

The In-Medium Behaviour of Finite Width Charmonia

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Hot & Dense Matter

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Statistical QCD

For $T \geq T_c \simeq 150 - 200$ MeV, strongly interacting matter becomes plasma of deconfined quarks and gluons (QGP)

How to probe QGP in strong interaction thermodynamics?

- e-m signals (real or virtual photons)
- quarkonia ($Q\bar{Q}$ pairs)
- jets (fast partons)

Ultimate aim:

ab initio calculation of in-medium behaviour of probes

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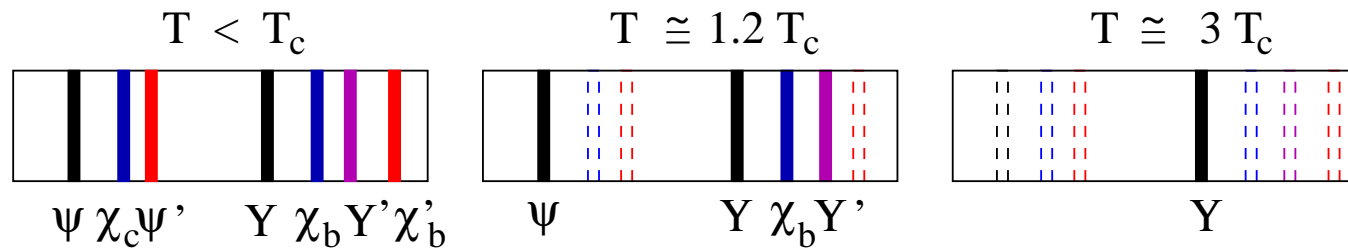
Survival of Charmonium States in Hot QGP

\Rightarrow Spectral Analysis of QGP \Leftarrow

NB: Thermodynamics, not nuclear collisions

Conceptual basis

- QGP consists of deconfined colour charges, hence
 - \exists colour charge screening for $Q\bar{Q}$ probe
- screening radius $r_D(T)$ decreases with temperature T
- when $r_D(T)$ falls below binding radius r_i of $Q\bar{Q}$ state i ,
 - Q and \bar{Q} cannot bind, quarkonium i cannot exist
- quarkonium dissociation points T_i specify temperature of QGP



How can one calculate quarkonium dissociation points?

Two possibilities:

- solve Schrödinger equation using a temperature-dependent heavy quark potential $V(r, T)$
- calculate quarkonium spectrum directly in finite T lattice QCD

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1. Potential Models for Quarkonium Dissociation

- heavy quark potential \sim Schwinger model

Karsch et al. 1988

Digal et al. 2001

$$V(r, T) = \sigma r \left\{ \frac{1 - e^{-\mu r}}{\mu r} \right\} - \frac{\alpha}{r} e^{-\mu r}$$

with screening mass $\mu(T) = 1/r_D(T)$

solve Schrödinger equation: with increasing T , bound state i disappears at some $\mu_i(T) = \mu(T_i)$

use screening mass from lattice estimates $\mu(T) \simeq 4 T$ for $T > 0$ to determine dissociation temperature T_i

charmonia:

ψ' and χ_c dissociated at $T \simeq T_c$

J/ψ at $T \simeq 1.2 T_c$

charmonia:

$$\psi' \text{ and } \chi_c \text{ dissociated at } T \simeq T_c$$
$$J/\psi \text{ at } T \simeq 1.2 T_c$$

- determine potential $V(r, T)$ from lattice studies of heavy quark free energy; various different forms

Shuryak & Zahed 04; Wong 04,...; Alberico et al. 05,...; Digal et al. 05; Mocsy & Petreczky 05,...

Lattice studies provide free energy difference $F(r, T)$ between medium with and without heavy quark pair; one possibility:

$$F = U - TS, \quad S = (\partial F / \partial T) \text{ specifies internal energy } U(r, T)$$

$$V(r, T) = U(r, T) = F(r, T) - T(\partial F / \partial T)$$

with $N_f = 2$ lattice results for $F(r, T)$.

no need of any separate screening mass

solve Schrödinger equation: with increasing T , bound state i disappears at some T_i

charmonia:

ψ' dissociated at $T \simeq 1.1 T_c$

χ_c dissociated at $T \simeq 1.2 T_c$

J/ψ survives up to $T \simeq 2 T_c$

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- reason for later dissociation: $U(r, T)$ provides stronger binding than Schwinger model potential

ambiguity in specifying “lattice” potential: $U(r, T)$ or $F(r, T)$

$F(r, T)$ results \sim Schwinger model

various alternatives: $V(r, T) = a F(r, T) + b U(r, T)$ reduce binding, lower dissociation temperatures

- dissociation defined mathematically, by $r \rightarrow \infty$, $\Delta E \rightarrow 0$
hence \exists a bound state region in which $r > 1/T$, $\Delta E < T$

what does that mean?

resolution: determine dissociation points directly in finite T lattice QCD

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2. Lattice Studies of In-Medium Charmonium Survival

quenched: Umeda et al. 01,...; Asakawa & Hatsuda 04; Datta et al. 04,...; Iida et al. 05; Jakovac et al. 05; unquenched: Aarts et al. 05,...

Calculate correlation function $G_i(\tau, T)$ for specific mesonic quantum number channel i , specified by spectral distribution $\sigma_i(\omega, T)$

$$G(\tau, T) = \int d\omega \sigma_i(\omega, T) K(\omega, \tau, T)$$

with kernel

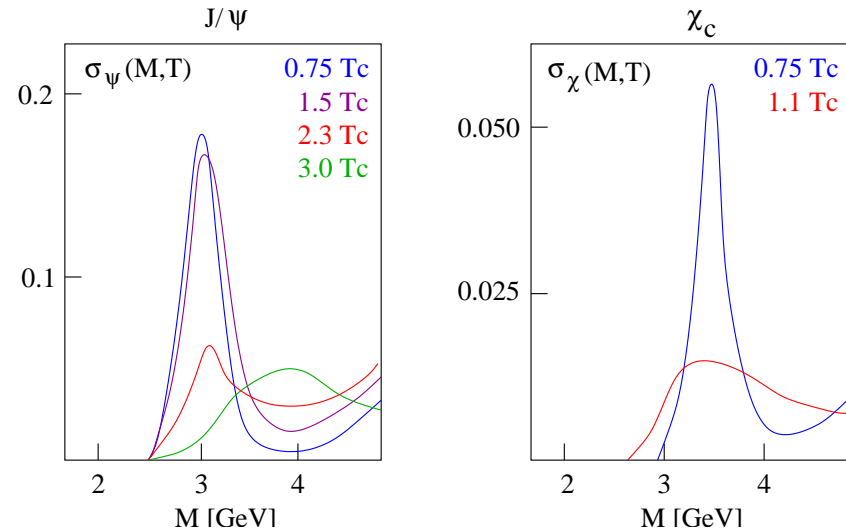
$$K(\omega, \tau, T) = \frac{\cosh[\omega(\tau - (1/2T))]}{\sinh(\omega/2T)}$$

relating imaginary time τ and $c\bar{c}$ energy ω ; invert $G(\tau, T)$ by **MEM** to get $\sigma(\omega, T)$:

- results for quenched and unquenched ($N_f = 2$) QCD agree

schematic pattern

lattice resolution limits
precision; reliable only
for resonance peak strength
& position, not for widths &
continuum ($\omega > 4 - 5$ GeV)



charmonia

χ_c is dissociated for $T \geq 1.1 T_c$
 J/ψ persists up to $1.5 T_c < T < 2.3 T_c$

preliminary conclusion: – higher excited states melt near T_c
 – J/ψ melts around $2 T_c$

(in accord with U -based potential model studies)

● caveat: finite T widths

report here on an attempt to address this problem:

H.-T. Ding, O. Kaczmarek, F. Karsch, HS (in preparation)

3. Construction Kit for Spectral Distributions

recall correlator $G(\tau, T) = \int d\omega \sigma_i(\omega, T) K(\omega, \tau, T)$

with kernel $K(\omega, \tau, T) = \cosh[\omega(\tau - (1/2T))]/\sinh(\omega/2T)$

and spectral distribution $\sigma_i(\omega, T)$ in $c\bar{c}$ channel i

present standard lattice study of charmonia in hot QGP:

compare correlator $G(\tau, T)$ for $T > T_c$

to a reference correlator $G_0(\tau, T)$

using spectral function at $T = 0$

$$G_0(\tau, T) = \int d\omega \sigma_i(\omega, T = 0) K(\omega, \tau, T)$$

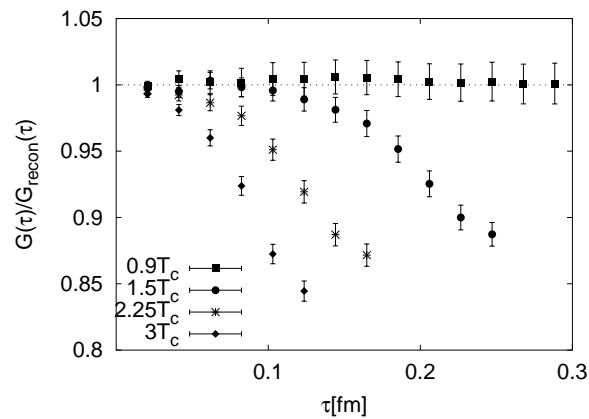
shows what correlator would look like if spectrum at $T > T_c$ were
same as at $T = 0$

ratio $R(\tau, T) = G(\tau, T)/G_0(\tau, T)$

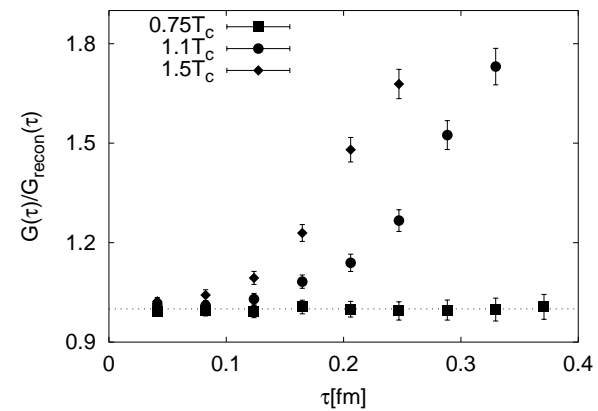
indicates finite temperature modifications of spectrum

use for $\sigma_i(\omega, T = 0)$ spectrum obtained for $0 < T \ll T_c$ from lattice QCD via MEM (some lattice artifacts cancel); get

Datta et al. 04



J/ψ (vector channel)



χ_{c0} (scalar channel)

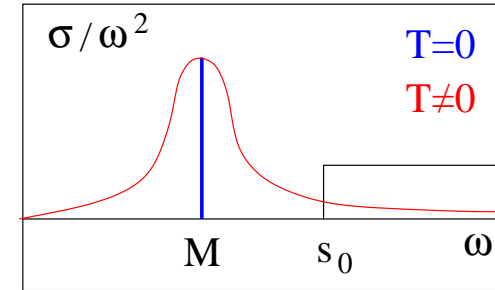
what does this tell us about spectrum, about compatibility of potential theory and lattice results?

Mocsy & Petreczky 05,...; Wong 06,...; Alberico et al. 06;...

idealized spectrum at $T = 0$

$$\sigma(\omega, T = 0) = f \delta(\omega - M) + c \omega^2 \theta(\omega - s_0)$$

$f \sim$ strength of resonance
 $c \sim$ strength of continuum



assume that at $T > 0$ resonance broadens (relativistic B-W),
 but retains same strength

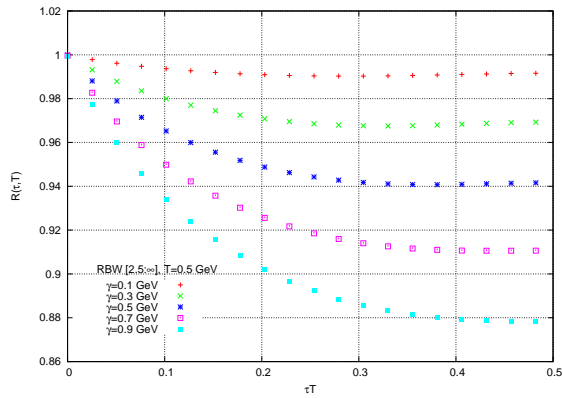
$$\sigma_r(\omega, T) = N(\gamma) f \frac{M}{\pi} \left\{ \frac{2\omega\gamma}{\omega^2\gamma^2 + (\omega^2 - M^2)^2} \right\}$$

$N(\gamma)$ assures normalization for width $\gamma = \gamma(T)$

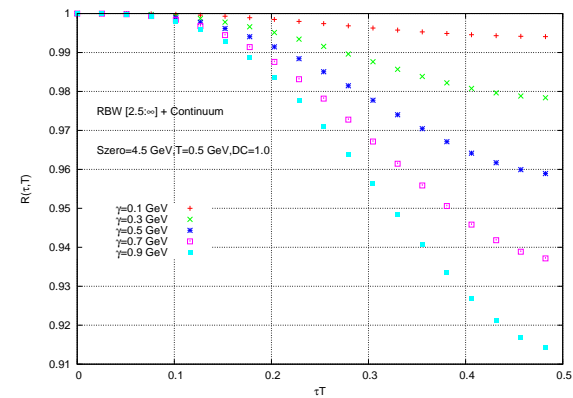
calculate correlator ratio $R(\tau, T) = G(\tau, T)/G_0(\tau, T)$

- using resonance contribution only, with $2 m_c \leq \omega$
- using resonance, with $2 m_c \leq \omega$, plus $T = 0$ continuum

[NB: no zero mode]



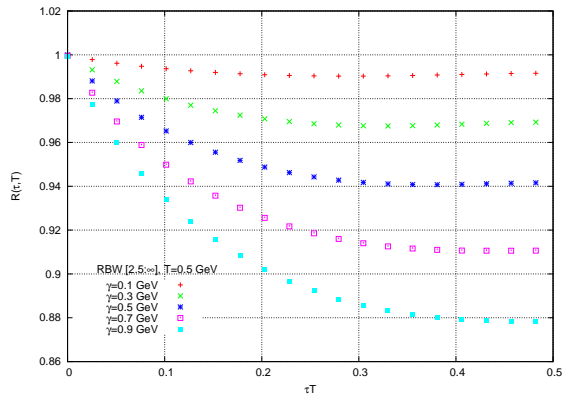
resonance only



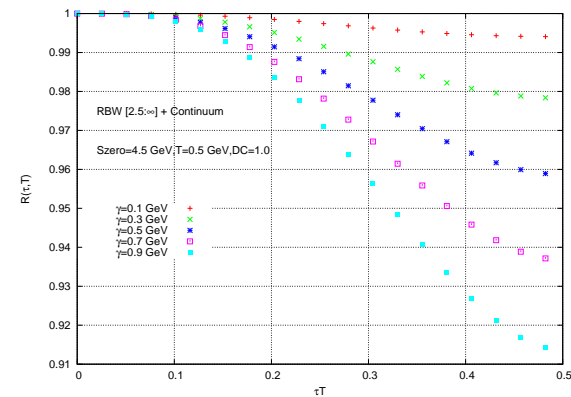
resonance + continuum

for $\gamma \leq 0.5 - 0.8 \text{ GeV}$ correlator ratio **decreases** with τ ,
but varies less than 10 %

conclusion: $R(\tau, T) \simeq 1$ compatible with resonance broadening
over wide range of widths



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continuum threshold \sim open charm threshold

for $T > T_c$, M_D decreases

(decrease with T of $F(T, r = \infty)$ in heavy quark lattice studies)

what happens for decreasing continuum threshold $s(T) < s_0$?

correlator ratio **increases**
rapidly with decreasing $s(T)$

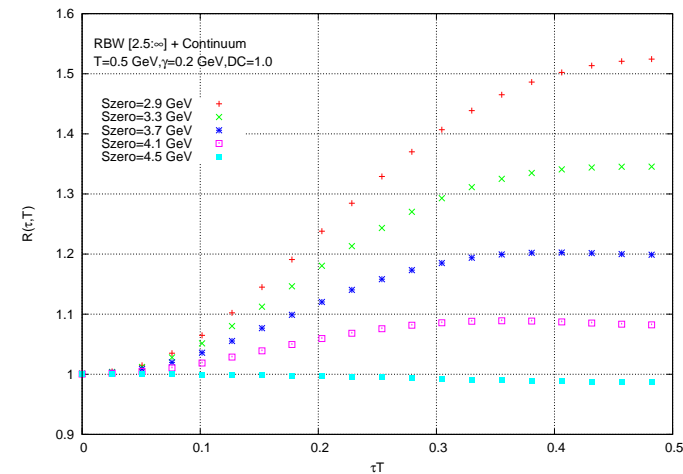
competing effects:

- increase $\gamma \Rightarrow R(\tau, T) \downarrow$
- decrease $s(T) \Rightarrow R(\tau, T) \uparrow$

decrease of continuum threshold affects χ_c at lower T
than J/ψ or η_c

hence possible; R_χ increases with τ
 $R_{J/\psi}$ decreases with τ

check in detail



Still missing:

$\omega = 0$ contribution to spectrum at $T \neq 0$:

c and \bar{c} annihilate & “heat the medium”

contribution to spectral function:

$$\sigma_0(\omega) = T a(T) \omega \delta(\omega)$$

crucial: T -dependence of $a(T)$

lattice studies use $\sigma(\omega, T < T_c)$, not $\sigma(\omega, T = 0)$

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we're tuning, stay tuned...

last word not yet known

\Rightarrow talk of Agnes Mocsy for alternative

