = \frac{\langle KL \rangle - \langle K \rangle \langle L \rangle}{\langle L^2 \rangle - \langle L \rangle^2}$ , i.e. ratios of QNS : Shown Theoretically Robust

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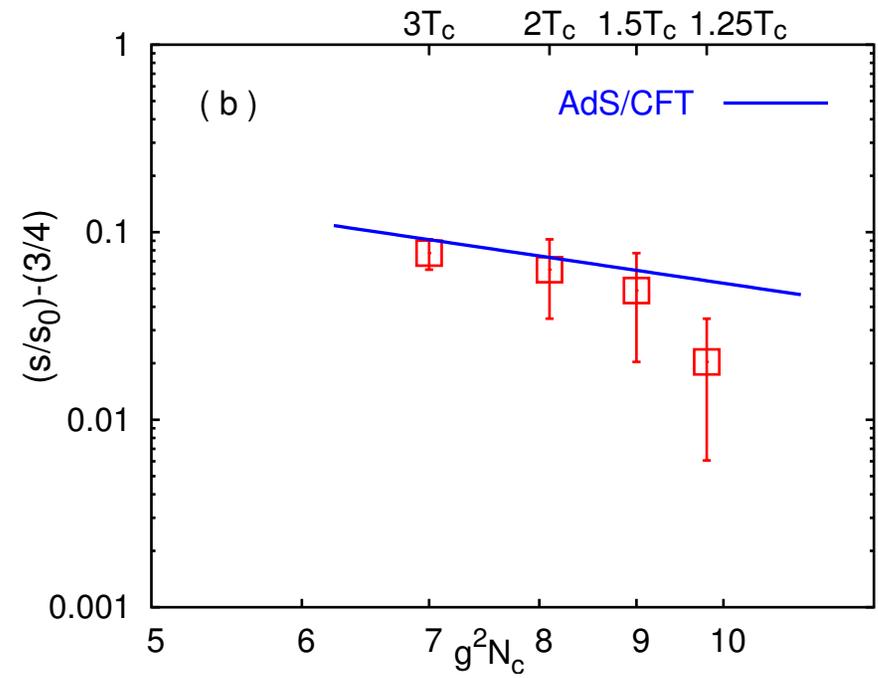
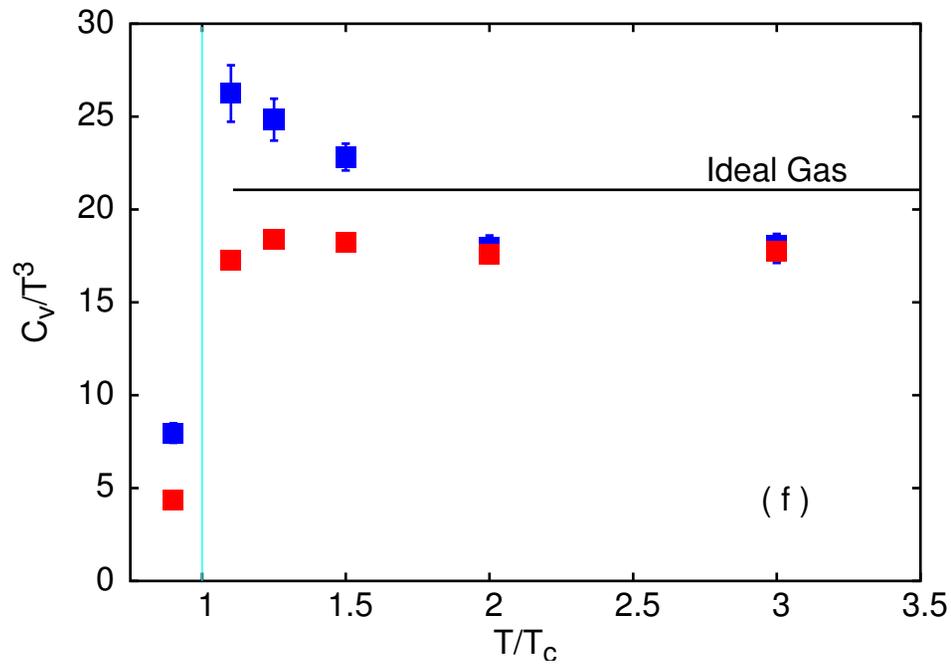
♣ Baryon Number(Charge)–Strangeness correlation suggest strangeness -1 carried by objects with baryon number 1/3 and charge -1/3. Similarly for  $u$  and  $d$  quarks.  
 $\implies$  quasiquarks. (RVG & Sourendu Gupta, PR D 2006).

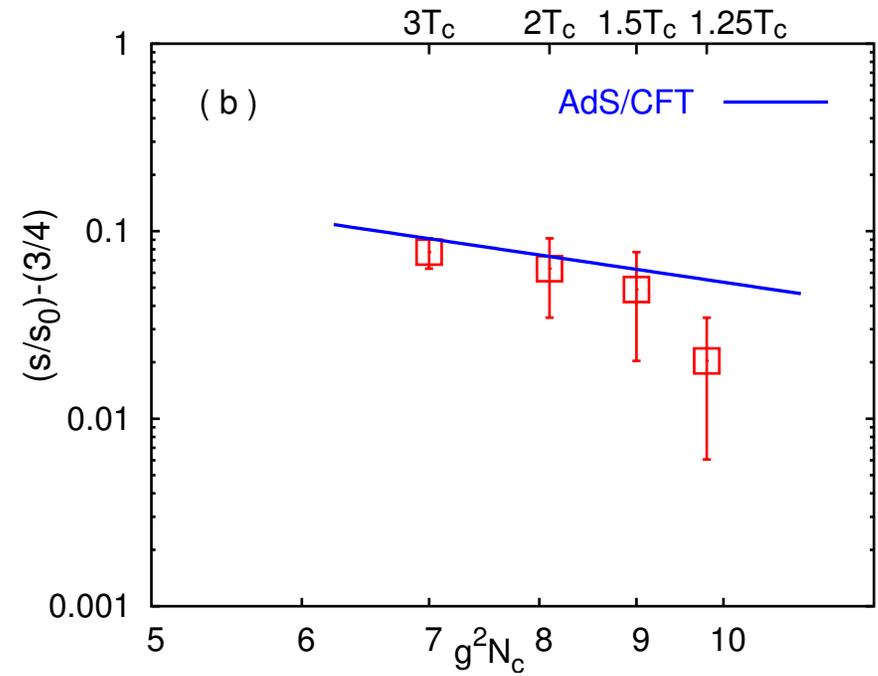
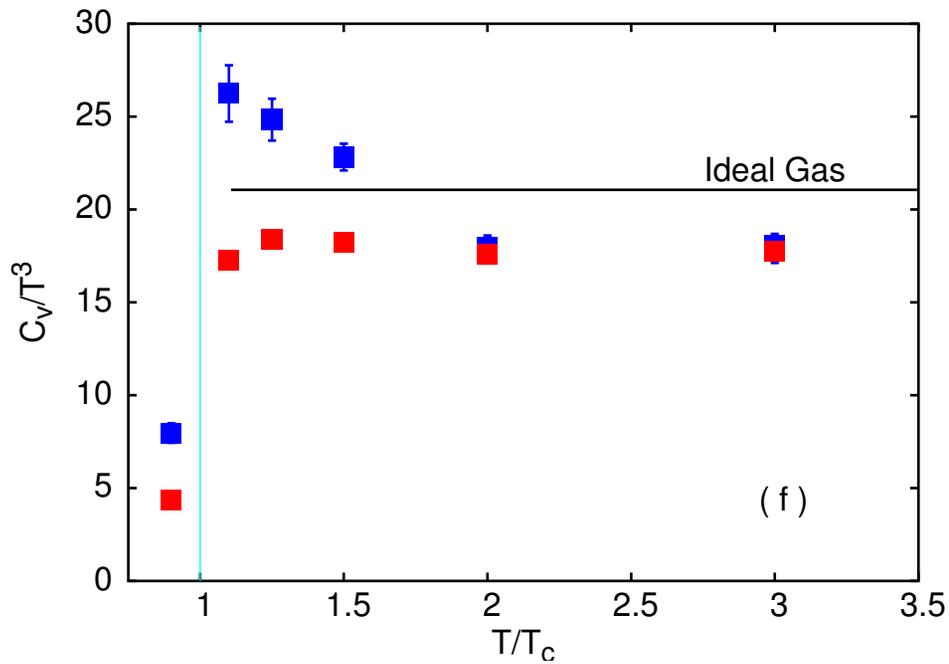
# QGP in Bulk : EoS, Speed of Sound...

- $C_s$  – Crucial for elliptic flow, hydrodynamical studies ...
- $C_v$  – Event-by-event temperature/ $p_T$  fluctuations.

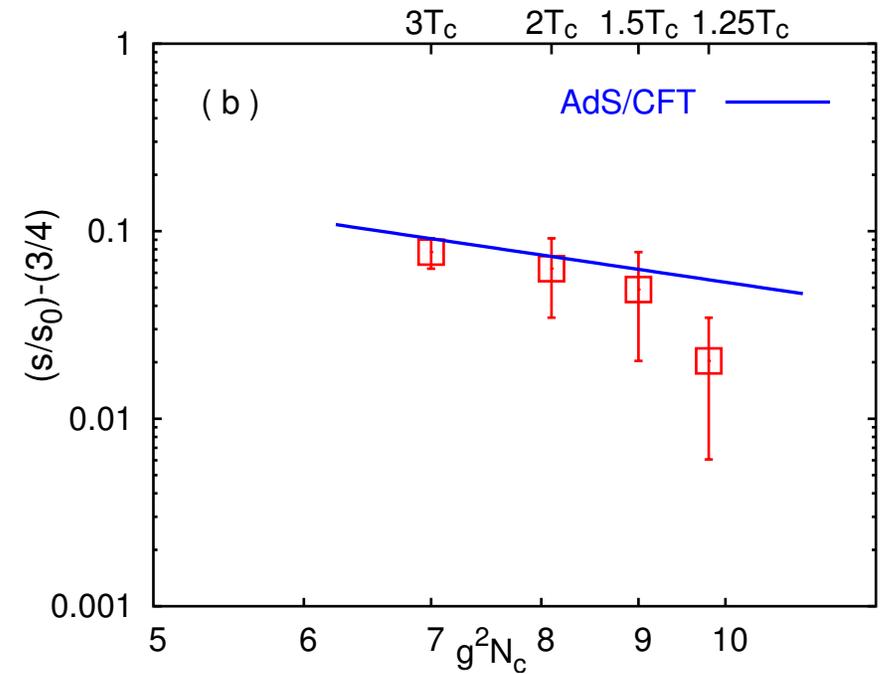
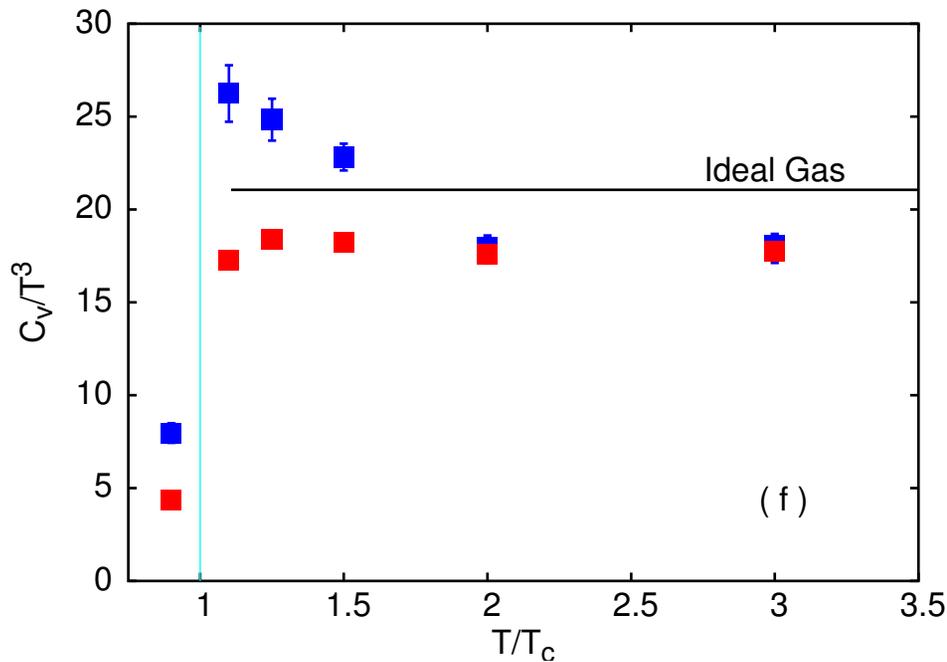
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- $C_s$  – Crucial for elliptic flow, hydrodynamical studies ...
- $C_v$  – Event-by-event temperature/ $p_T$  fluctuations.
- Obtained these by relating them to the temperature derivative of anomaly measure  $\Delta/\epsilon$  and showed them to have correct high  $T$  limit.  
(RVG, S. Gupta and S. Mukherjee, PR D71 (2005) )
- New method to obtain these & EoS differentially without getting negative pressure. Introduced an improved operator than used in earlier Bielefeld studies.  
(RVG, S. Gupta and S. Mukherjee, hep-lat/0506015)





♠ Specific heat  $\iff$  fluctuations in  $p_T$ . Possible to extract from RHIC data?



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- Entropy agrees with strong coupling SYM prediction (Gubser, Klebanov & Tseytlin, NPB '98, 202) for  $T = 1.5 - 3T_c$  but fails at lower  $T$ , as do various weak coupling schemes:  $\frac{s}{s_0} = f(g^2 N_c)$ , where  $f(x) = \frac{3}{4} + \frac{45}{32}\zeta(3)x^{-3/2} + \dots$  and  $s_0 = \frac{2}{3}\pi^2 N_c^2 T^3$ .

- Screening Correlators & Overlap fermions

↪ Sourendu's talk.

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- Deconfinement in  $SU(4)$  Gauge Theory: Showed Latent Heat  $\uparrow$ , as  $N_c \uparrow$ .  
 $\implies$  Conjecture (Pisarski & Tytgat) explaining why  $\epsilon \uparrow$  by  $\mathcal{O}(N_c^2)$   
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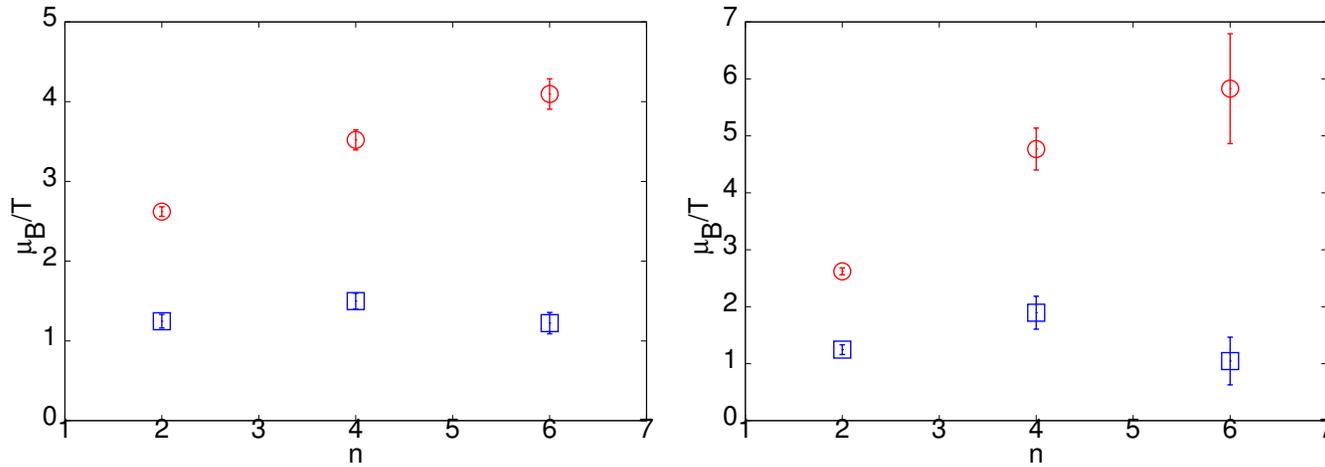
⇒ Conjecture (Pisarski & Tytgat) explaining why  $\epsilon \uparrow$  by  $\mathcal{O}(N_c^2)$   
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- Future Plans :

- Continuum limit & Realistic Pion Mass.
- Better Algorithms
- LHC Physics :  $\Upsilon$  family

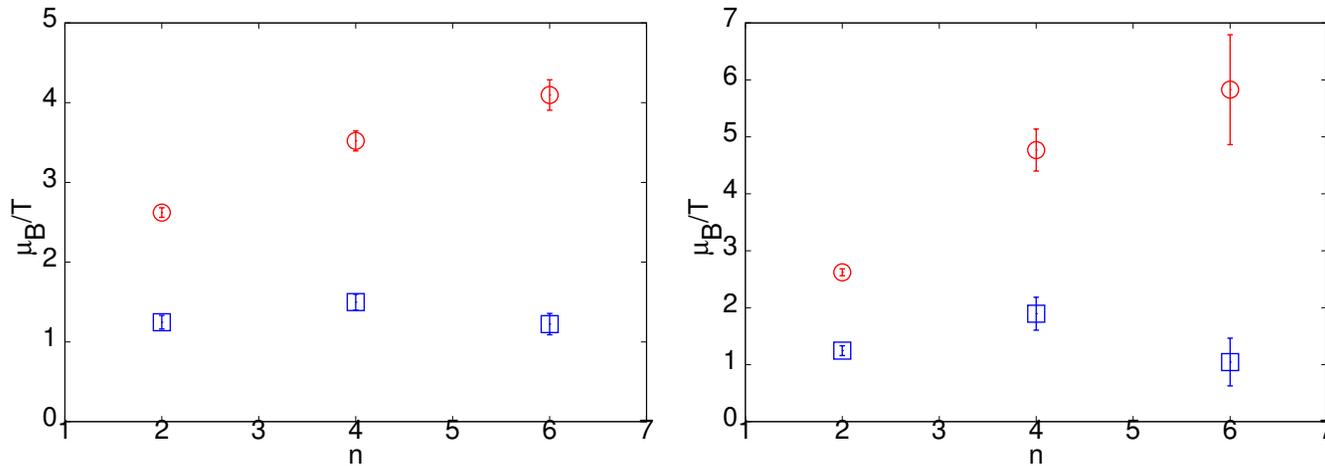
# Back-Up : Critical Point Estimate

RVG & S. Gupta, PR D 71 2005.



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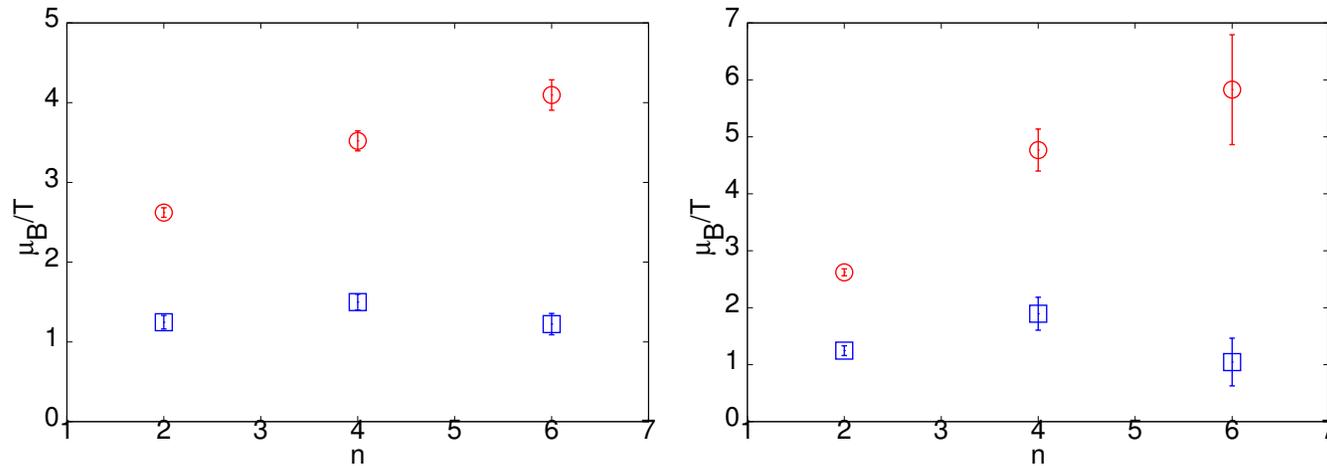
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♠ Radii of convergence as a function of the order of expansion at  $T = 0.95T_c$  on  $N_s = 8$  (circles) and 24 (boxes). Left panel for  $\rho_n$  and right one for  $r_n$ .

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♠ Extrapolation in  $n \rightsquigarrow \mu^E/T^E = 1.1 \pm 0.2$  at  $T^E = 0.95T_c$ . Finite volume shift consistent with Ising Universality class.

$m_\rho/T_c$	$m_\pi/m_\rho$	$m_N/m_\rho$	$N_s m_\pi$	flavours	$T^E/T_c$	$\mu_B^E/T^E$
5.372 (5)	0.185 (2)	—	1.9–3.0	2+1	0.99 (2)	2.2 (2)
5.12 (8)	0.307 (6)	—	3.1–3.9	2+1	0.93 (3)	4.5 (2)
5.4 (2)	0.31 (1)	1.8 (2)	3.3–10.0	2	0.95 (2)	1.1 (2)
5.4 (2)	0.31 (1)	1.8 (2)	3.3	2	—	—
5.5 (1)	0.70 (1)	—	15.4	2	—	—

Table 1: Summary of critical end point estimates—the lattice spacing is  $a = 1/4T$ .  $N_s$  is the spatial size of the lattice and  $N_s m_\pi$  is the size in units of the pion Compton wavelength, evaluated for  $T = \mu = 0$ . The ratio  $m_\pi/m_K$  sets the scale of the strange quark mass.

Results are sequentially from Fodor-Katz '04, Fodor-Katz '02, Gavai-Gupta, de Forcrand- Philipsen and Bielefeld-Swansea.