

Charm production in AA collisions

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Introduction

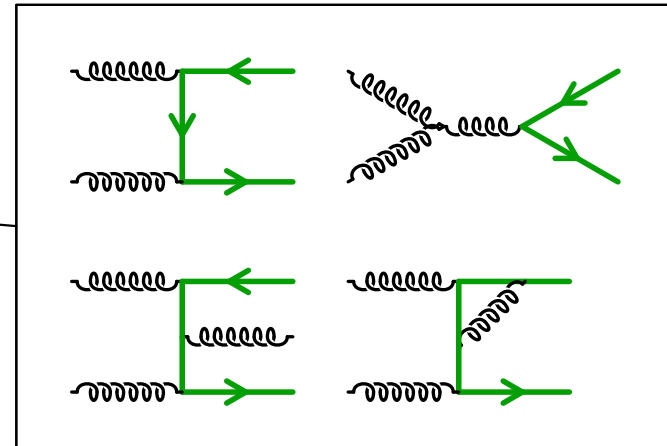
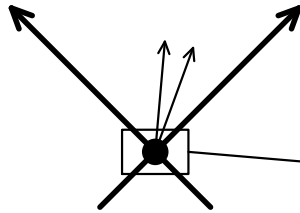
Collinear factorization

QQbar production at small x

Introduction

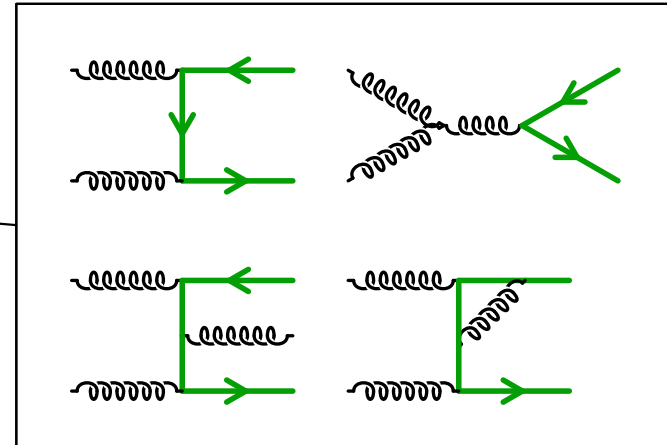
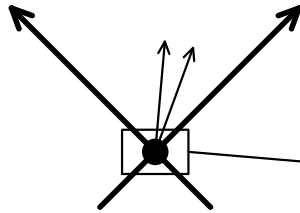
Heavy quark production

■ Standard collinear factorization

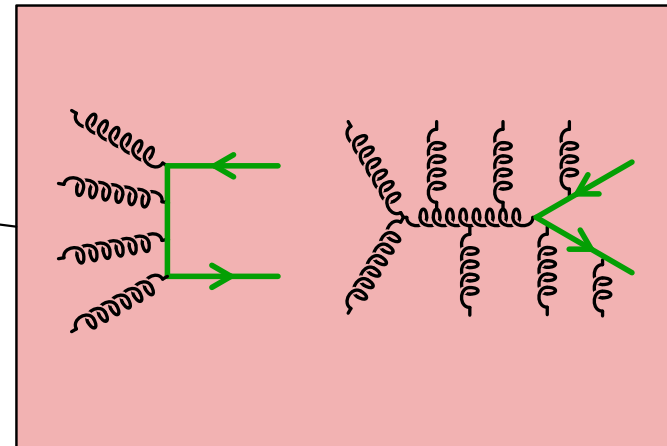
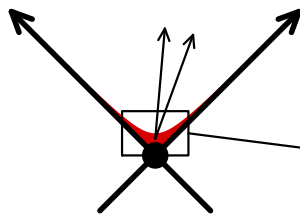


Heavy quark production

■ Standard collinear factorization



■ ...or higher twist effects ?

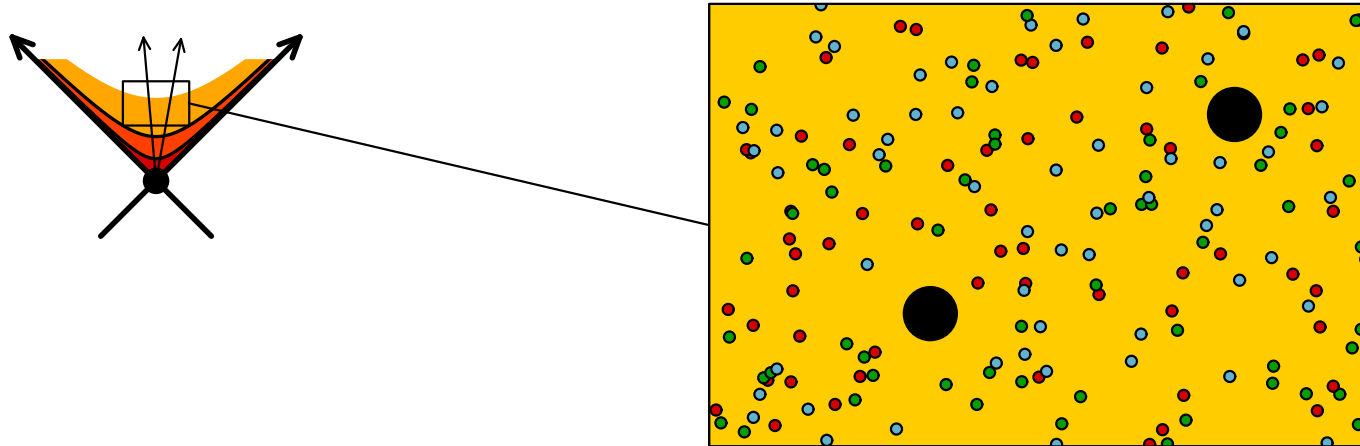


In-medium J/ψ suppression

Introduction

Collinear factorization

$Q\bar{Q}$ production at small x



- Debye screening prevents the formation of quarkonium states [Matsui, Satz \(1986\)](#)
 - ◆ the heavy quarks pick a light quark instead and form a D meson
- Heavy quark potential, screening masses, and spectral functions (?) calculable on the lattice
- Relevant observable :

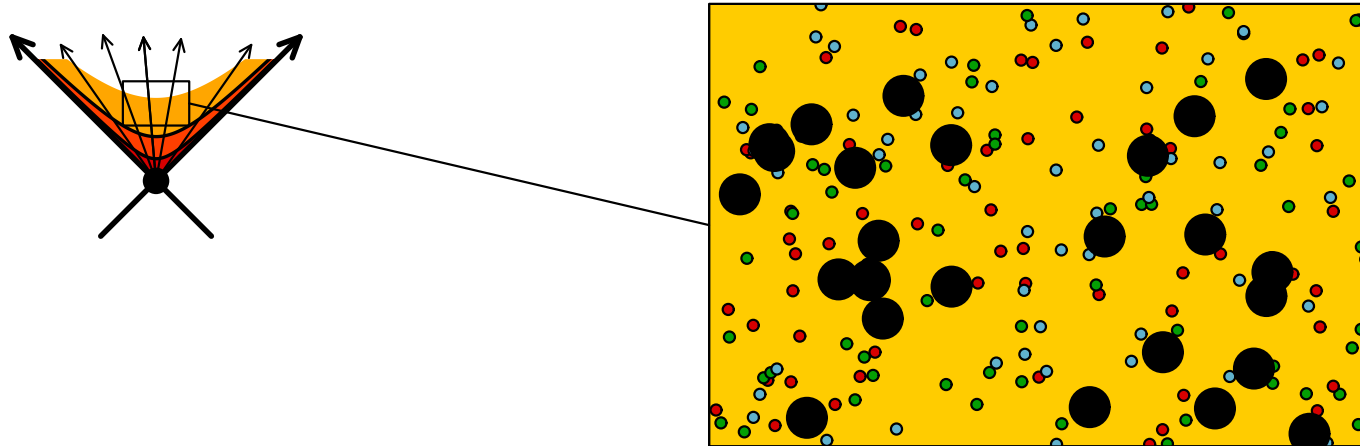
$$[J/\psi] / [\text{Open charm}]$$

...or $Q\bar{Q}$ recombination ?

Introduction

Collinear factorization

$Q\bar{Q}$ production at small x



- Many $Q\bar{Q}$ pairs are produced in each AA collision
 Braun-Munzinger, Stachel (2000)
 Thews, Schroedter, Rafelski (2001)
 - ◆ A Q from one pair can recombine with a \bar{Q} from another pair
- Avoids the conclusion of the Matsui-Satz scenario, provided that the average distance between heavy quarks is smaller than the Debye screening length
- Leads to an enhancement of J/ψ formation



Outline

Introduction

Collinear factorization

$Q\bar{Q}$ production at small x

- Collinear factorization
- $Q\bar{Q}$ production at small x



Introduction

Collinear factorization

- Fixed order
- Resummations

QQbar production at small x

Collinear factorization

Fixed order calculations

Introduction

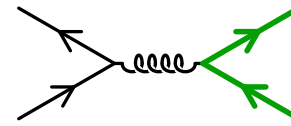
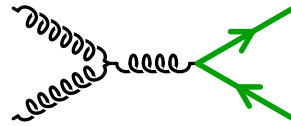
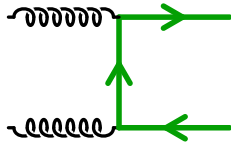
Collinear factorization

● Fixed order

● Resummations

QQbar production at small x

■ LO [$\mathcal{O}(\alpha_s^2)$]:



Fixed order calculations

Introduction

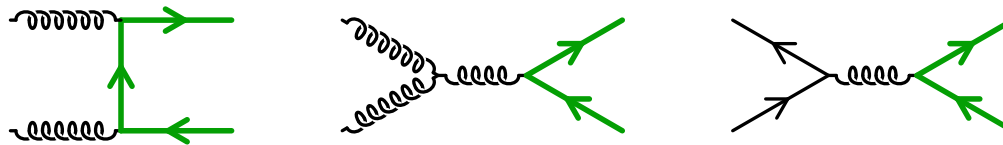
Collinear factorization

● Fixed order

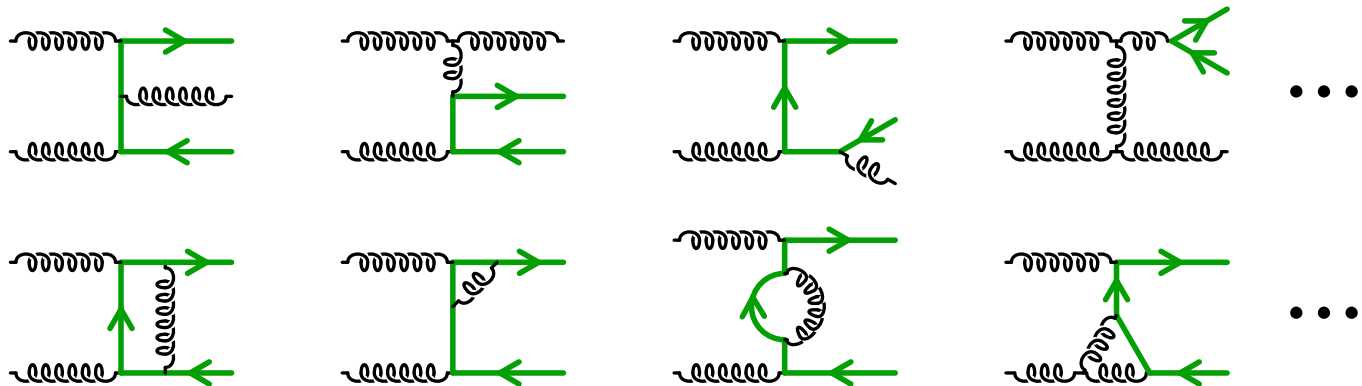
● Resummations

QQbar production at small x

■ LO [$\mathcal{O}(\alpha_s^2)$]:



■ NLO [$\mathcal{O}(\alpha_s^3)$]: Nason, Dawson, Ellis (1988)



- NLO almost as large as LO + rather large scale dependence
- NNLO not known yet for this process

Fixed order calculations

Introduction

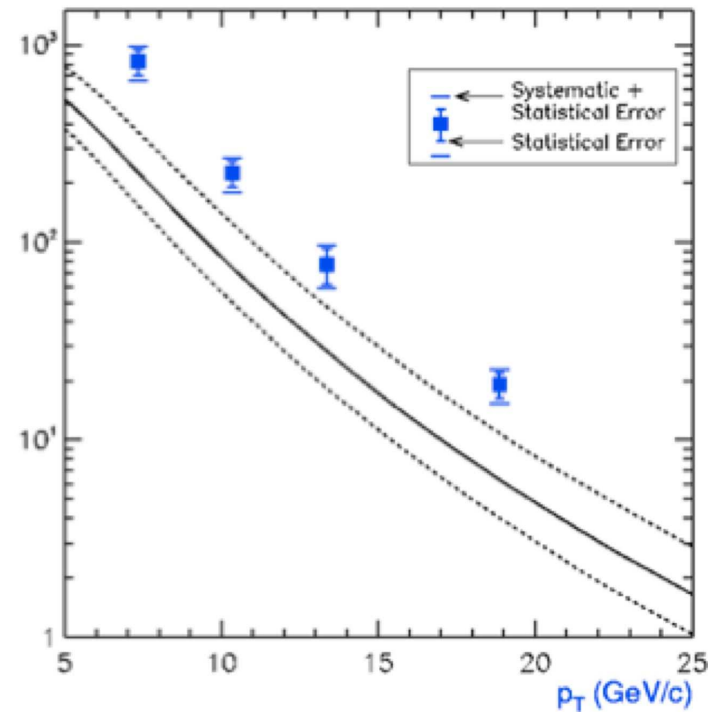
Collinear factorization

● Fixed order

● Resummations

QQbar production at small x

- Plain LO+NLO has been problematic for a long time:
B production at CDF vs NLO-pQCD, as of 2001



▷ data / theory ~ 2.9 ... somewhat embarrassing for pQCD...



Resummation of logarithms

Introduction

Collinear factorization

● Fixed order

● Resummations

QQbar production at small x

- The coefficients of the perturbative expansion may be enhanced by logarithms

$$d\sigma_{ij \rightarrow Q\bar{Q}} = \sum_{n=2}^{\infty} c_n \alpha_s^n, \quad c_n = \sum_{k=0}^{n-2} c_n^{(n-2-k)} [\ln Q]^{n-2-k}$$

where Q might be large enough so that $\alpha_s \ln Q \geq 1$

- Logs that are independent of the observable :
 - ◆ Threshold logs: $Q = \hat{s}/4m_Q^2 - 1$
 - ◆ Small- x logs: $Q = \hat{s}/m_Q^2$
- Logs that depend on the details of the observable :
 - ◆ Single Q spectrum at large momentum: $Q = p_{\perp}(Q)/m_Q$
 - ◆ $Q\bar{Q}$ spectrum at low pair momentum: $Q = m_Q/p_{\perp}(Q\bar{Q})$
 - ◆ $Q\bar{Q}$ spectrum in a back-to-back configuration: $Q = 1 - \phi_{Q\bar{Q}}/\pi$



Resummation of logarithms

Introduction

Collinear factorization

● Fixed order

● Resummations

QQbar production at small x

- Including these logarithms amounts to taking into account extra radiation in the final state
- Rearrangement of the perturbative expansion:

$$d\sigma = \alpha_s^2 \sum_{n=0}^{\infty} \alpha_s^n \sum_{i=0}^{\infty} r_i^{(n)} [\alpha_s \ln Q]^i + \mathcal{O}(Q^{-1})$$

- ◆ $n = 0$: Leading Log (LL)
- ◆ $n = 1$: Next-to-Leading Log (NLL)
- Two different implementations :
 - ◆ **FONLL** : NLO fixed order + analytic resummation of leading logs
Cacciari, Greco, Nason (1998)
 - ◆ **MC@NLO** : NLO fixed order + resummation of logs via a “parton shower”
Frixione, Webber (2002)

Present data vs theory situation

Introduction

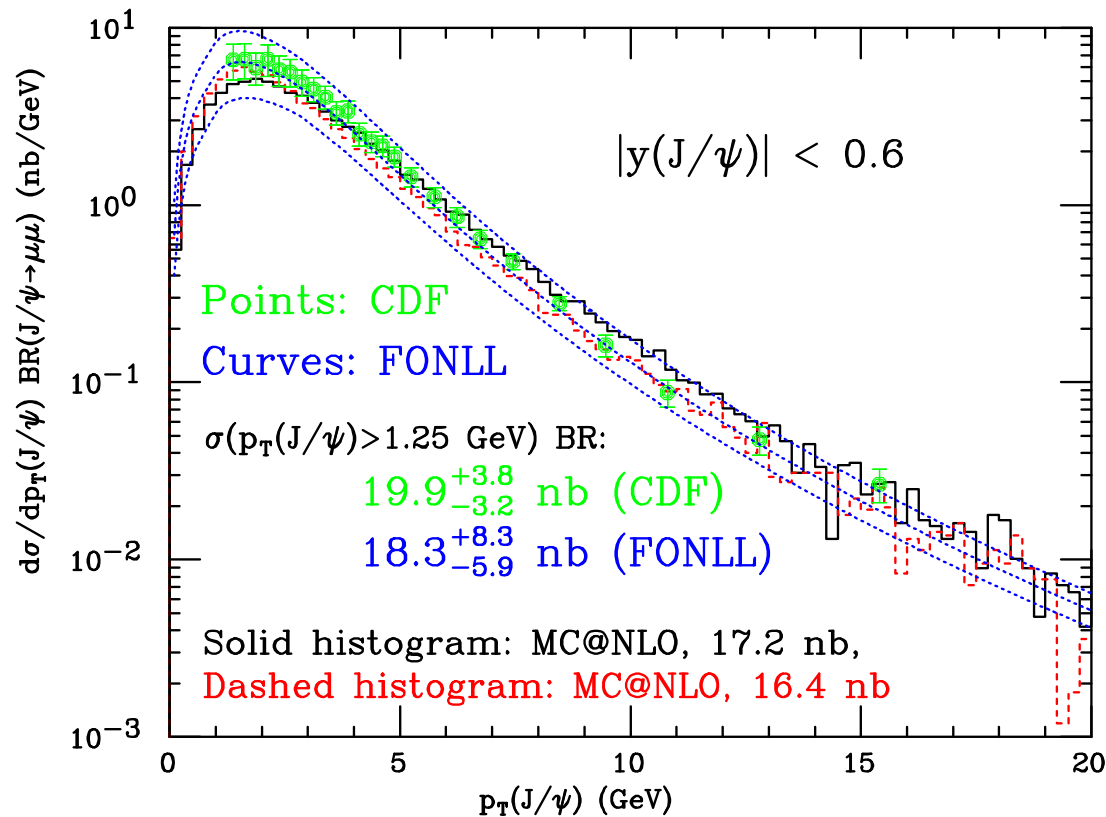
Collinear factorization

● Fixed order

● Resummations

QQbar production at small x

- Resummations + better fragmentation functions: better agreement with data : **B production at Tevatron II**



▷ **Note** : the data has gone down as well...



Introduction

Collinear factorization

QQbar production at small x

- Relevant x range
- Kt-factorization
- Color glass condensate
- High density effects for pA
- AA collisions

QQbar production at small x



Relevant x range at the LHC

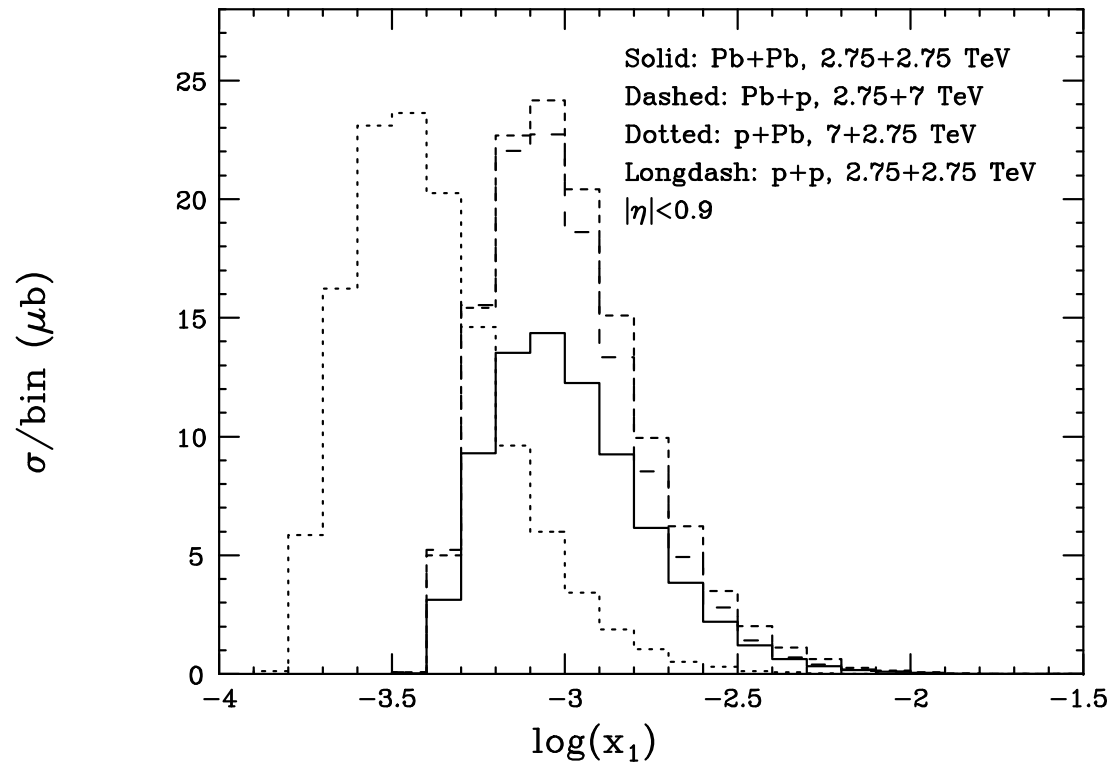
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- x coverage for $c\bar{c}$ production at the LHC : **central rapidity**



Relevant x range at the LHC

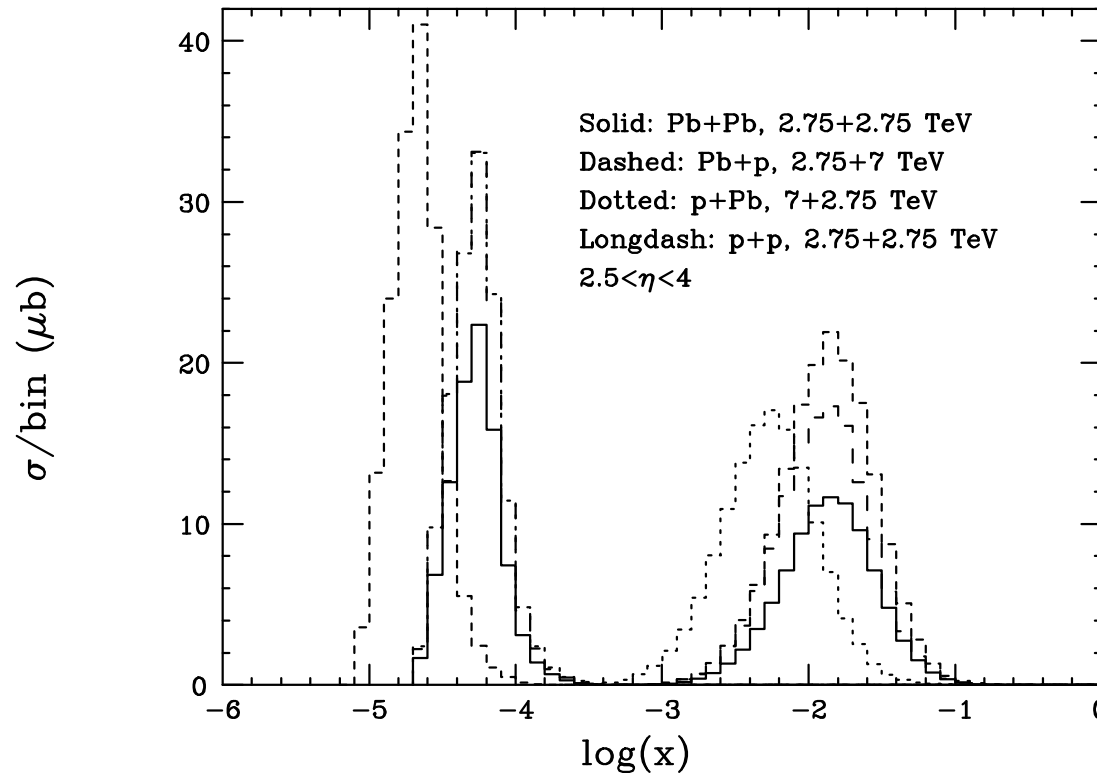
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- x coverage for $c\bar{c}$ production at the LHC : **forward rapidity**



- ▷ very small values of x reached in one of the projectiles

Kt-factorization

Introduction

Collinear factorization

QQbar production at small x

● Relevant x range

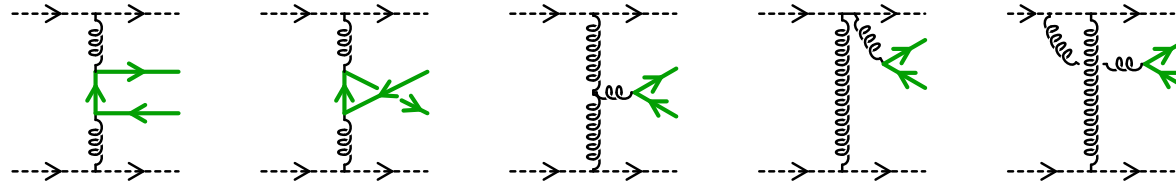
● Kt-factorization

● Color glass condensate

● High density effects for pA

● AA collisions

■ Included diagrams :



■ $Q\bar{Q}$ cross-section in k_{\perp} -factorized form :

$$\frac{d\sigma_{pp \rightarrow Q\bar{Q}}}{d\Phi_Q d\Phi_{\bar{Q}}} = \int \frac{\delta(\vec{k}_{1\perp} + \vec{k}_{2\perp} - \vec{p}_{\perp}(Q\bar{Q}))}{k_{1\perp}^2 k_{2\perp}^2} \varphi_p(x_1, k_{1\perp}) \varphi_p(x_2, k_{2\perp}) |\mathcal{M}|^2$$

■ Pros :

- ◆ Includes intrinsic k_{\perp} and of resums logs of $1/x$
- ◆ Some NLO and NNLO diagrams are already included
- ◆ This formalism can be generalized to include saturation

■ Cons :

- ◆ The incoming gluons are off-shell \Rightarrow difficult calculations
- ◆ Only a subset of the NLO terms is included
- ◆ Factorization proven only to Leading Log



Color glass condensate

Introduction

Collinear factorization

QQbar production at small x

● Relevant x range

● Kt-factorization

● Color glass condensate

● High density effects for pA

● AA collisions

McLerran, Venugopalan (1994)

Iancu, Leonidov, McLerran (2001)

- Small x modes have a large occupation number
 - ▷ they are described by a **classical color field**
- Large x modes are described by “frozen” color sources ρ_a
- The classical field obeys Yang-Mills equations:

$$[D_\nu, F^{\nu\mu}]_a = \delta^{\mu+} \delta(x^-) \rho_a(\vec{x}_\perp)$$

- The color sources ρ_a are **random**, and their distribution is described by a **functional** $W_{x_0}[\rho]$, where x_0 is the separation between “small x ” et “large x ”. $W_{x_0}[\rho]$ changes with x_0 according to the **JIMWLK** equation.
- Observables are calculated in the presence of the classical field, and then averaged over the configurations of the sources ρ_a :

$$\langle \mathcal{O} \rangle = \int [D\rho_a] W_{x_0}[\rho_a] \mathcal{O}[\rho_a]$$



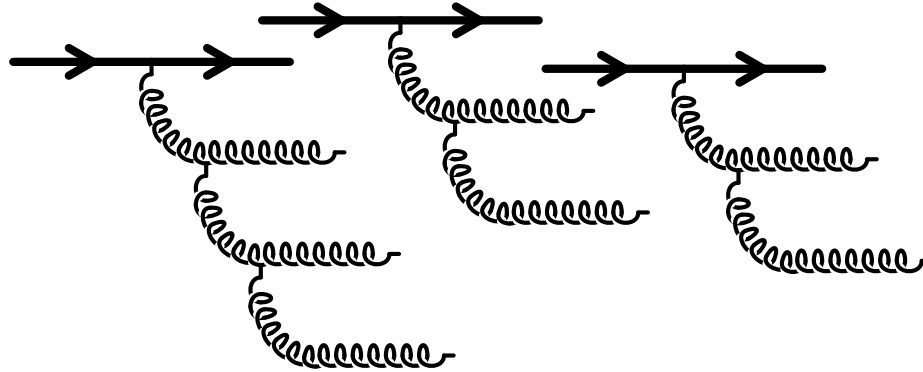
Quark production in the CGC

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▷ get $W_{x_1}[\rho_1]$ for the first projectile

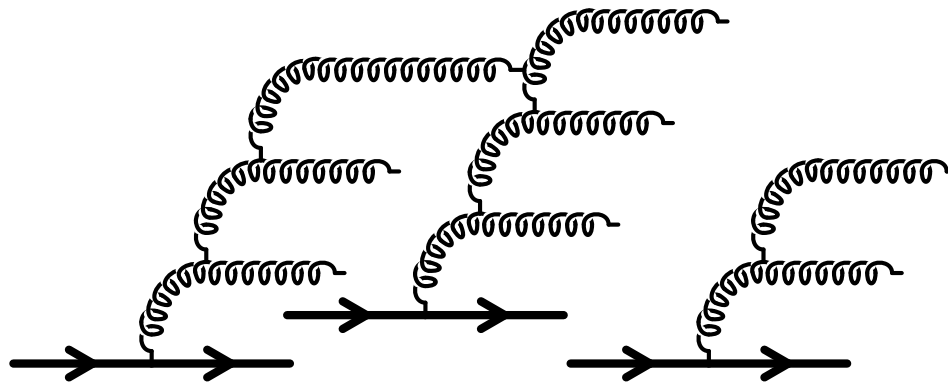
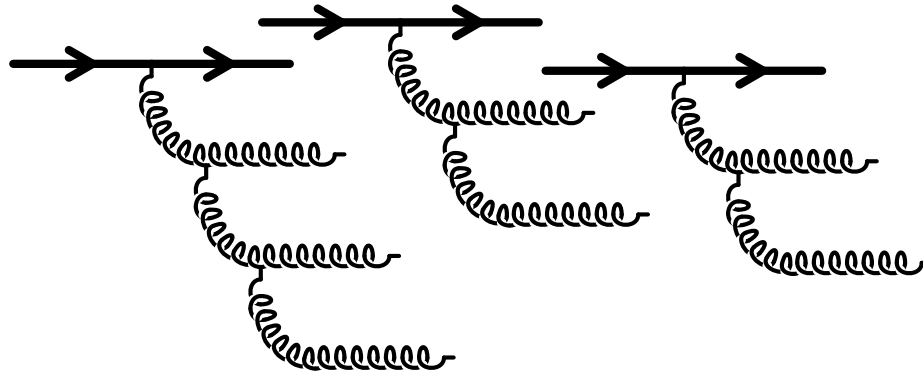
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▷ get $W_{x_2}[\rho_2]$ for the second projectile

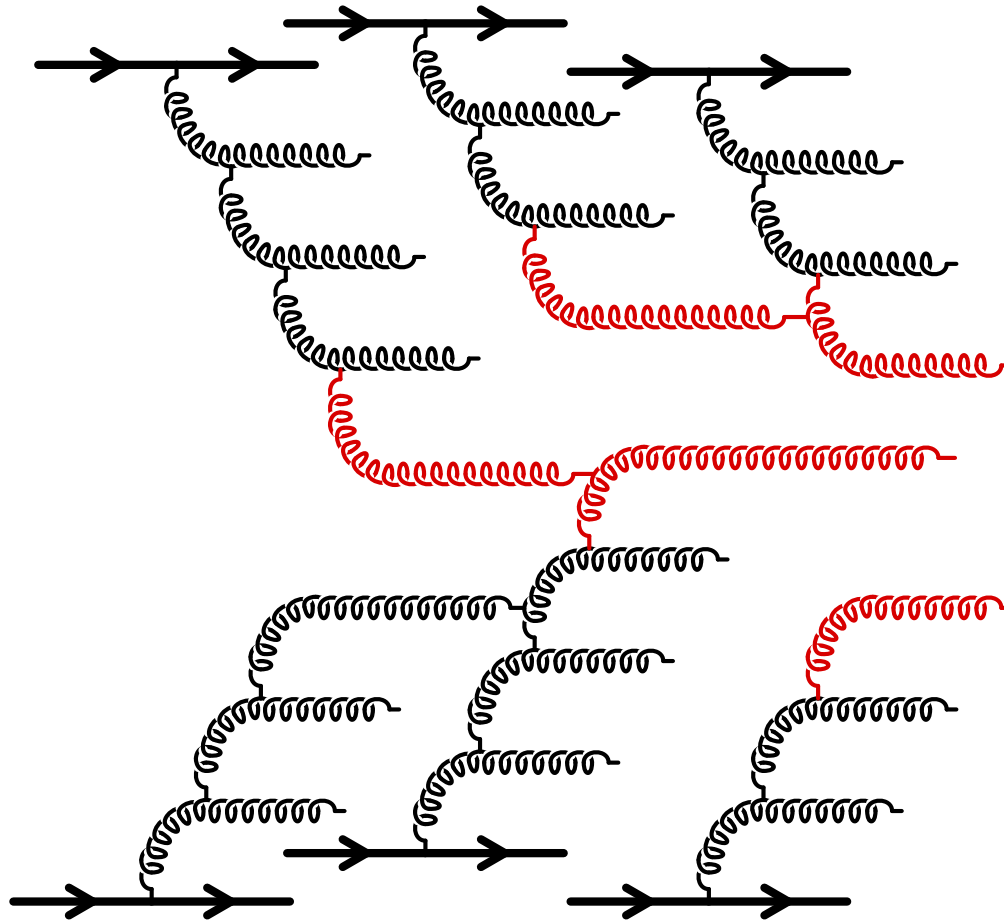
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▷ solve the Yang-Mills equations for the sources ρ_1, ρ_2

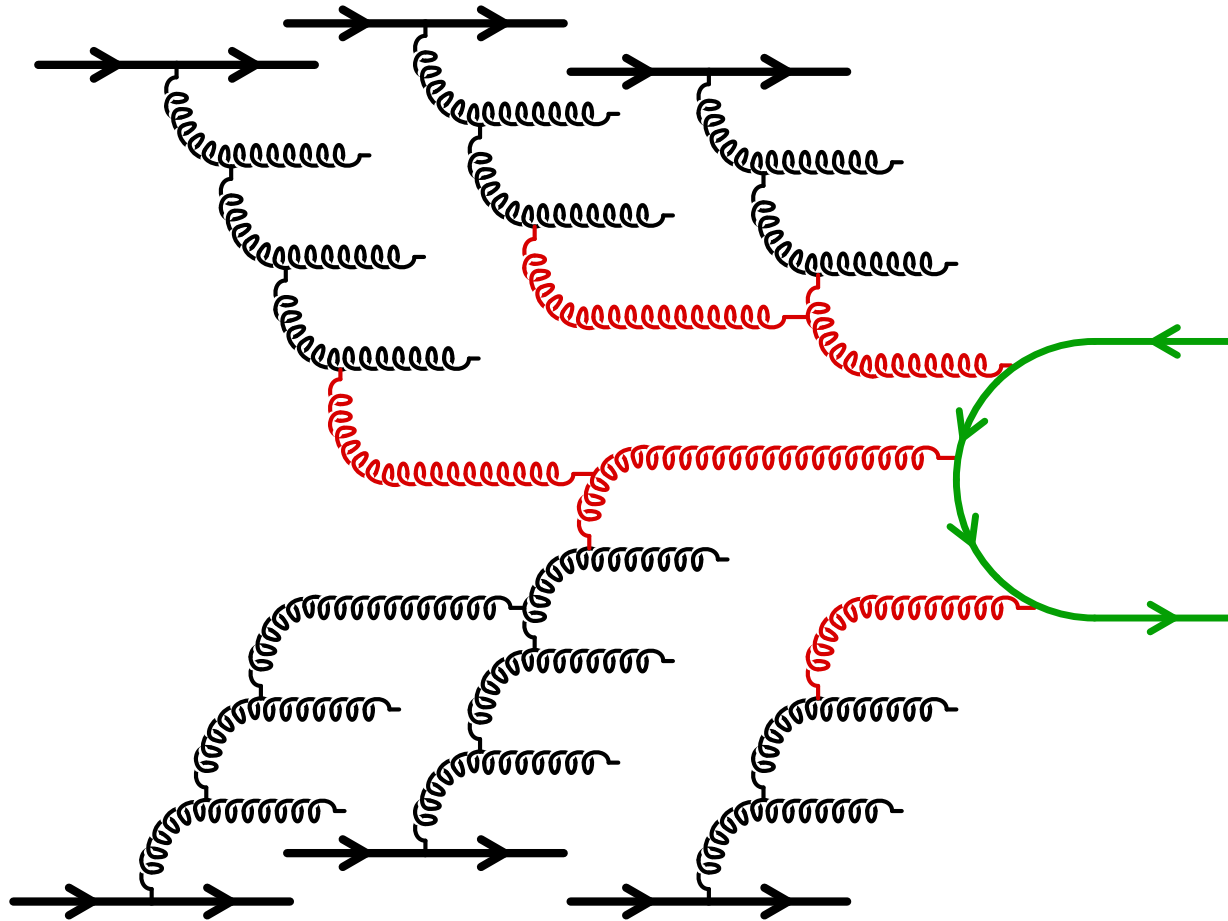
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▷ compute the quark propagator in the classical field



Quark production in the CGC

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Baltz, FG, McLerran, Peshier (2001)

FG, Venugopalan (2003)

Blaizot, FG, Venugopalan (2004)

- The single inclusive quark spectrum can be expressed in terms of the **retarded** quark propagator :

$$E_p \frac{dN_Q}{d^3\vec{p}} \sim \int \frac{d^3\vec{q}}{(2\pi)^3 2E_q} |\bar{u}(\vec{p}) T_R(p, -q) v(\vec{q})|^2$$

- The calculation can be carried out analytically only at lowest order in one of the two sources

i.e. $\rho_1 \sim g^{-1} \quad \rho_2 \rightarrow 0$

Cronin effect for single quarks

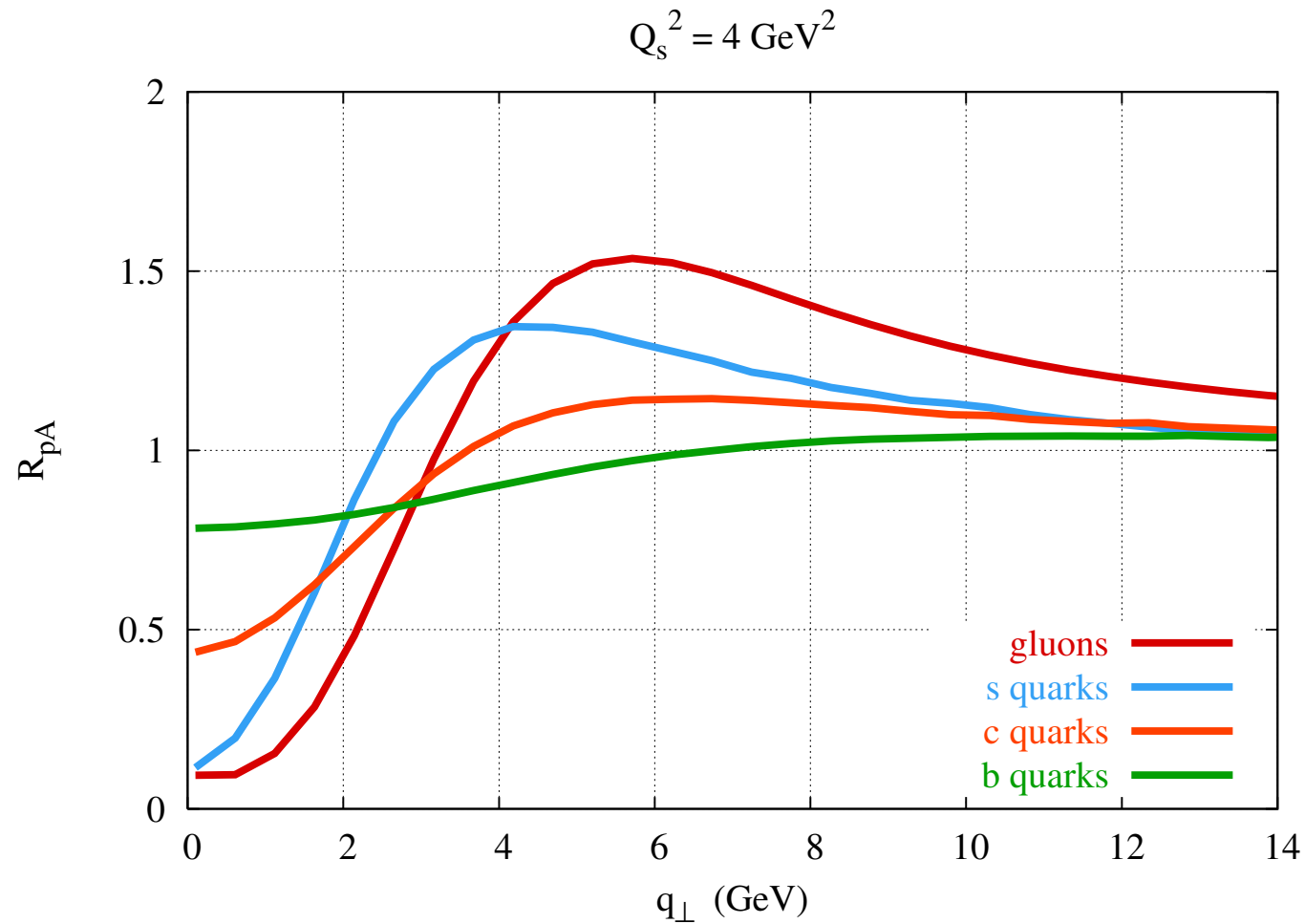
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■ RpA at moderate x :



Cronin effect for single quarks

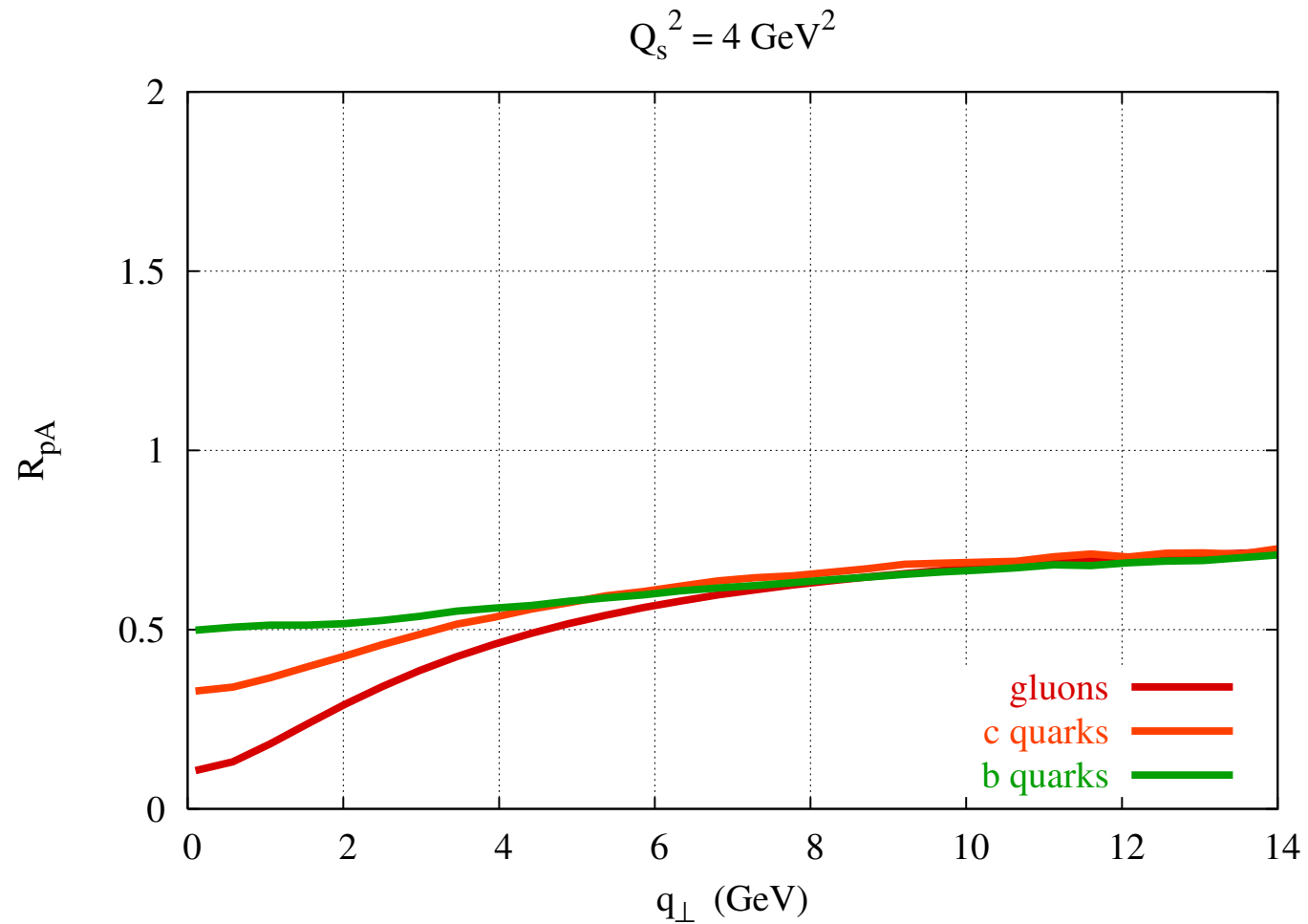
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Collinear factorization

QQbar production at small x

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■ RpA at small x :





Formulation for AA collisions

Introduction

Collinear factorization

QQbar production at small x

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- AA collisions

FG, Kajantie, Lappi (2004, 2005)

- To all orders in both sources, the gauge field is known only numerically. It is possible to reformulate the problem of quark production in a way which is suitable for a numerical approach
- Alternate representation of the **retarded** amplitude:

$$\bar{u}(\vec{q}) T_R(p, -q) v(\vec{p}) = \lim_{\tau \rightarrow +\infty} \tau \int d\eta d^2 \vec{x}_\perp e^{i p \cdot x} u^\dagger(\vec{p}) e^{-\eta \gamma^0 \gamma^3} \psi_q(t, \vec{x})$$

where $\psi_q(t, \vec{x})$ obeys Dirac's equation with retarded boundary conditions :

$$(i \not{\partial}_x - g A(x) - m) \psi_q(x) = 0, \quad \psi_q(t, \vec{x}) \xrightarrow[t \rightarrow -\infty]{} v(\vec{q}) e^{i q \cdot x}$$

Classical color field

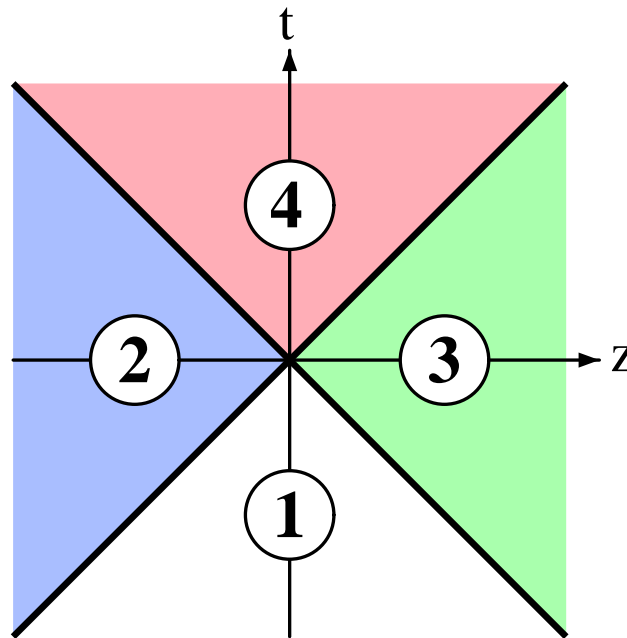
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Space-time structure of the classical color field:



- ◆ Region 1: $A^\mu = 0$
- ◆ Region 2: $A^\pm = 0$,
 $A^i = \frac{i}{g} U_1 \nabla_\perp^i U_1^\dagger$
- ◆ Region 3: $A^\pm = 0$,
 $A^i = \frac{i}{g} U_2 \nabla_\perp^i U_2^\dagger$
- ◆ Region 4: $A^\mu \neq 0$

Notes:

- ◆ $U_{1,2}(\vec{x}_\perp) = \exp(-ig \frac{1}{\nabla_\perp^2} \rho_{1,2})$
- ◆ In the region 4, A^μ is known only numerically
Krasnitz, Venugopalan (2000,2001), Lappi (2003)

Quark propagation

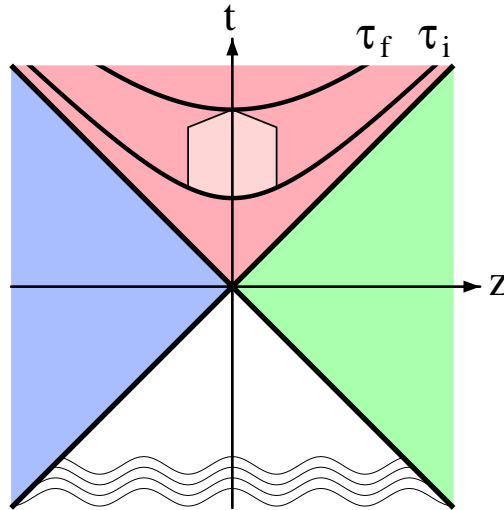
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- Propagation through region 4:



$$\partial_\tau \psi_{\mathbf{p}}(\tau, \eta, \vec{x}_\perp) = \left[-\frac{1}{2\tau} - \frac{\gamma^0 \gamma^3}{\tau} (\partial_\eta + igA_\eta) \right. \\ \left. + \gamma^0 \vec{\gamma}_\perp \cdot (\vec{\nabla}_\perp + ig\vec{A}_\perp) - i\gamma^0 m \right] \psi_{\mathbf{p}}(\tau, \eta, \vec{x}_\perp)$$

- The initial condition is known analytically at $\tau_i \rightarrow 0^+$

Time dependence

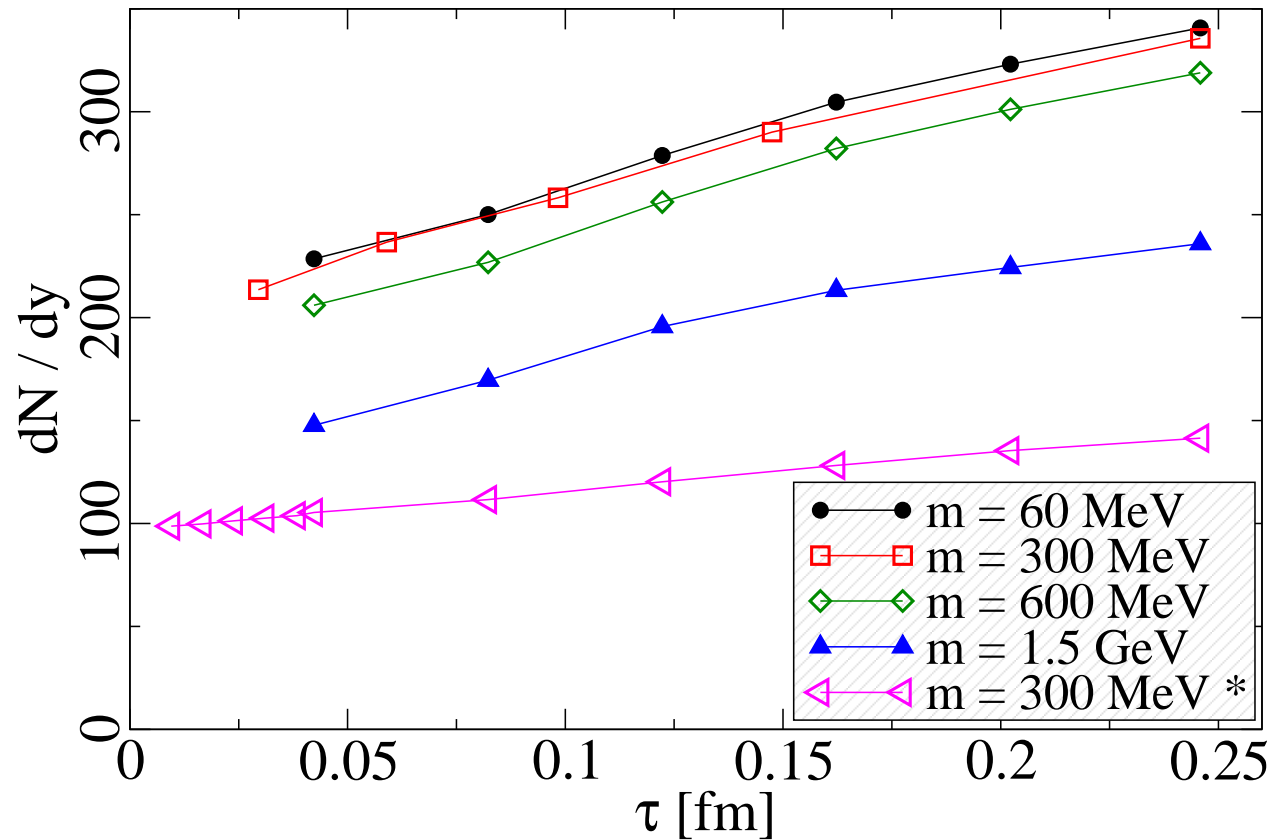
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Collinear factorization

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- $g^2\mu = 2 \text{ GeV}$, (*) $g^2\mu = 1 \text{ GeV}$:



Spectra for various quark masses

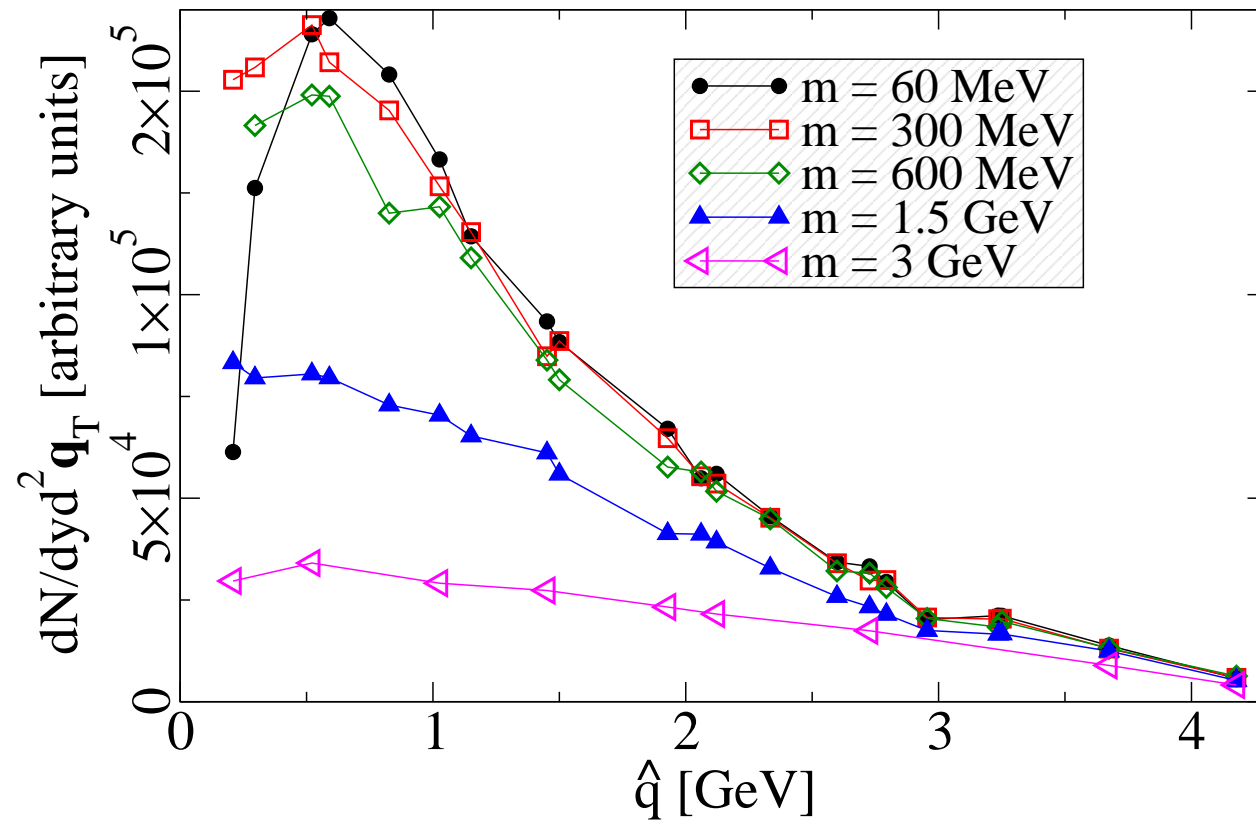
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Collinear factorization

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■ $g^2 \mu = 2 \text{ GeV}$, $\tau = 0.25 \text{ fm}$:



Qs dependence of dN/dy

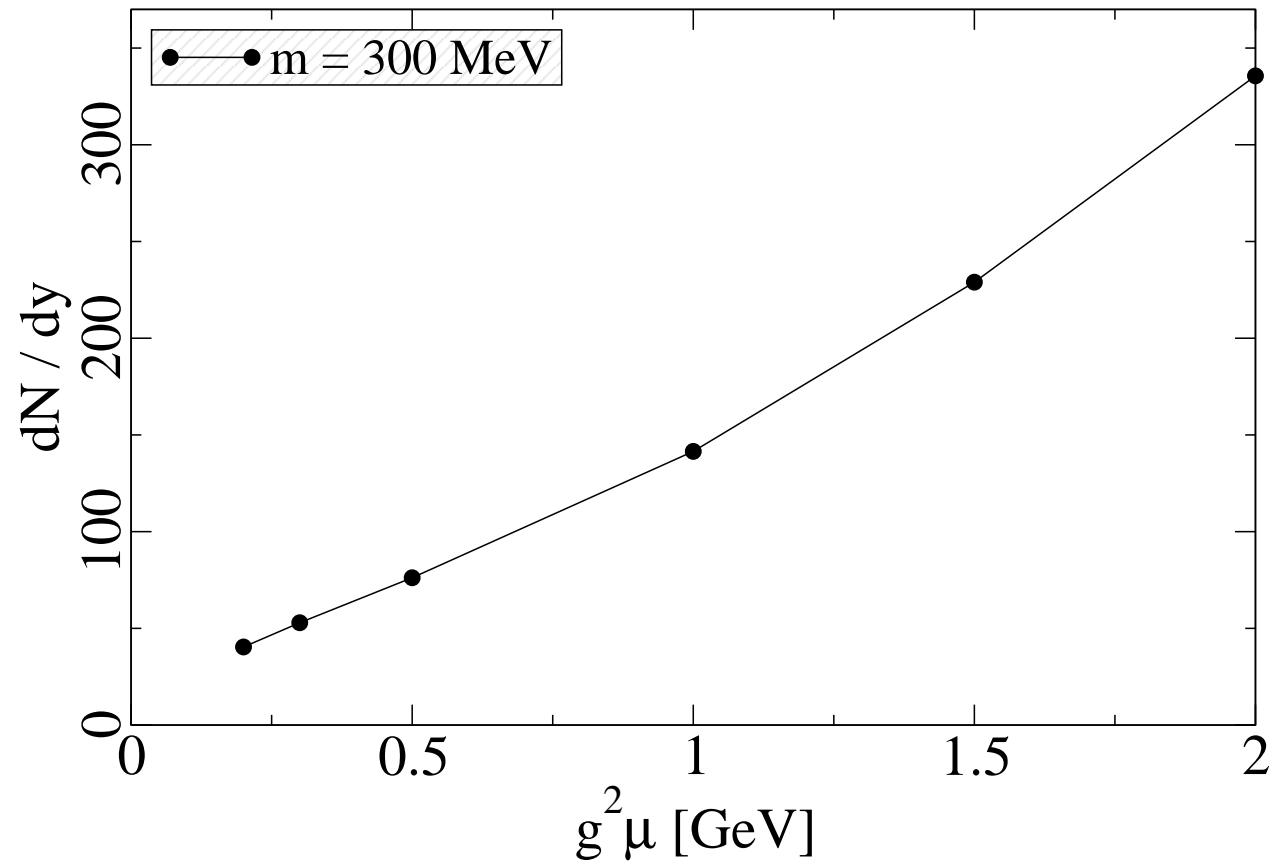
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QQbar production at small x

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- Number of quarks at $\tau = 0.25$ fm :





Shortcomings

Introduction

Collinear factorization

QQbar production at small x

- Relevant x range
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- Color glass condensate
- High density effects for pA
- AA collisions

- Factorization of logs of $1/x$ plausible not proven
- Numerical evaluation done on a coarse lattice due to limited computational resources
 - ▷ large lattice artifacts at large momentum/mass
- Instead of $dN_Q/d^3\vec{p}$, one should calculate $f_Q(t, \vec{x}, \vec{p})$
(easy to fix)



Introduction

Collinear factorization

QQbar production at small x

Dynamical evolution

● QQbar recombination

Dynamical evolution



QQbar recombination

Introduction

Collinear factorization

QQbar production at small x

Dynamical evolution

● QQbar recombination

- What has been said so far is correct if there is only a few $Q\bar{Q}$ pairs in the system
- At LHC energies, pQCD predicts that hundreds of $c\bar{c}$ pairs are being produced in a central PbPb collision
- Q and \bar{Q} that have been produced uncorrelated may encounter and form a quarkonium state
- Model independent estimates :
 - ◆ $\text{Prob}(J/\psi) \sim N_c/N_{u,d,s} \sim N_{c\bar{c}}/N_{\text{ch}}$
 - ◆ $N_{J/\psi} \sim N_{c\bar{c}}^2/N_{\text{ch}}$
 - ◆ Since $N_{c\bar{c}}^2$ grows faster with energy than N_{ch} , this mechanism of J/ψ production will eventually be dominant
- Two different implementations :
 - ◆ Statistical hadronization
 - ◆ Kinetic models



Statistical hadronization

Introduction

Collinear factorization

QQbar production at small x

Dynamical evolution

● QQbar recombination

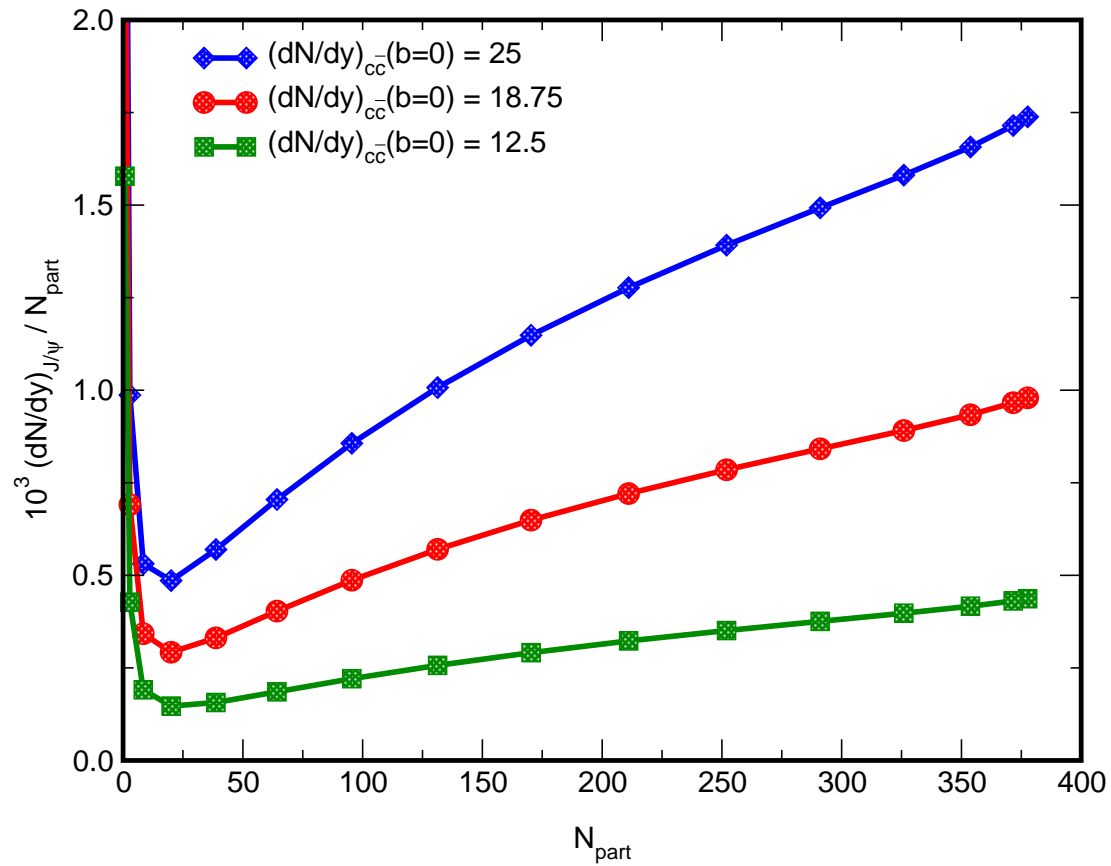
Braun-Munzinger, Stachel (2000)

- Early attempts to include charm in thermal fits underpredicted the yield of charmed hadrons
- However, the ratio $\sigma_{\psi'}/\sigma_{J/\psi}$ measured at SPS goes to its thermal value when N_{part} is large
- One assumes that the number of c, \bar{c} quarks is determined by early hard collisions (no thermal production/annihilation)
- Hadronization is assumed to follow thermal distributions, modified by an “enhancement factor” γ_c (one power of γ_c per c or \bar{c} quark in the hadron). Conservation of charm :

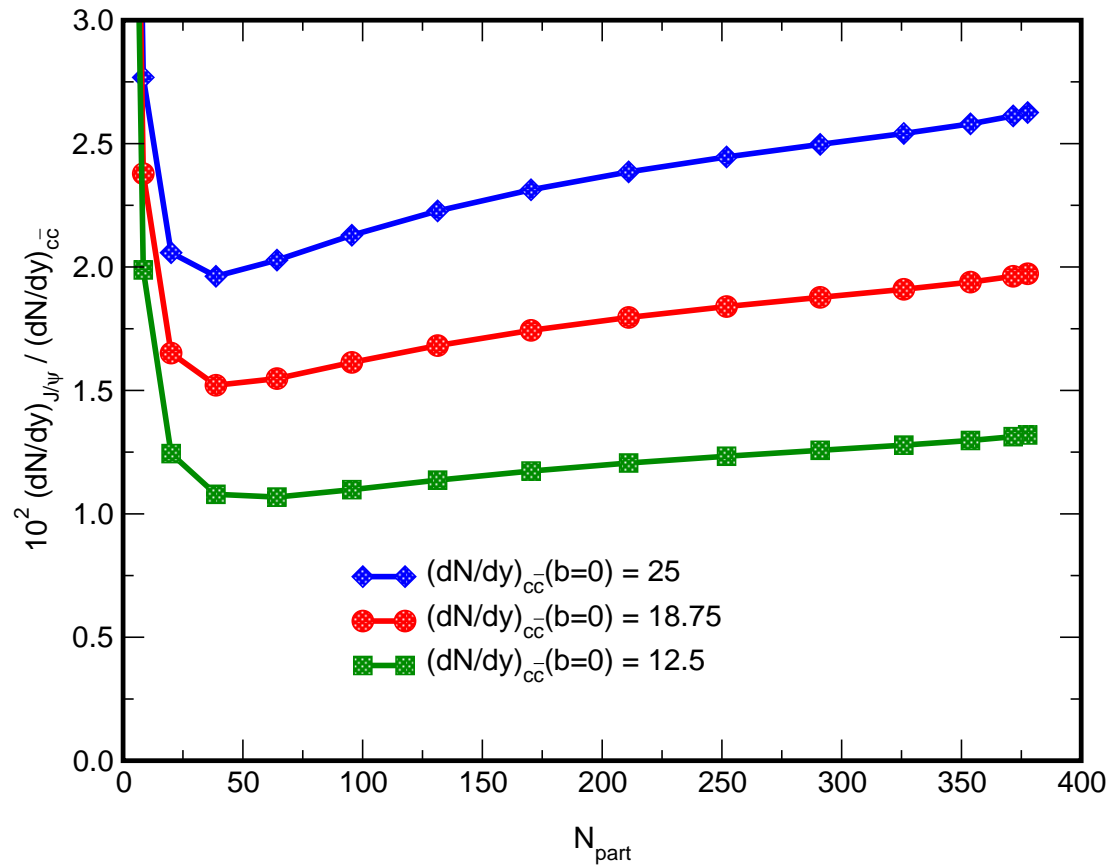
$$N_{c\bar{c}}^{\text{direct}} = \frac{1}{2} \gamma_c V \sum_i (n_{\text{th}}(D_i) + n_{\text{th}}(\Lambda_i)) + \gamma_c^2 V \sum_i n_{\text{th}}(\psi_i) + \dots$$

- Then : $N_D = \gamma_c V n_{\text{th}}(D)$ and $N_{J/\psi} = \gamma_c^2 V n_{\text{th}}(J/\psi)$

■ LHC : J/ψ yield per participant



■ LHC : J/ψ yield per $c\bar{c}$ pair



▷ this behavior with centrality is the opposite of what one expects in the Matsui-Satz scenario



Kinetic formation

Introduction

Collinear factorization

QQbar production at small x

Dynamical evolution

● QQbar recombination

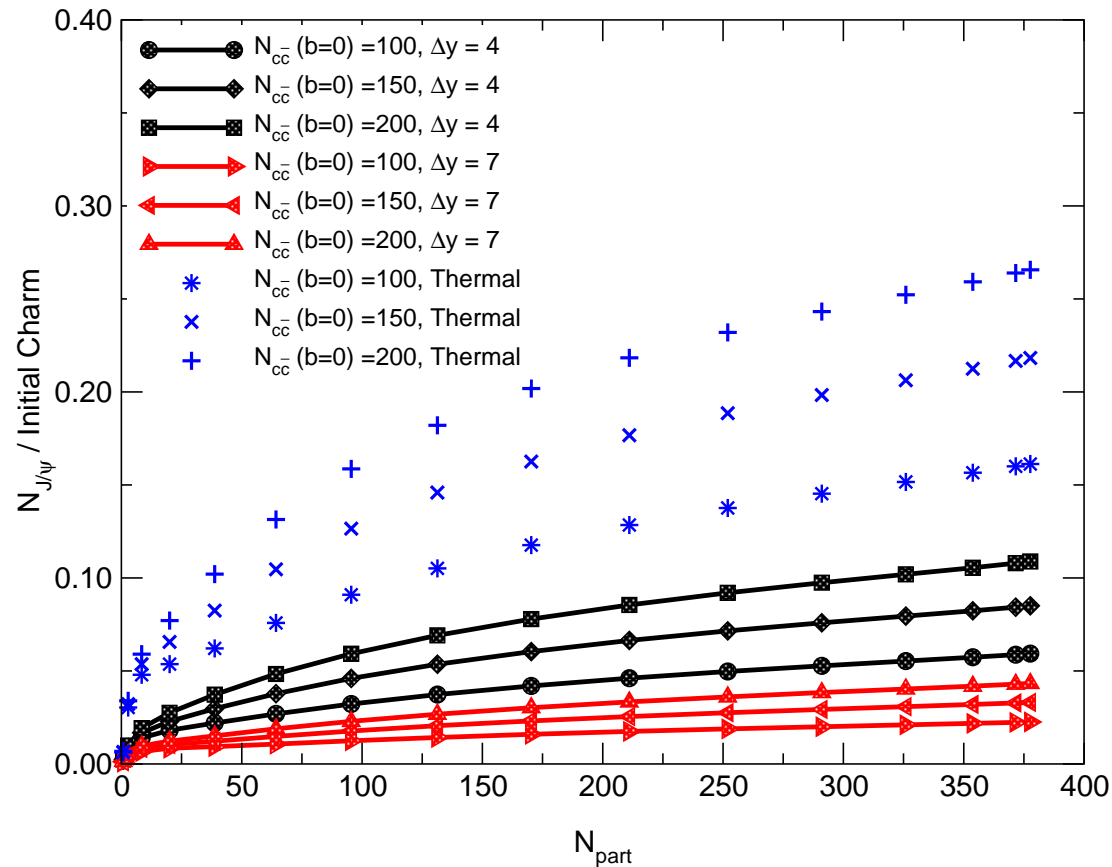
Thews, Schroedter, Rafelski (2001)

- Dominant in-medium J/ψ breakup process : $g + J/\psi \rightarrow c\bar{c}$
- The reverse process $c\bar{c} \rightarrow J/\psi + g$ should also occur, with a probability that increases like the square of the density of charmed quarks
- Kinetic equation :

$$\frac{dN_{J/\psi}}{d\tau} = \lambda_F \frac{N_c N_{\bar{c}}}{V(\tau)} - \lambda_D \rho_g N_{J/\psi}$$

- ◆ $V(\tau)$: τ -dependent volume (expansion plays against recombination)
- ◆ ρ_g : gluon density
- ◆ $\lambda_{F,D}$: formation and dissociation rates ($\lambda = \overline{\sigma v_{\text{rel}}}$)
- Solution : $N_{J/\psi}(\tau) = \epsilon(\tau) \left[N_{J/\psi}(\tau_i) + N_{c\bar{c}}^2 \int_{\tau_i}^{\tau} d\tau \frac{\lambda_F}{V(\tau)\epsilon(\tau)} \right]$
with $\epsilon(\tau) = \exp\left(-\int_{\tau_i}^{\tau} d\tau \rho_g \lambda_D\right)$

■ LHC : J/ψ yield per $c\bar{c}$ pair



- ◆ very sensitive to the distribution of initial charm
See [Gossiaux, Guiho, Aichelin \(2004\)](#) for a Fokker-Plank description of the time evolution of the c, \bar{c} distributions



Introduction

Collinear factorization

QQbar production at small x

Bound states in a medium

- Hadronization in vacuum
- in-medium suppression
- lattice results

Bound states in a dense medium



Quarkonium production in vacuum

Introduction

Collinear factorization

QQbar production at small x

Bound states in a medium

● Hadronization in vacuum

● in-medium suppression

● lattice results

- More difficult than the inclusive fragmentation $c \rightarrow D + X$
- LO is clearly insufficient in order to get the p_{\perp} distribution of J/ψ or Υ , since by construction $p_{\perp}(Q\bar{Q}) = 0$ at this order
- Several approaches :
 - ◆ Color Singlet Model (CSM)
 - ◆ Non-Relativistic QCD (NRQCD) [aka Color Octet Model]
 - ◆ Color Evaporation Model (CEM)
 - ◆ Comover Enhancement Scenario (CES)



Charmonium suppression in the QGP

Introduction

Collinear factorization

QQbar production at small x

Bound states in a medium

● Hadronization in vacuum

● in-medium suppression

● lattice results

Matsui, Satz (1986), Kharzeev, Satz (1994), and many others...

- If the Debye screening radius is smaller than the size of quarkonium state, the binding of the Q and \bar{Q} is destroyed by the surrounding light quarks and gluons
- The Q and \bar{Q} drift in the QGP, and cannot find each other again
- At hadronization time, they pick up a light quark and form D or B mesons
- A suppression of the ratio $[J/\psi] / [\text{Open charm}]$ could be a signature of the QGP
- Not as simple though : there is also a suppression in pA collisions. One should therefore look for “anomalous” suppression effects



Normal nuclear suppression

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- Parameterization of the J/ψ absorption in cold nuclear matter :

$$\sigma_{\text{abs}}(\sqrt{s}) = \sigma_{\text{abs}}(\sqrt{s_0}) \left(\frac{s}{s_0} \right)^{\Delta/2}$$

$$\sigma_{\text{abs}}(\sqrt{s_0} = 17.3 \text{ GeV}) = 5 \pm 0.5 \text{ mb} \quad , \quad \Delta \approx 0.125$$

- Quarkonium survival probability in an AB collision :

$$S(\vec{b}) = \int d^2 \vec{s} dz_A dz_B \rho_A(\vec{s}, z_A) \rho_B(\vec{b} - \vec{s}, z_B) \\ \times \exp \left[-(A-1) \int_{z_A}^{\infty} dz \rho_A \sigma_{\text{abs}} \right] \exp \left[-(B-1) \int_{z_B}^{\infty} dz \rho_B \sigma_{\text{abs}} \right]$$

Normal nuclear suppression

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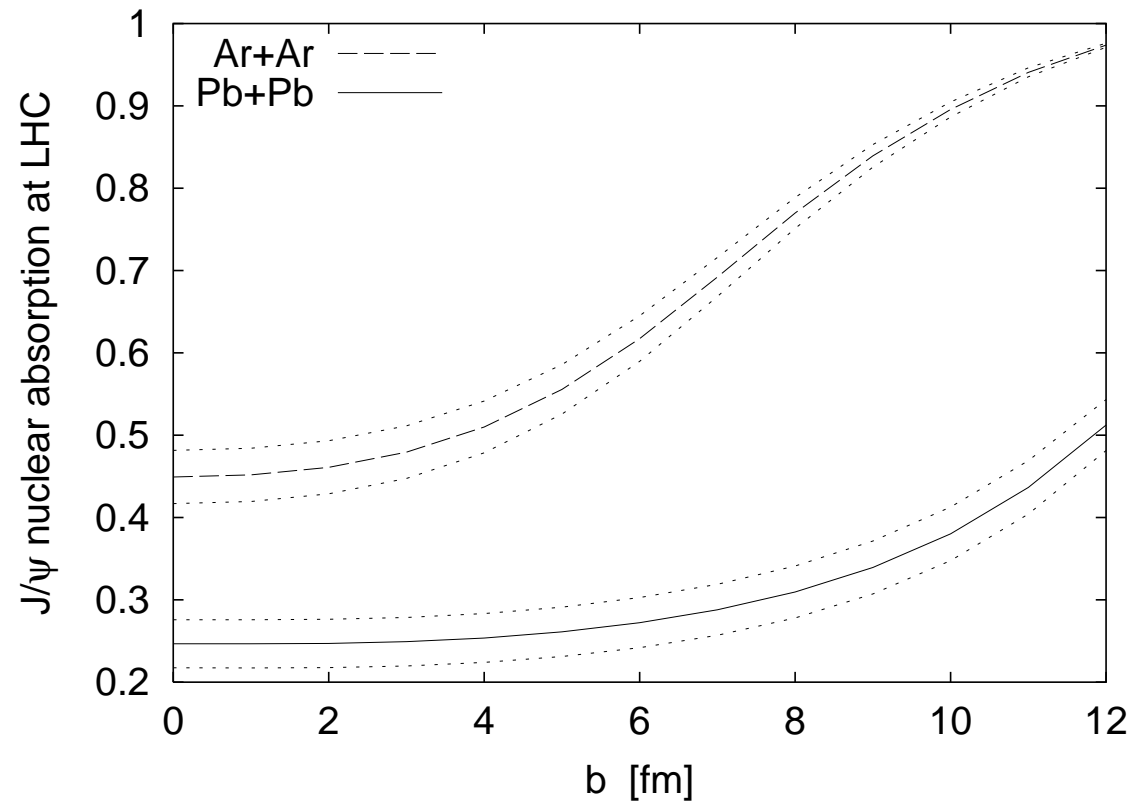
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- Impact parameter dependence of the survival probability :





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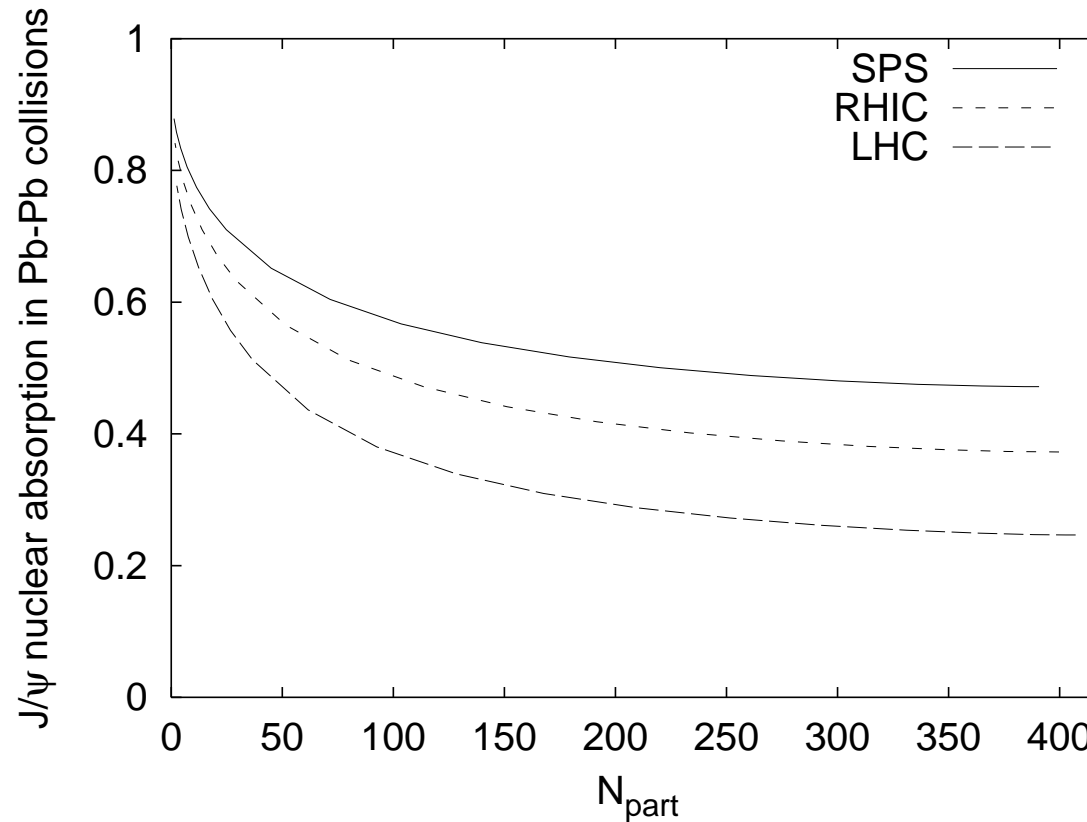
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- N_{part} dependence of the survival probability :





Lattice results

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- Reminder : only Euclidean quantities can be calculated directly in lattice Monte-Carlo simulations :

$$\text{Minkowkian} : e^{iS[A^\mu]} \longrightarrow \text{Euclidean} : e^{-S[A^\mu]}$$

- Potential between pairs of heavy quarks in a QGP
 - ◆ Can be fed into a non-relativistic Schrödinger equation in order to compute the binding energy of the bound states
- Extraction of the $Q\bar{Q}$ spectral functions from lattice data
 - ◆ Fairly new method, still in development
 - ◆ Results in qualitative agreement with the previous one
- These issues are totally unexplored at finite μ_B



Heavy quark potential

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- The “averaged” free-energy is obtained from Polyakov loops :

$$e^{-F(r,T)/T} = \frac{1}{9} \left\langle \text{tr} L(\vec{r}) \text{tr} L^\dagger(\vec{0}) \right\rangle, \quad L(\vec{r}) = \prod_{i=1}^{N_\tau} U_0(\vec{r}, \tau)$$

- It can be divided into a color singlet and a color octet parts :

$$e^{-F(r,T)/T} = \frac{1}{9} e^{-F_1(r,T)/T} + \frac{8}{9} e^{-F_8(r,T)/T}$$

$$e^{-F_1(r,T)/T} = \frac{1}{3} \left\langle \text{tr} L(\vec{r}) L^\dagger(\vec{0}) \right\rangle$$

$$e^{-F_8(r,T)/T} = \frac{1}{8} \left\langle \text{tr} L(\vec{r}) \text{tr} L^\dagger(\vec{0}) \right\rangle - \frac{1}{24} \left\langle \text{tr} L(\vec{r}) L^\dagger(\vec{0}) \right\rangle$$

- In principle, one needs to transform that into the potential energy U :

$$F = U - TS, \quad S = -\frac{\partial F}{\partial T}$$

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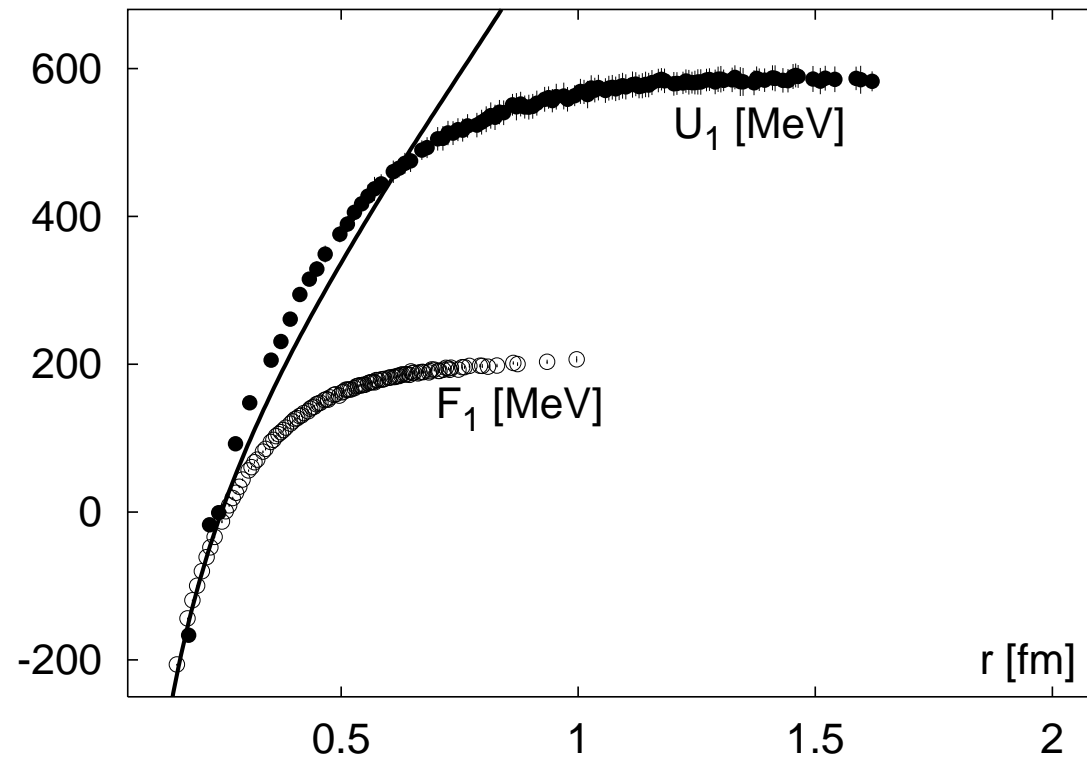
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■ Results for $T/T_c = 1.5$:



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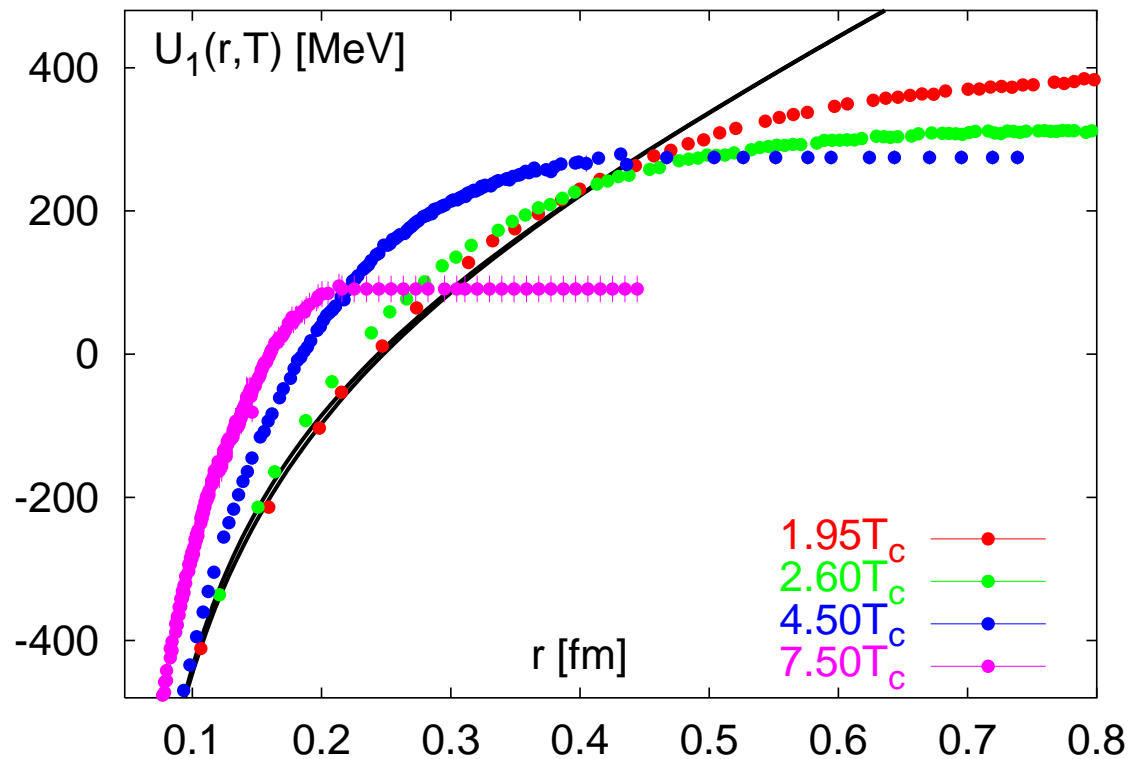
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- T -dependence of the potential above T_c :



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■ What do we do with that?

- ◆ Shrödinger equation for $Q\bar{Q}$ bound states :

$$\left[2m_Q + \frac{1}{m_Q} \vec{\nabla}^2 + U_1(r, T) \right] \psi_i = M_i(T) \psi_i$$

- ◆ Non-relativistic
- ◆ Assumes 2-body interactions only

■ Dissociation temperatures :

state	J/ψ	χ_c	ψ'	Υ	χ_b	Υ'
T_d/T_c	2.0	1.1	1.1	4.5	2.0	2.0

▷ the quarkonium states do not get immediately dissolved above the critical temperature



Heavy quark spectral functions

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- Method for extracting spectral functions :

$$G_H(\tau, \vec{p}) = \int_0^\infty d\omega \rho_H(\omega, \vec{p}|T) \frac{\cosh(\omega(\tau - 1/2T))}{\sinh(\omega/2T)}$$

$$G_H(\tau, \vec{p}) = \int d^3\vec{x} e^{i\vec{p}\cdot\vec{x}} \langle J_H(\tau, \vec{x}) J_H(0, \vec{0}) \rangle, \quad J_H = \bar{\psi} \Gamma_H \psi$$

state	χ_c^0	η_c	J/ψ	χ_c^1
Γ_H	1	γ_5	γ_μ	$\gamma_\mu \gamma_5$

- $\rho_H(\omega, \mathbf{p})$ has a sharp peak for stable states in the corresponding channel (broad peak for an unstable state)
- Main problem : $G_H(\tau, \vec{p})$ is known at a finite number of τ 's
 - ▷ the inversion of the spectral integral in order to obtain the function ρ_H is a mathematically ill-defined problem



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■ Maximum Entropy Method :

- ◆ Many more degrees of freedom in $\rho_H(\omega, \vec{p})$ than data points
 - ▷ a χ^2 -fit would have flat directions...
- ◆ Most of the multiple solutions would have unphysical features: non-positivity, not smooth, incorrect large ω behavior
- ◆ Idea : add a convex term F to the χ^2 so that there is a unique minimum

$$\chi^2 \longrightarrow \chi^2 + \alpha F[\rho_H]$$

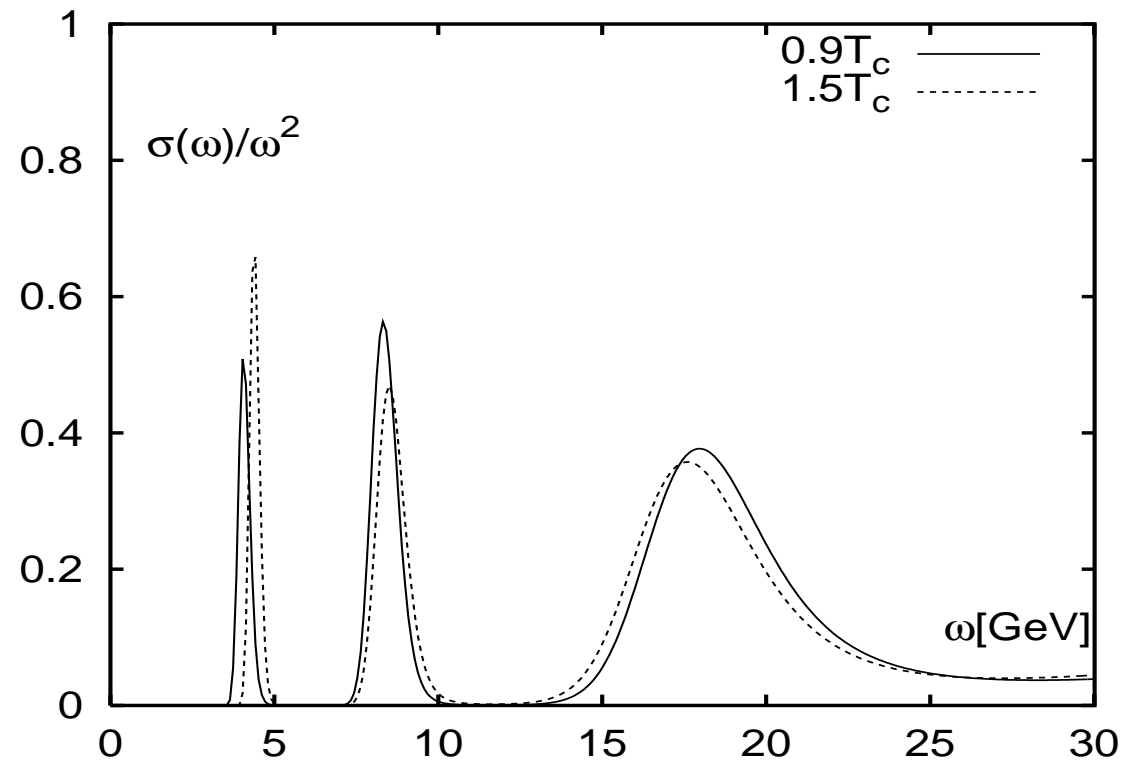
- ◆ MEM :

$$F[\rho_H] = \int_0^\infty d\omega [\rho_H(\omega) - \rho_0(\omega) - \rho_H(\omega) \ln(\rho_H(\omega)/\rho_0(\omega))]$$

- ▷ ensures the positivity of ρ_H
- ▷ for $\alpha \rightarrow \infty$, the solution wants to be identical to the “prior” ρ_0
- ▷ use with extreme caution because you may only get what you bring...

Heavy quark spectral function

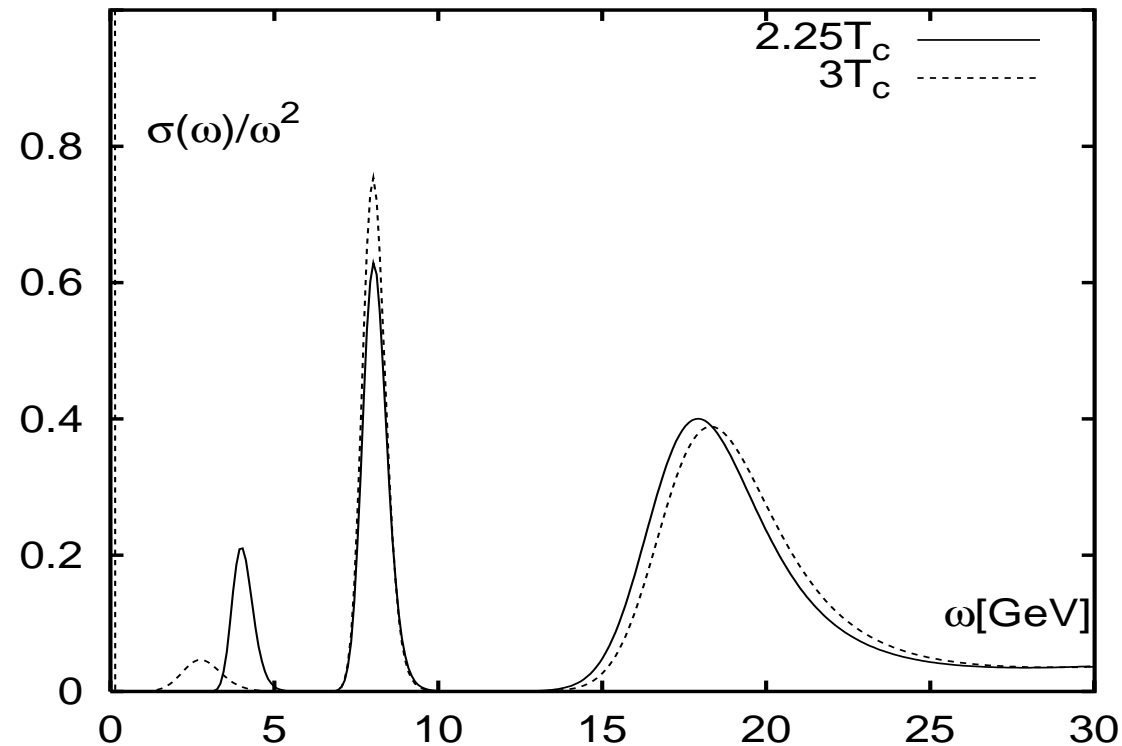
- J/ψ spectral function below T_c :



- The second and third peaks (the fat ones...) are lattice artifacts. Shouldn't we worry about them contaminating the physical peak?

Heavy quark spectral function

- J/ψ spectral function above T_c :



- The J/ψ peak starts going down for T above $2T_c$
 - ▷ good qualitative agreement with the method based on the heavy quark potential